

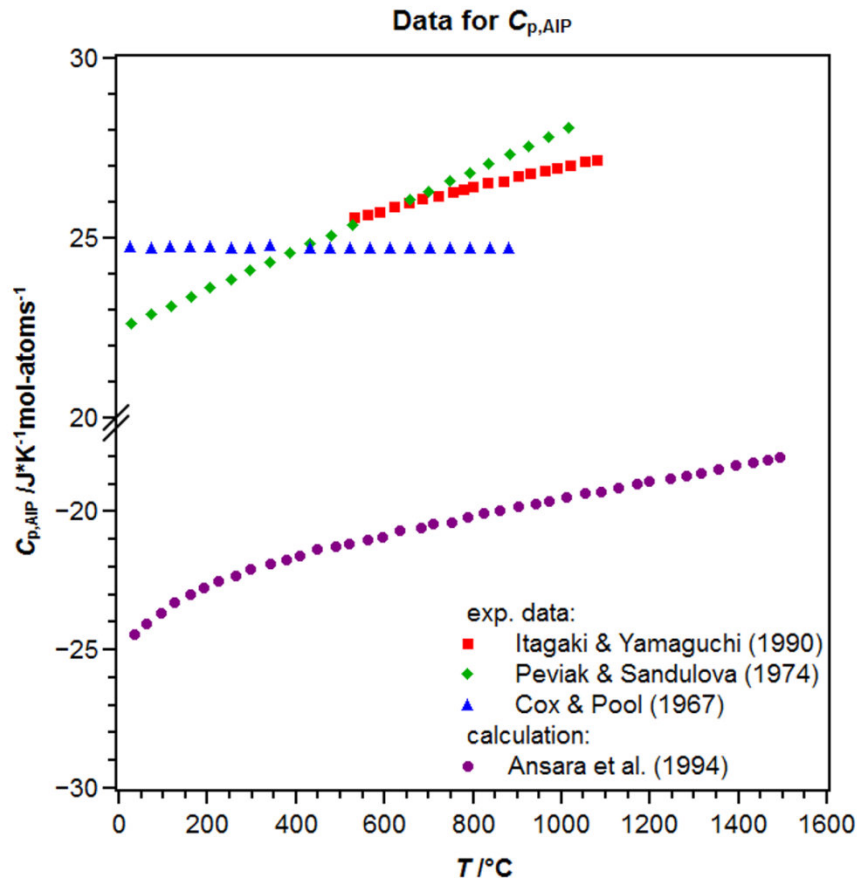
Reassessing the reassessment of the AI-P System

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System Al-P: Ansara et al.

description of Ansara et al. [94Ans] produces *negative* values of $c_p(\text{AIP})$ over the whole T-range.



exp. data:

Cox & Pool \Rightarrow constant,
data for low T

Peviak & Sandulova
 \Rightarrow linear, positive slope,
data for low T

Itagaki & Yamaguchi
 \Rightarrow linear, positive slope,
limited T-range

[94Ans]:

