

# The ALLEE project – Linking thermodynamics and diffusion with materials properties

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V. Mohles

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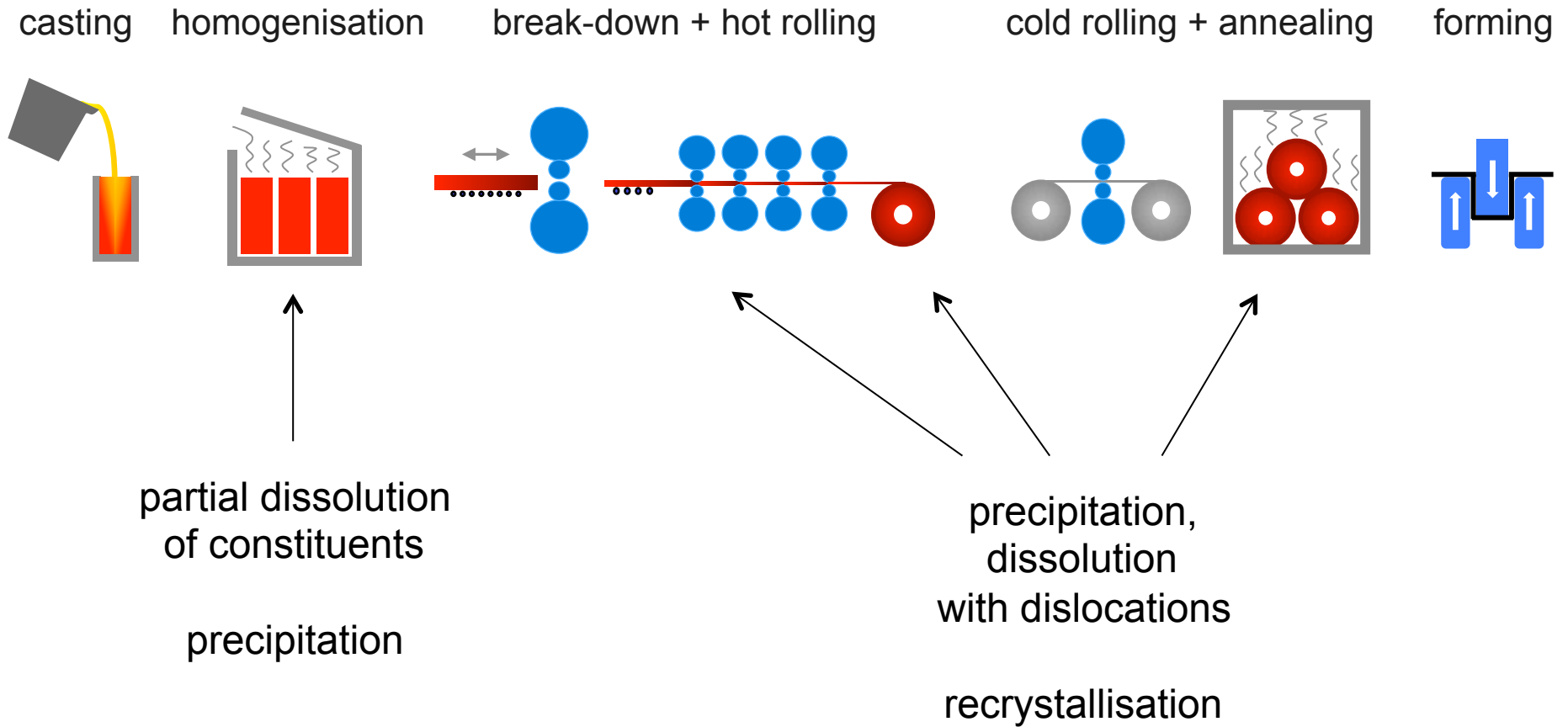
GTT user meeting, Herzogenrath, 2. - 4. 7. 2014

# Overview

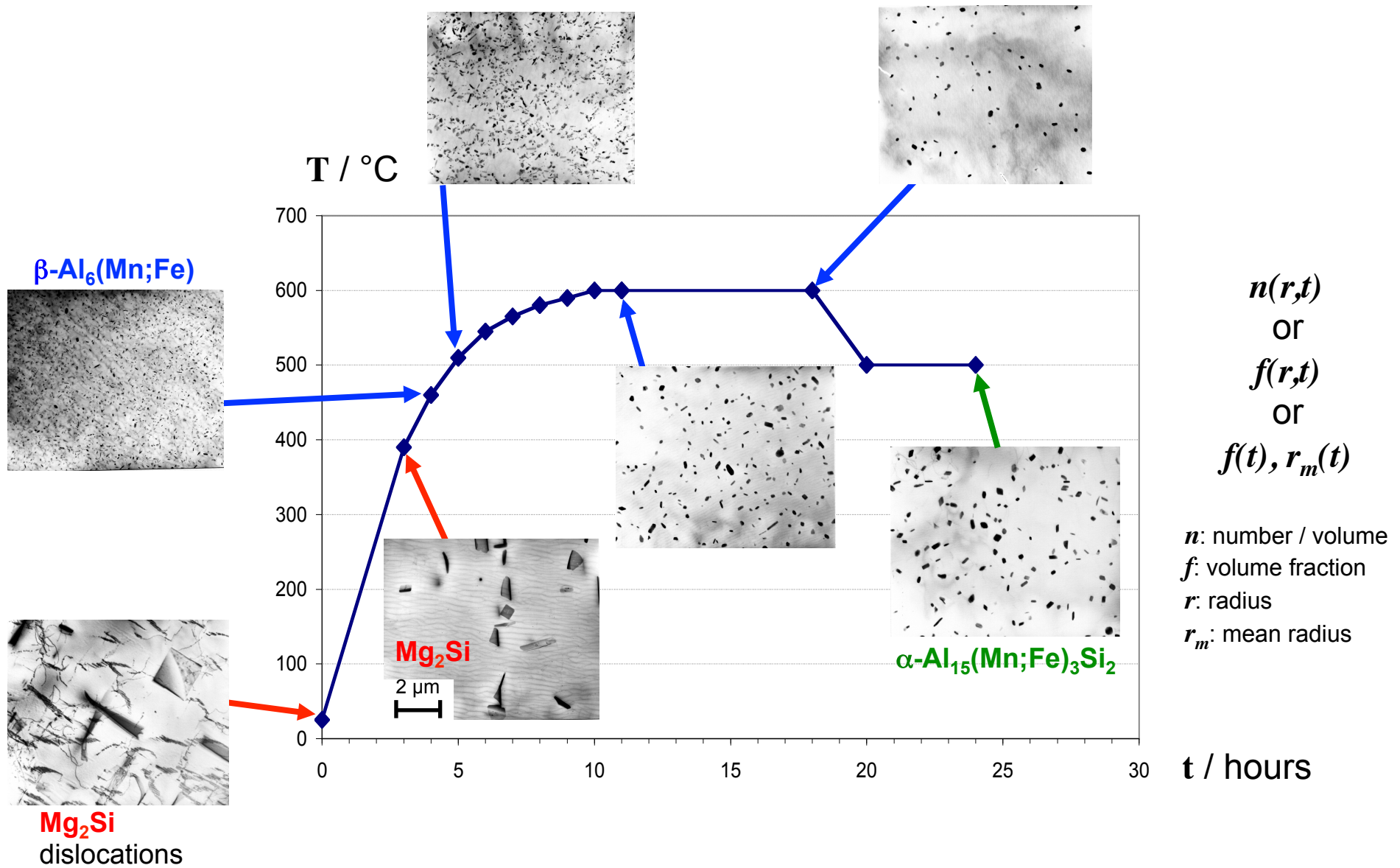
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- ::: ClANG model
- ::: ALLEE project

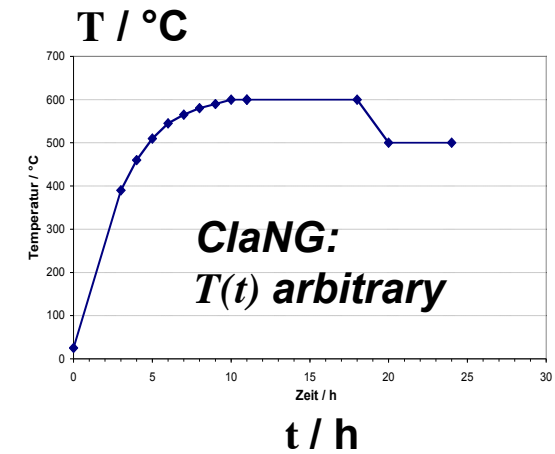
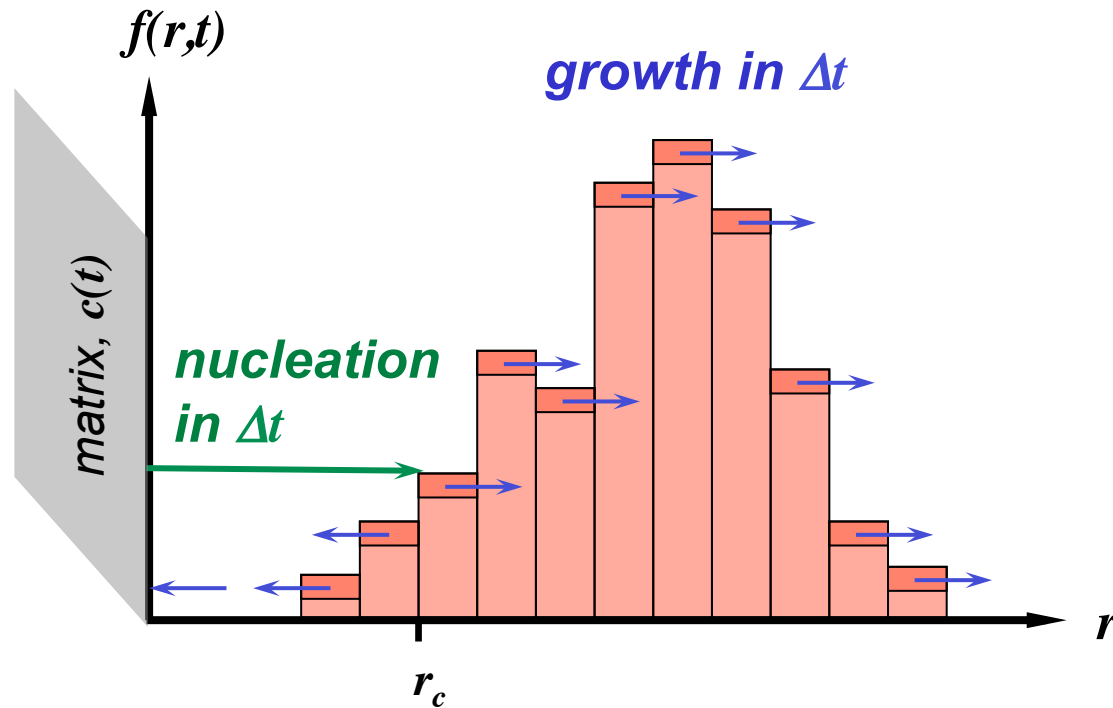
# Through process modelling



# Homogenisation AA3104



# Statistical precipitation: ClaNG

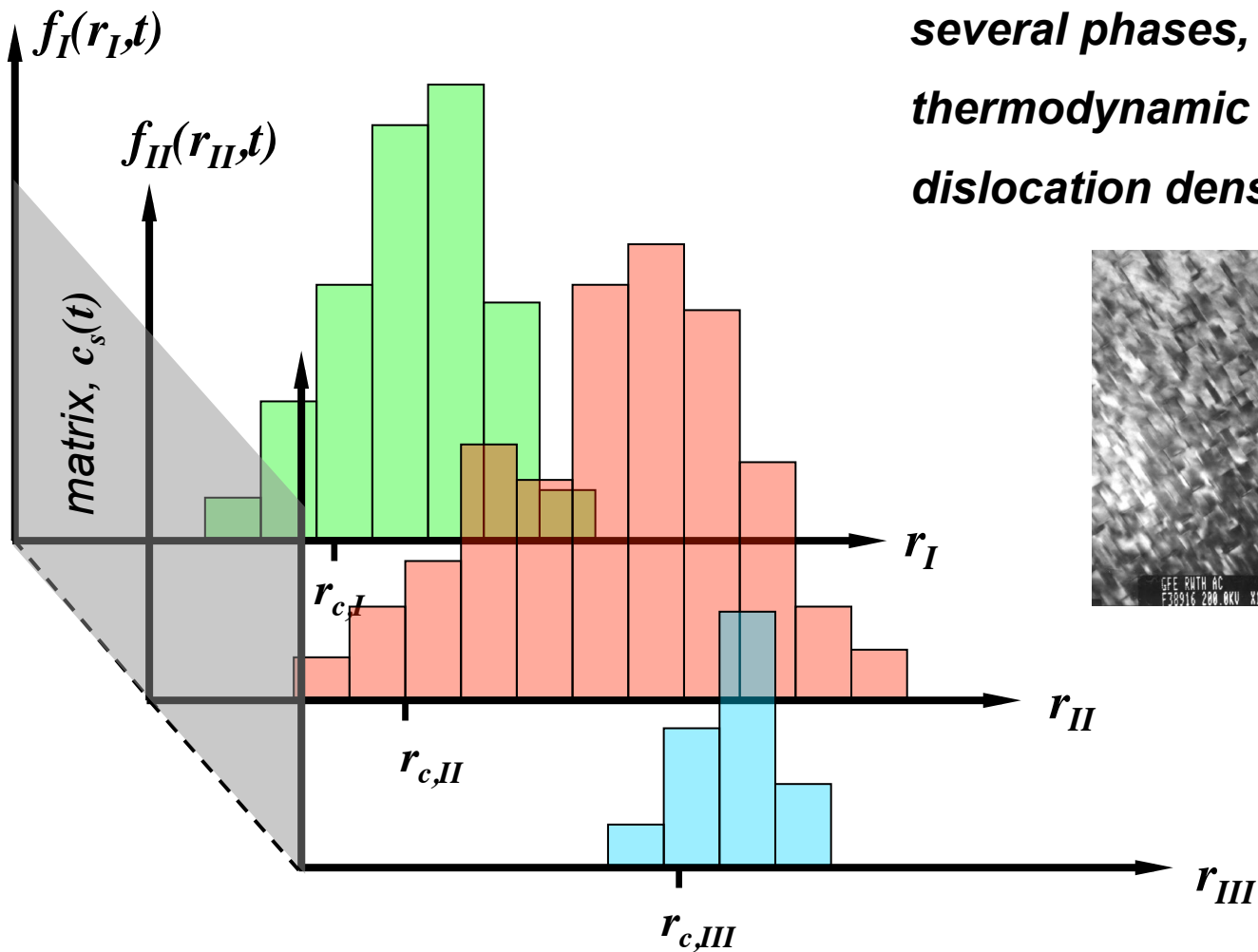


*generalized ansatz of Lifshitz, Slyozov; Wagner*

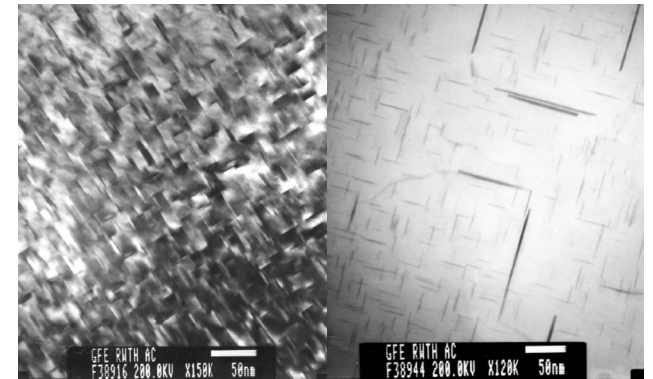
*nucleation rate  $dN/dt$*

*general temperature curve  $T(t)$  relevant for application*

# Statistical precipitation: ClaNG



*several phases, e.g.  $\alpha$ ,  $\beta$ ,  $Mg_2Si$*   
*thermodynamic data from database*  
*dislocation density  $\rho$  considered*

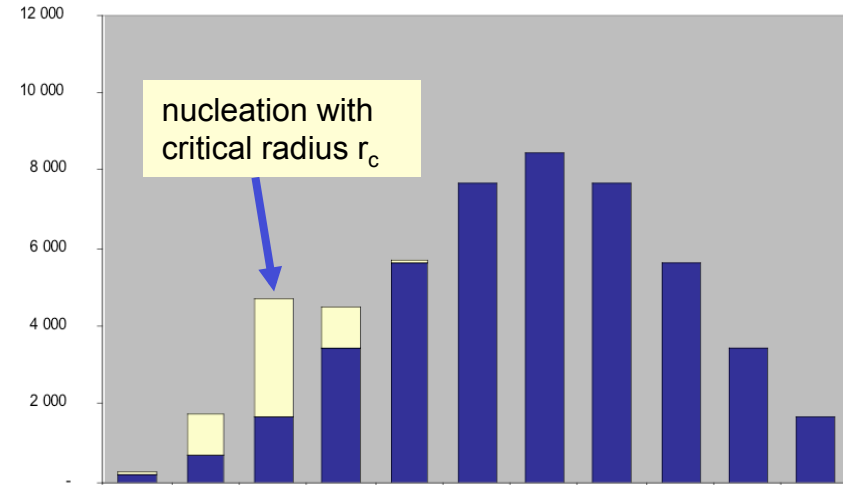
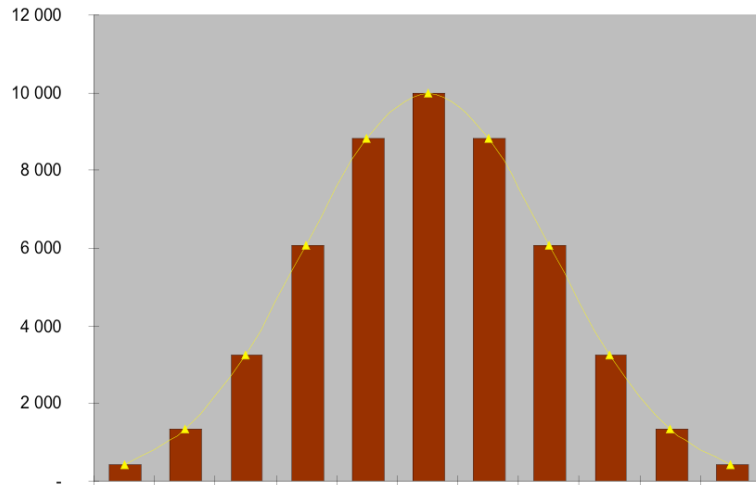


0% def.

8% def.

*several specific phases I, II, III, ... considered*

# Continuity / material conservation



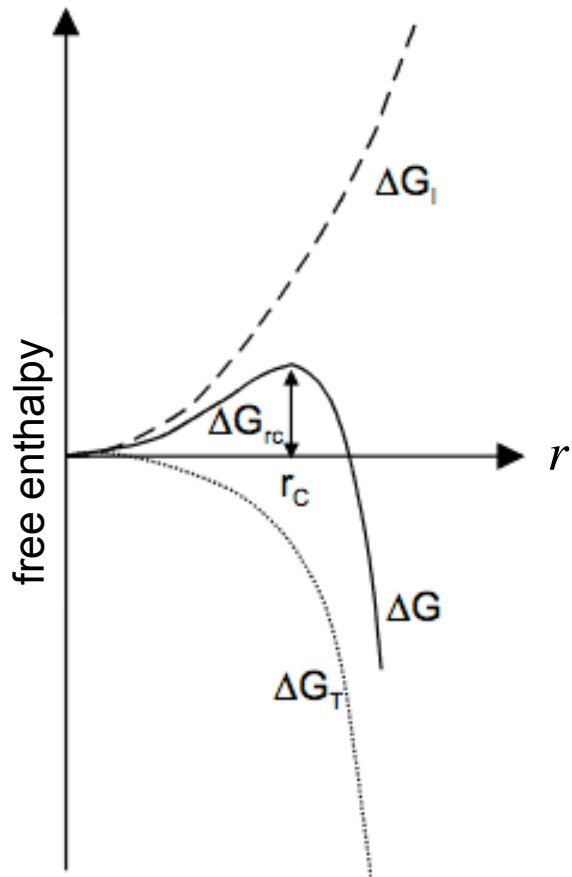
$$\frac{\partial f(r,t)}{\partial t} + \underbrace{\frac{\partial}{\partial r}(\dot{r} \cdot f(r,t))}_{\dot{r} \cdot \frac{\partial f(r,t)}{\partial r} + \frac{\partial \dot{r}}{\partial r} \cdot f(r,t)} = \dot{N}(t)$$

$$\dot{r} \cdot \frac{\partial f(r,t)}{\partial r} + \frac{\partial \dot{r}}{\partial r} \cdot f(r,t)$$

solved numerically with formulations for nucleation rate  $\dot{N}$   
and growth law  $\dot{r}$

# Nucleation

nucleation radius: from  $Max( -\Delta G_T(r) + \Delta G_i(r) + \Delta G_{elast}(r) )$



$$r_c = \frac{2\sigma_{nucl}}{\Delta g_T - \epsilon_{elast}} \approx K \frac{2\sigma}{\Delta g_T}$$

ChemApp  
GTT

$$\Delta g_T = g_{nucl}(c_{nucl}) - g_{matrix}(c_{matrix})$$

$\sigma$  = interface energy at  $r \rightarrow \infty$

$\sigma_{nucl}$  = interface energy at  $r = r_c$

$\epsilon_{elast}$  = elastic energy

$K$  - fit parameter

accounting for  $\sigma_n / \sigma$

and  $\epsilon_{el}$



# Nucleation

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**nucleation rate :**  $\dot{N}_{\text{total}} = \dot{N}_{\text{hom}} + \dot{N}_{\text{het}}$

$$\dot{N}(t) = N_0 \beta \exp\left(-\frac{\Delta G(r_c)}{kT}\right)$$

$N_0$  - site density

$N_{0,\text{hom}}$  : all atoms that can form precipitates

$N_{0,\text{het}}$  :  $\rho^{3/2}/2$  with  $\rho$ : dislocation density

$\beta$  - atomic attachment rate  $\beta = \text{Min}\left( 4\pi r_c^2 D(T) c(t) \lambda^{-4} \right)$

$D$  - bulk/pipe diffusion coefficient

$\lambda$  - lattice parameter

# Nucleation

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$$\dot{N}(t) = N_0 \beta \exp\left(-\frac{\Delta G(r_c)}{kT}\right) \cdot Z$$

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$Z$  - Zeldovich non-equilibrium factor  $Z = \sqrt{\frac{\Delta G(r_c)}{3\pi kT \cdot (n_{\text{in nucleus}}^{\text{atoms}})^2}}$

# Nucleation

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**nucleation rate :**  $\dot{N}_{\text{total}} = \dot{N}_{\text{hom}} + \dot{N}_{\text{het}}$

$$\dot{N}(t) = N_0 \beta \exp\left(-\frac{\Delta G(r_c)}{kT}\right) \cdot Z \cdot \exp\left(-\frac{\tau}{\Delta t}\right) = \beta^{-1} Z^{-2}$$

$N_0$  - site density

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$N_{0,\text{het}}$  :  $\rho^{3/2}/2$  with  $\rho$ : dislocation density

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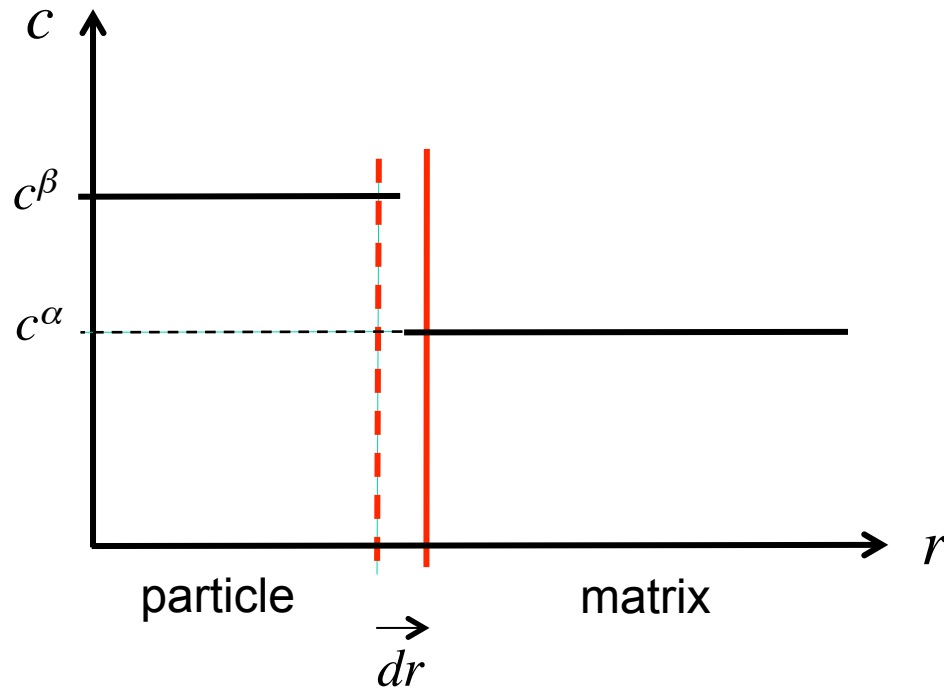
$Z$  - Zeldovich non-equilibrium factor  $Z = \sqrt{\frac{\Delta G(r_c)}{3\pi kT \cdot (n_{\text{in nucleus}}^{\text{atoms}})^2}}$

$\tau$  - incubation time to attain stable nucleation

$\Delta t$  - time after phase reaches stability

# Growth, ripening

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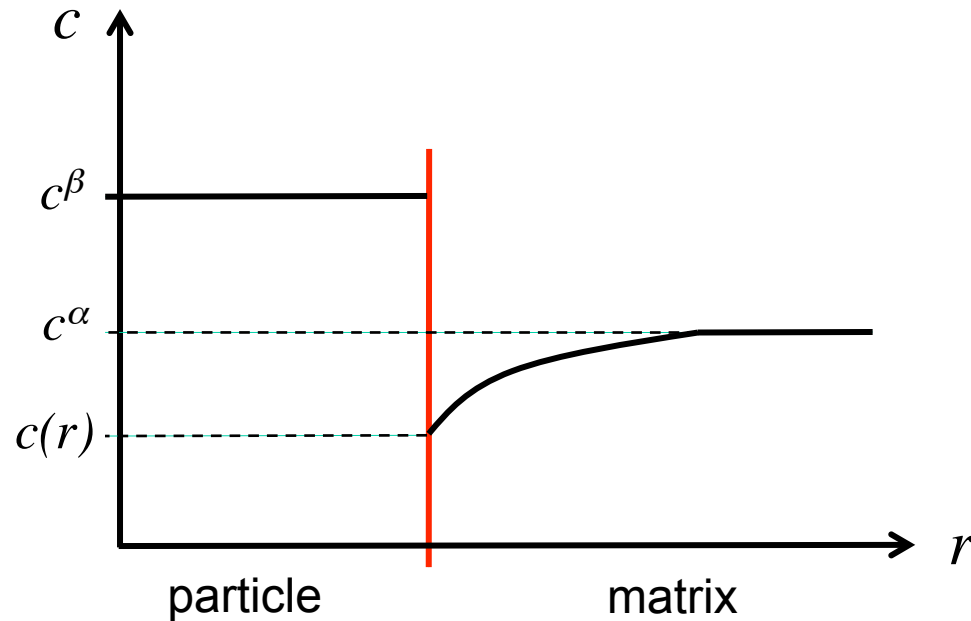
$$(c^\beta - c^\alpha) dr = j dt$$

$c^\alpha$  = atom density in matrix  $\alpha$

$c^\beta$  = atom density in phase  $\beta$

$j$  = atoms current density

# Growth, ripening



$$4\pi r^2 (c^\beta - c(r)) \frac{dr}{dt} = J$$

$c^\alpha$  = atom density in matrix  $\alpha$

$c^\beta$  = atom density in phase  $\beta$

$J$  = atom current to be provided

atom current provided:

$$J = 4\pi R^2 D \left. \frac{dc}{dR} \right|_R \Rightarrow \text{Zener's growth law for binary alloys: } \frac{dr}{dt} = \frac{D}{r} \frac{c^\alpha - c(r)}{c^\beta - c(r)}$$

# Growth, ripening

Gibbs-Thomson concentration at the interface:

$$c_i^{\alpha/\beta}(r) = c_i^{\alpha/\beta}(\infty) \cdot \exp\left(\frac{2\sigma V_a}{r \cdot kT}\right)$$

$$\frac{2\sigma V_a}{r} = kT \ln\left(\frac{c_i^{\alpha/\beta}(r)}{c_i^{\alpha/\beta}(r \rightarrow \infty)}\right)$$

Gibbs energy  
enhancement  
of the particle

Gibbs energy  
enhancement  
in the matrix

$$\frac{2\sigma V_a}{r} = \sum_i c_i^\beta \cdot kT \ln\left(\frac{c_i^{\alpha/\beta}(r)}{c_i^{\alpha/\beta}(r \rightarrow \infty)}\right) \left. \vphantom{\frac{2\sigma V_a}{r}} \right\} \frac{2\sigma V_a}{r} = \sum_i c_i^\beta \cdot kT \ln\left(\frac{1 - f(r) \frac{c_i^\beta}{c_i^\alpha}}{1 - f(r)}\right)$$

$$c_i^\alpha = (1 - f(r)) c_i^{\alpha/\beta}(r) + f(r) c_i^\beta$$

## Growth, ripening

$$\frac{2\sigma V_a}{r} + \Delta g_T = \sum_i c_i^\beta \cdot kT \ln \left( \frac{1 - f(r) \frac{c_i^\beta}{c_i^\alpha}}{1 - f(r)} \right)$$

fitted function:  $h = 1 - (r_c / r)^a$

numerically resolved for  $f(r)$ :  $f(r) = f_{\max} \cdot h(r / r_c)$        $f_{\max} = \frac{c_i^\alpha - c_i^{\alpha/\beta}(\infty)}{c_i^\beta - c_i^{\alpha/\beta}(\infty)}$

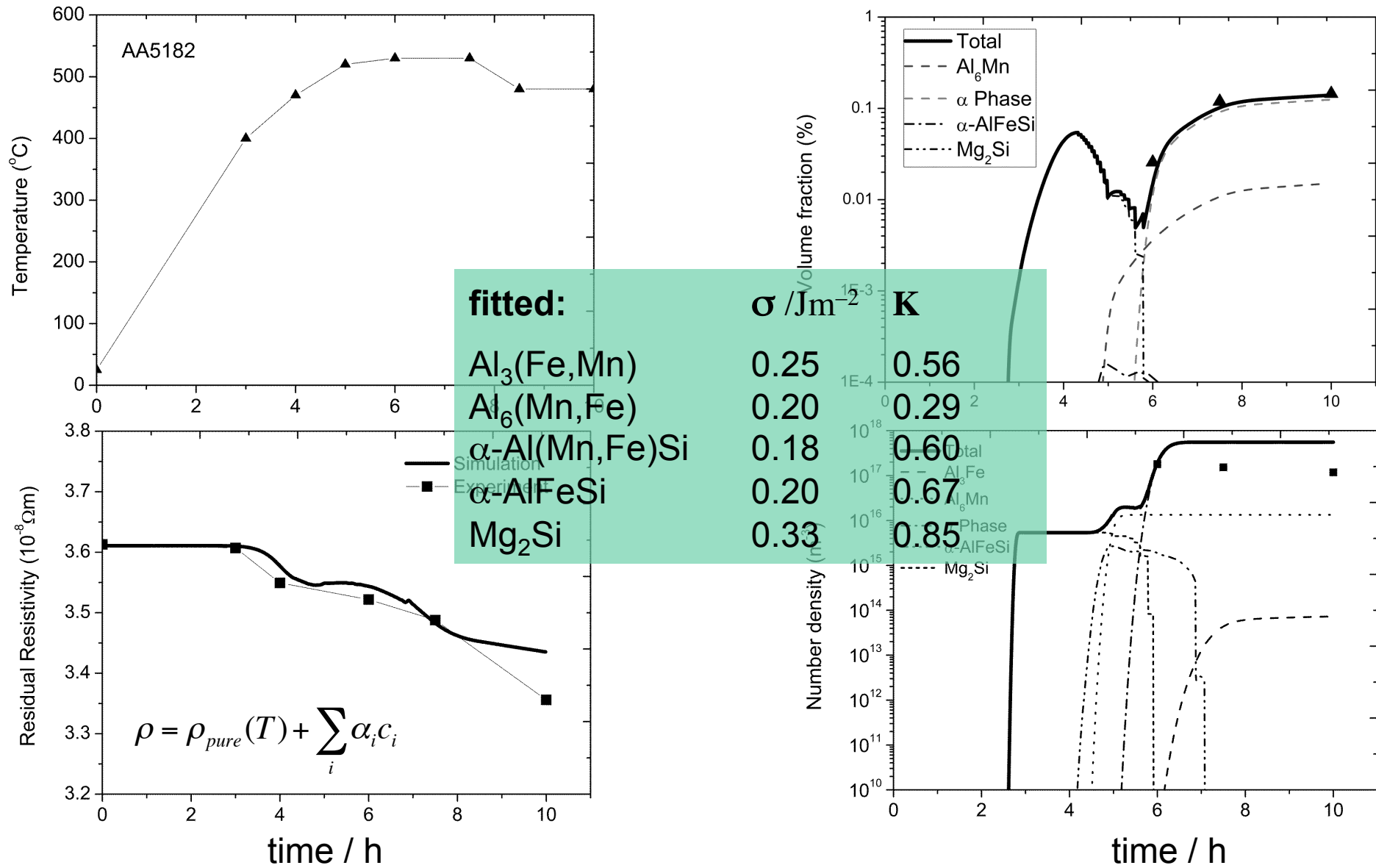
from mass conservation:  $f(r) = \frac{c_i^\alpha - c_i^{\alpha/\beta}(r)}{c_i^\beta - c_i^{\alpha/\beta}(r)}$

compare with Zener's law:  $\frac{dr}{dt} = \frac{c^\alpha - c^{\alpha/\beta}(r)}{c^\beta - c^{\alpha/\beta}(r)} \frac{D}{r}$

$\Rightarrow$  growth law:  $\frac{dr}{dt} = \frac{D}{r} f(r) = \frac{D}{r} f_{\max} h(r / r_c)$

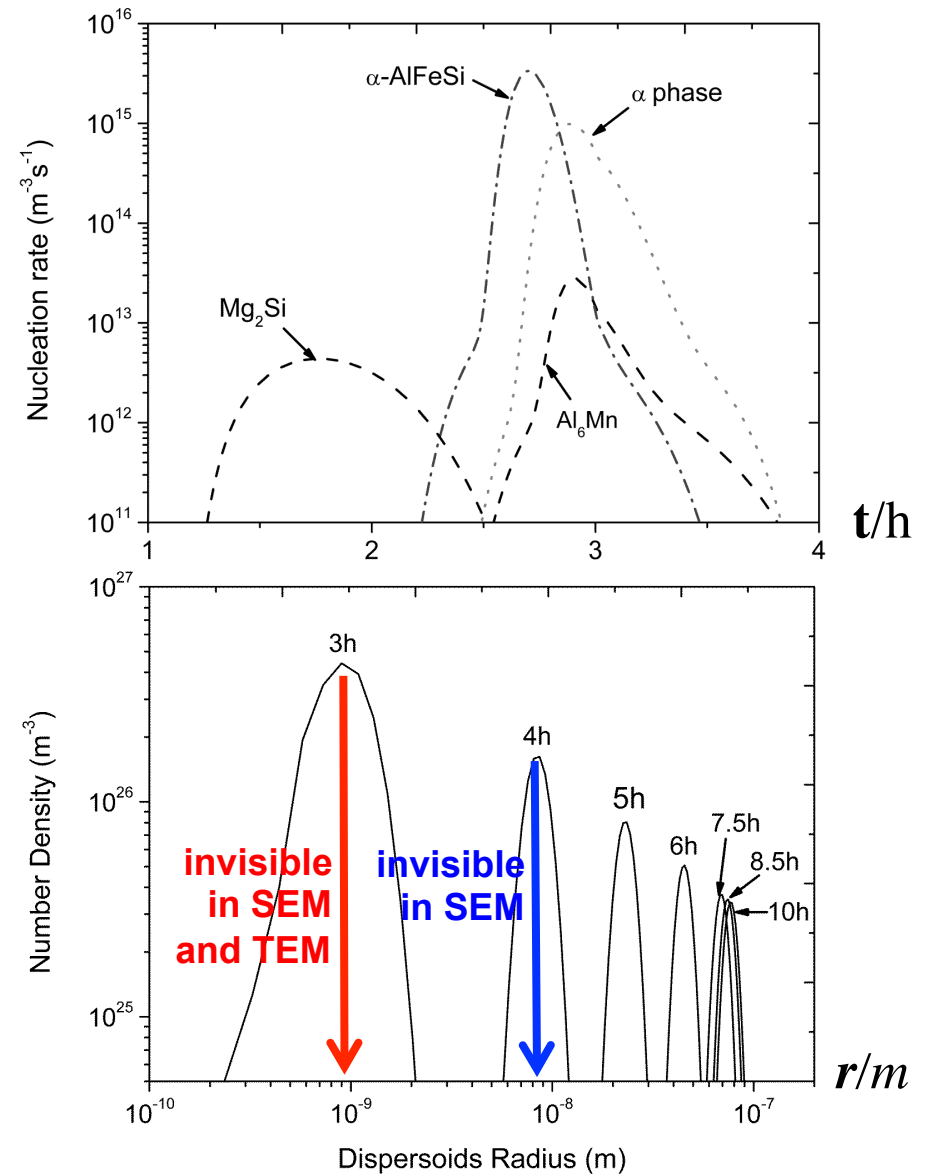
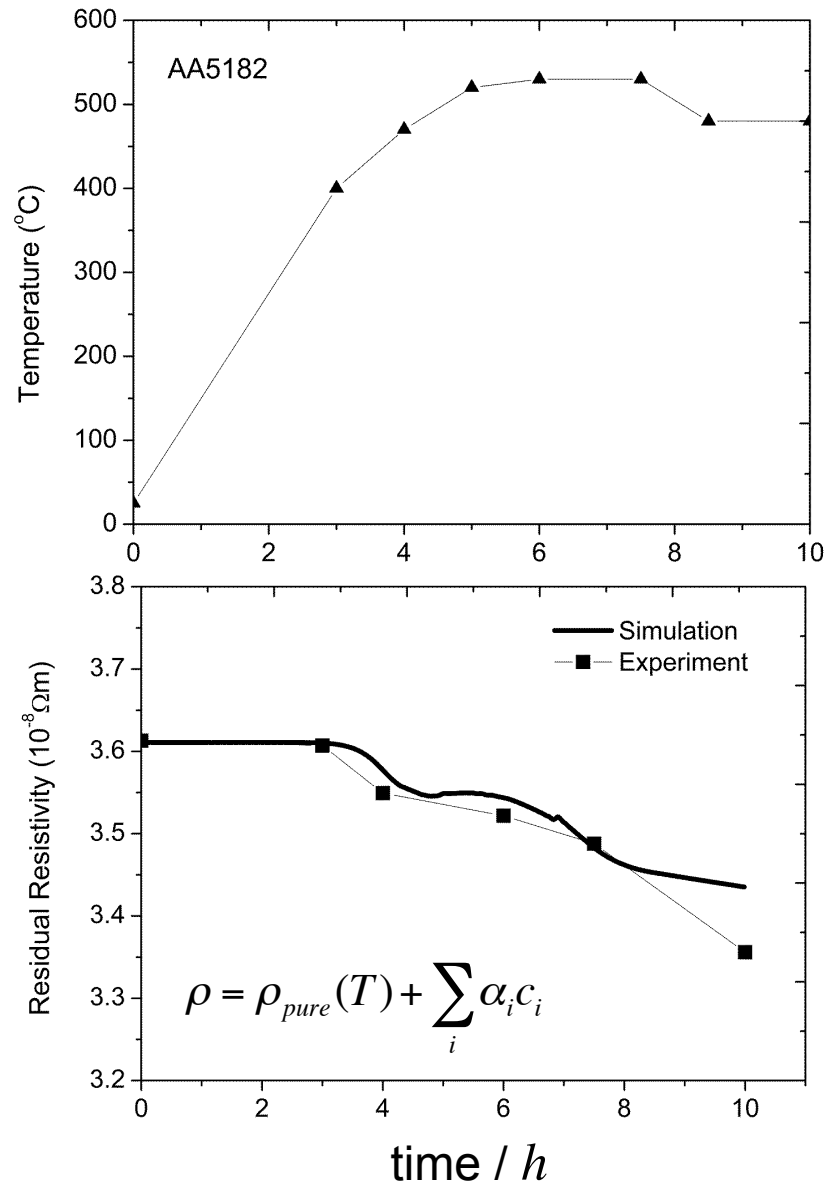
with  $D = \text{Min}(D_i^{\text{bulk}}(T) + (\rho / \rho_0) D_i^{\text{pipe}}(T))$

# ClanG+, AA5182: calibration

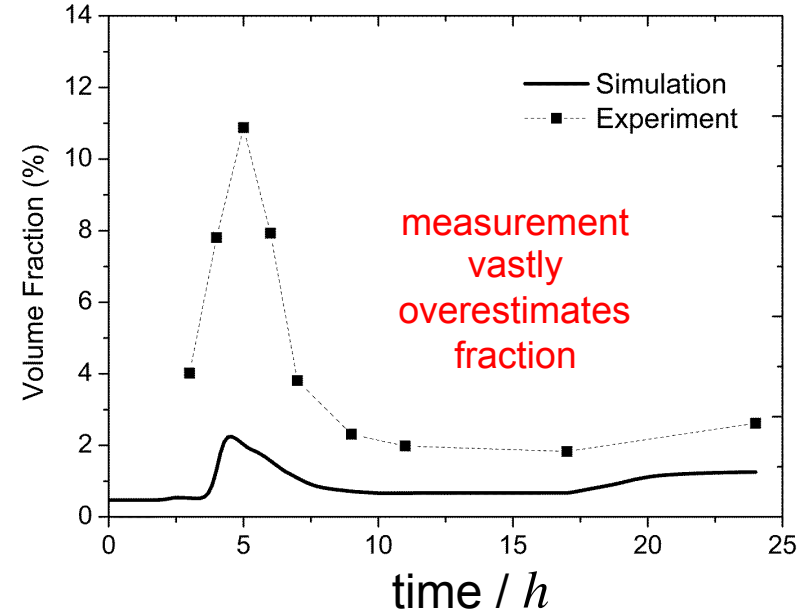
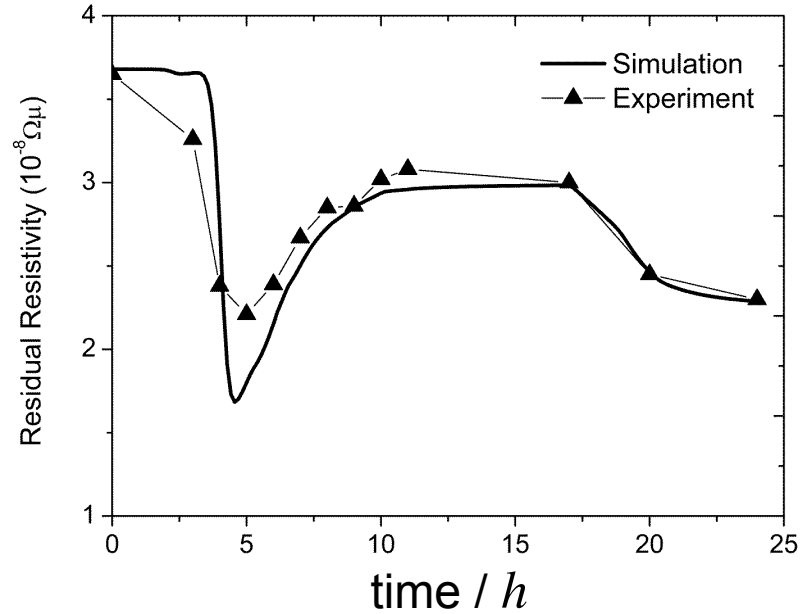
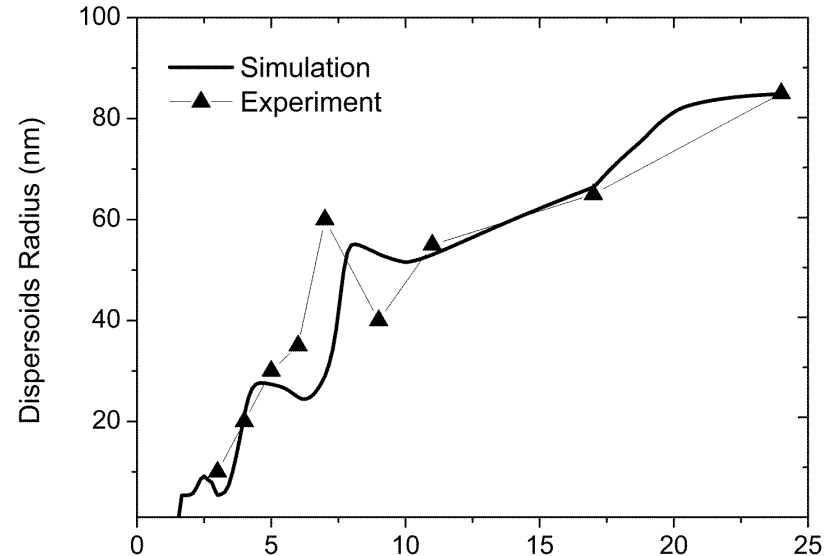
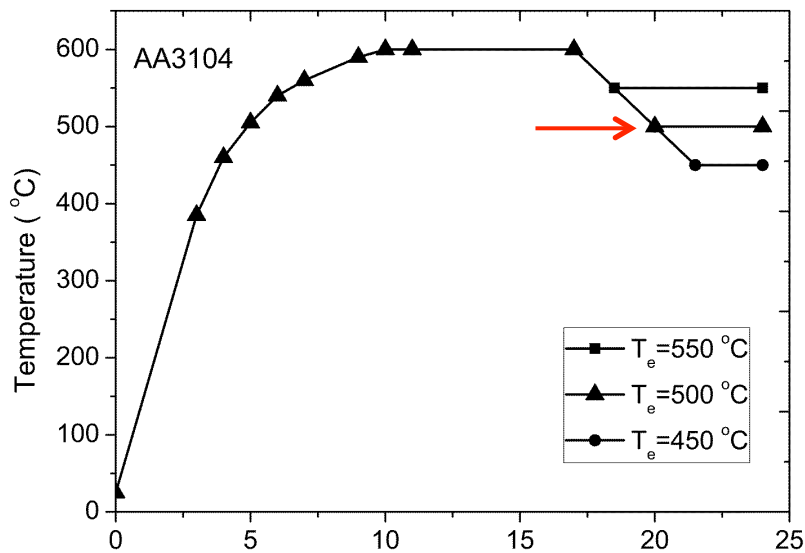




# ClANG+, AA5182: nucleation



# ClaNG+, AA5182 calibrated; AA3104 predictions



# Overview

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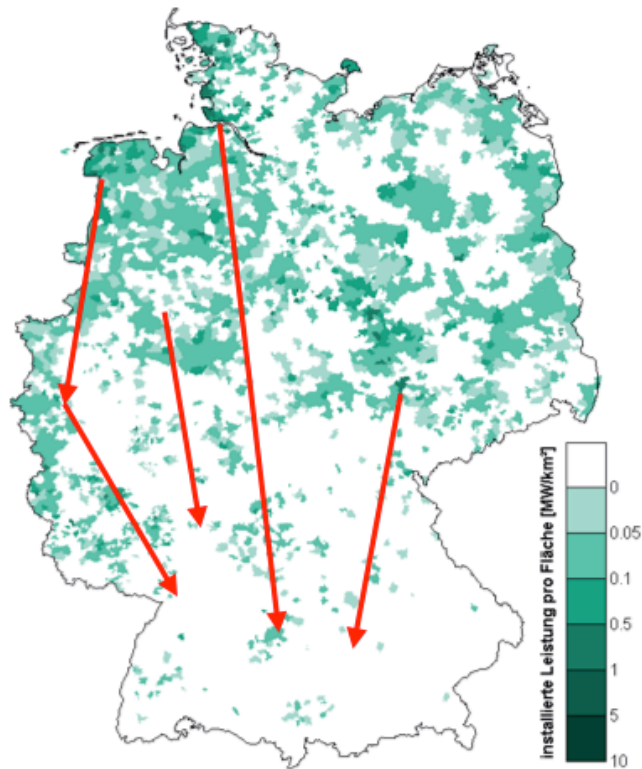
- ::: ClANG model
- ::: ALLEE project

# BMBF project: ALLEE

BMBF: Support initiative „Zukunftsfähige Stromnetze“

topics: transmission and distribution techniques

⇒ „Langzeitstabile Aluminiumlegierungen für elektrische Verbindungen“



44 GW of wind energy produced in the north  
to be transferred to the energy hungry south

Copper:  $16.7 \cdot 10^{-9} \Omega\text{m}$  (@RT)

Aluminium:  $26.5 \cdot 10^{-9} \Omega\text{m}$  (@RT)  
but cheaper  
known problem: creep resistance

requested: application temperature  $140^\circ\text{C}$   
period of use: 50 a

Abb. 1: Onshore-Windleistung [Fraunhofer  
IWES 2011] und geplante Energieautobahnen  
[\[www.netzentwicklungsplan.de\]](http://www.netzentwicklungsplan.de)

# BMBF project: ALLEE

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## „Langzeitstabile Aluminiumlegierungen für elektrische Verbindungen“

- management:** Prof. Dr.-Ing. O. Kessler  
Lehrstuhl für Werkstofftechnik, Universität Rostock
- partners:** Prof. Dr.-Ing. Thomas Schoenemann  
Lehrst. f. Hochspannungs- u. Hochstromtechnik, Universität Rostock
- Prof. Dr.-Ing. Steffen Großmann  
Inst. f. Elektr. Energieversorgung u. Hochspannungstechnik, TU Dresden
- PD. Dr. Volker Mohles  
Institut für Metallkunde und Metallphysik, RWTH Aachen University
- Prof. Dr. Jürgen Hirsch  
Hydro Aluminium Rolled Products GmbH, F&E, Bonn
- Prof. Dr. Klaus Hack  
Ges. für Technische Thermochemie und –physik mbH, Herzogenrath
- start (?):** September 2014

# Requirements for ALLEE alloys

**low resistivity:** 
$$\rho(T) = \rho_{Al}(T) + \sum_x c_x^{sol} \rho_x$$

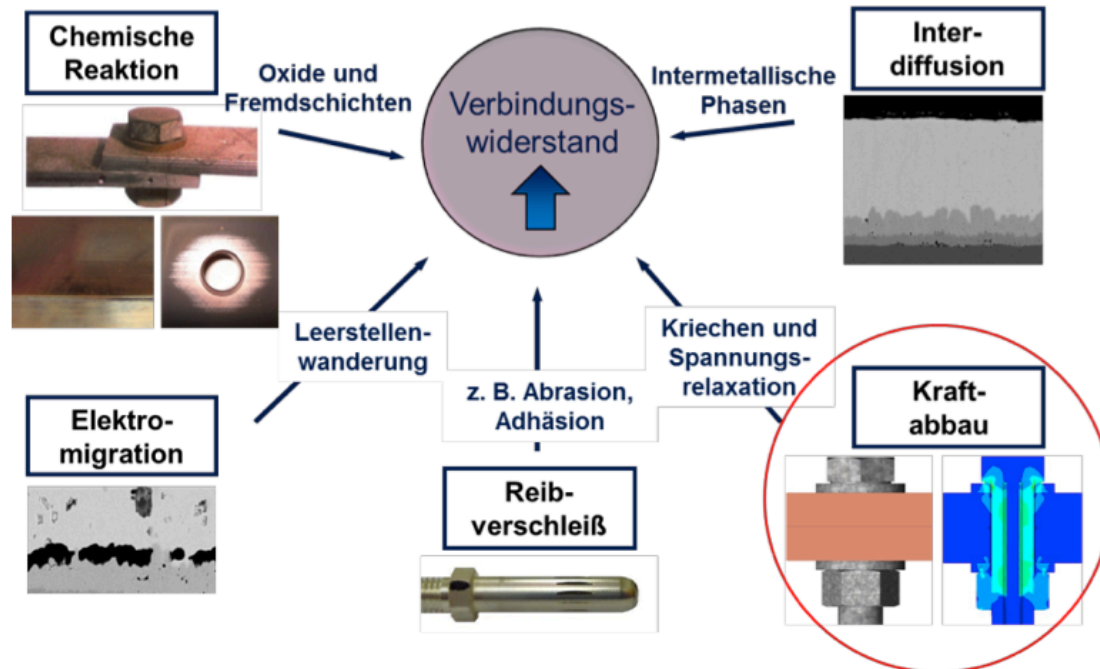
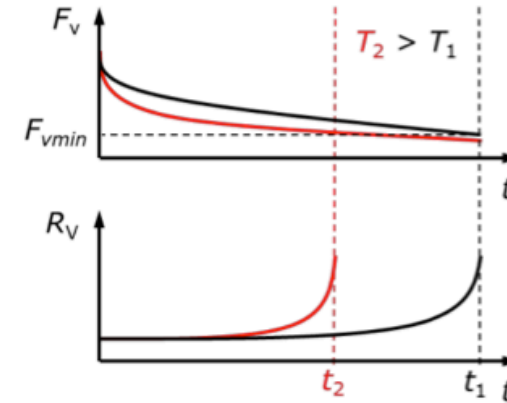
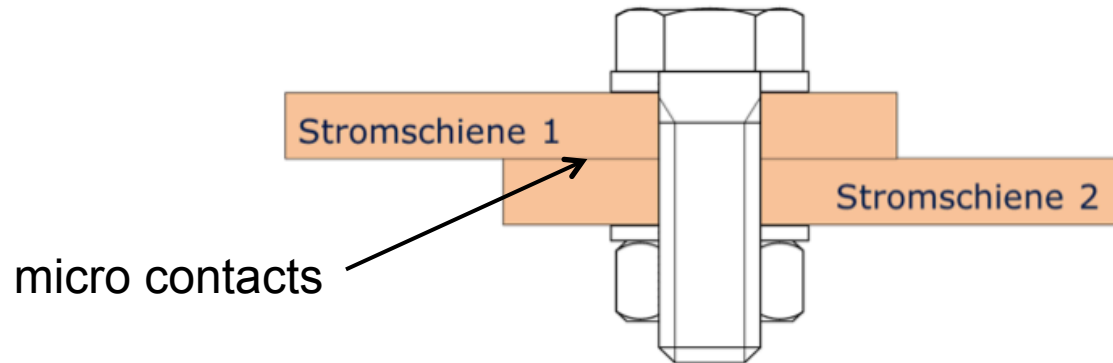
low solute concentration!

diffusion coefficient in Al,      solubility at 140°C

Element		$D_x / m^2/s$	$c_{max} / wt\%$	$\rho_x(1wt\%) / (10^{-9}\Omega m)$	$\rho_{Al} + \rho_x(max\%)$
Al		$1,67 \cdot 10^{-22}$		40 (100%, 140°C)	
Cr	Dispers. bildend	$1,86 \cdot 10^{-33}$	<< 1% 0.3% übers.	42	53 (0.3wt%)
Cu		$4,12 \cdot 10^{-22}$	<< 1%	3,0	40
Fe	Dispers. bildend	$3,38 \cdot 10^{-26}$	<< 1%	32	40
Mg		$3,99 \cdot 10^{-21}$	2%	5,5	51 (2wt%)
Mn	Dispers. bildend	$1,91 \cdot 10^{-29}$	<< 1% 0.3% übers.	38 / 36	51 (0.3wt%)
Ni	Dispers. bildend	$1,51 \cdot 10^{-22}$	<< 1%		
Si		$7,48 \cdot 10^{-21}$	<< 1%	6,5	40
Ti		$1,55 \cdot 10^{-34}$	<< 1%	31	40
Zr	Dispers. bildend	$1,80 \cdot 10^{-32}$	<< 1%		

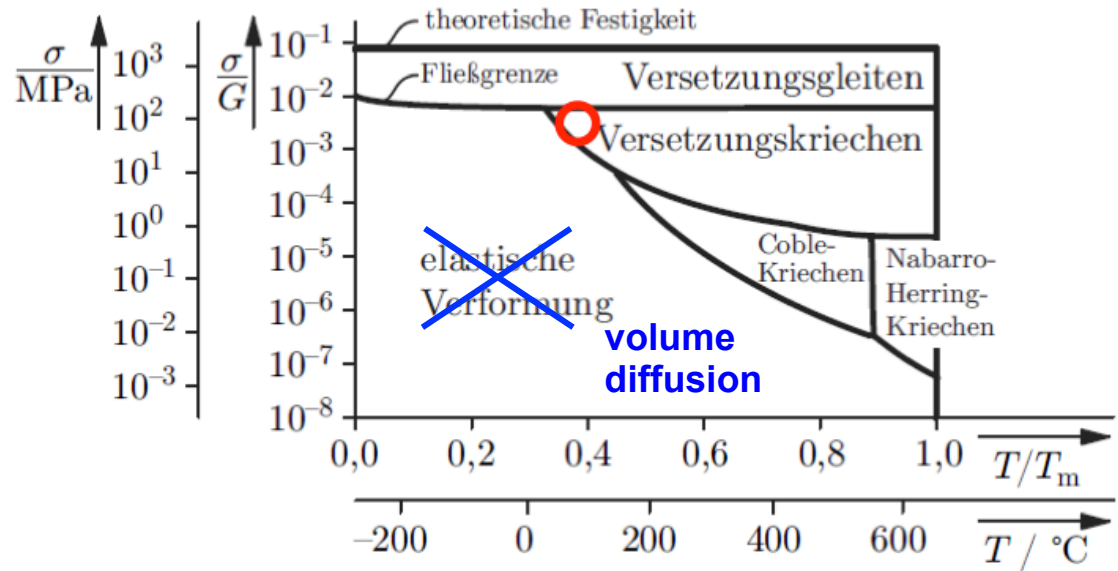
# Requirements for ALLEE alloys

high creep resistance



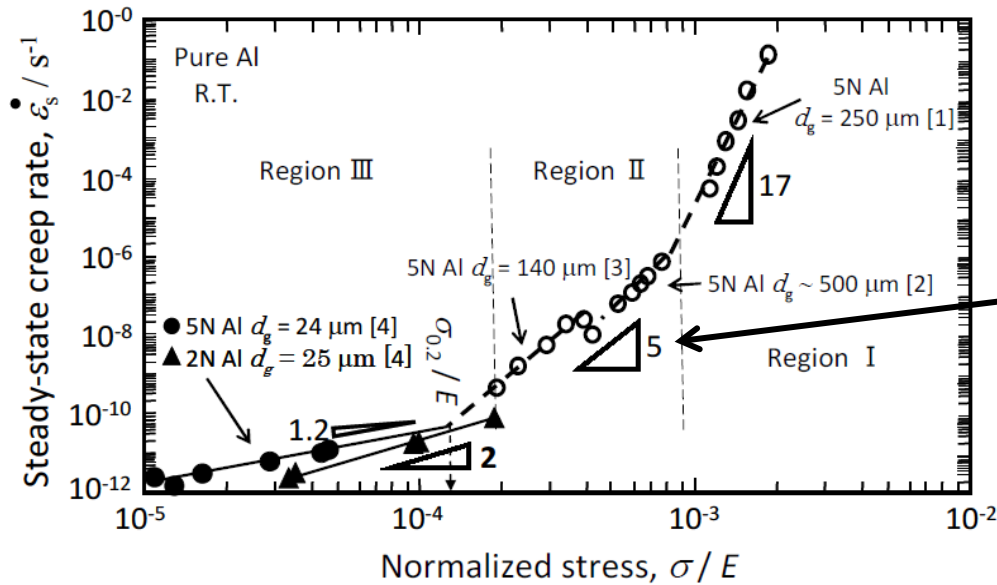
# Requirements for ALLEE alloys

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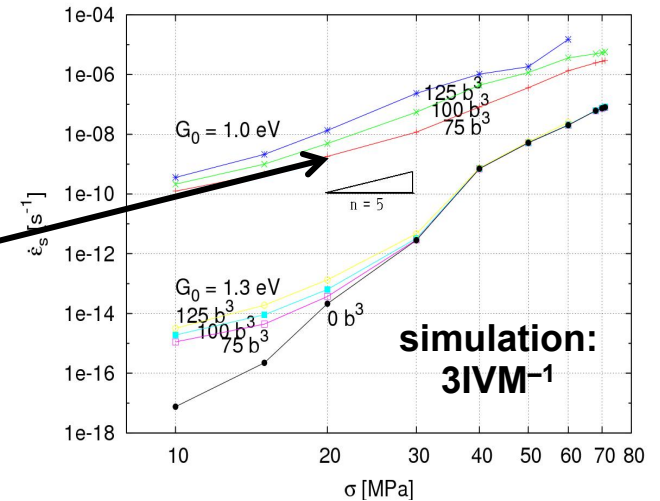


steady state creep

Materials Science Forum  
747-748 (2013) pp559-563



$$\dot{\epsilon} \sim \sigma^5$$



simulation:  
3IVM-1



# Requirements aggravation

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## applied so far:

stock alloys (AA1xxx) optimized for mechanical applications/purposes  
selected for low electrical resistivity

## future requirements:

increased temperature: 90°...110°C → 140°C  
increased currents / higher energy/power density / compact design  
increased life time / reduced down time (maintenance)  
increased strength to withstand electromagnetic forces (short circuit!)  
extreme environmental conditions (e.g. offshore)

## potential for optimized alloys:

large grains etc. - dislocations, grain boundaries not stable  
precipitates! - stable phases, aging slowly at 140°C  
- but forming fast enough during production  
→ selection of ideal alloying elements and contents  
- production route should ensure full precipitation  
→ optimization of the processing route

## project structure

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specification:	operating conditions, definition of test methods
alloy development:	<b>alloy selection</b> (initial and iterations) thermodynamic calculations (GTT) <b>precipitation modelling</b> : ClaNG (IMM)
alloy production:	primary shaping, homogenization, forming (Hydro)
characterization:	microstructure, calorimetry (LWT), mechanical properties electrical properties
long term experiments:	without current (HHT), with current (IEEH)
modelling an simulation:	<b>material model for creep</b> (IMM) system model (IEEH, LWT) ClaNG database extension (GTT)
evaluation:	including norming concept

# Alloy selection

Element		$D_x / \text{m}^2/\text{s}$	$c_{\text{max}} / \text{wt}\%$	$\rho_x(1\text{wt}\%) / (10^{-9}\Omega\text{m})$	$\rho_{\text{Al}} + \rho_x(\text{max}\%)$
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- 1) start with good **element candidates within the validated database**
- 2) look for better candidates
  - stability / resistivity
  - production feasibility, material and production cost, ...
- 3) extend database (GTT)
- 4) ClaNG simulations for application and production conditions

# Summary

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**::: ClaNG can deliver valuable information for other models:**

- recrystallisation
- particle / solute strengthening → creep
- texture predictions
  
- resistivity

**::: information about  $\Delta g_T$  and equilibrium solute concentrations from database,**

- to be extended towards other elements / phases
- planned: database for interface energies

**::: the ALLEE project will be a new big playground to utilize ClaNG**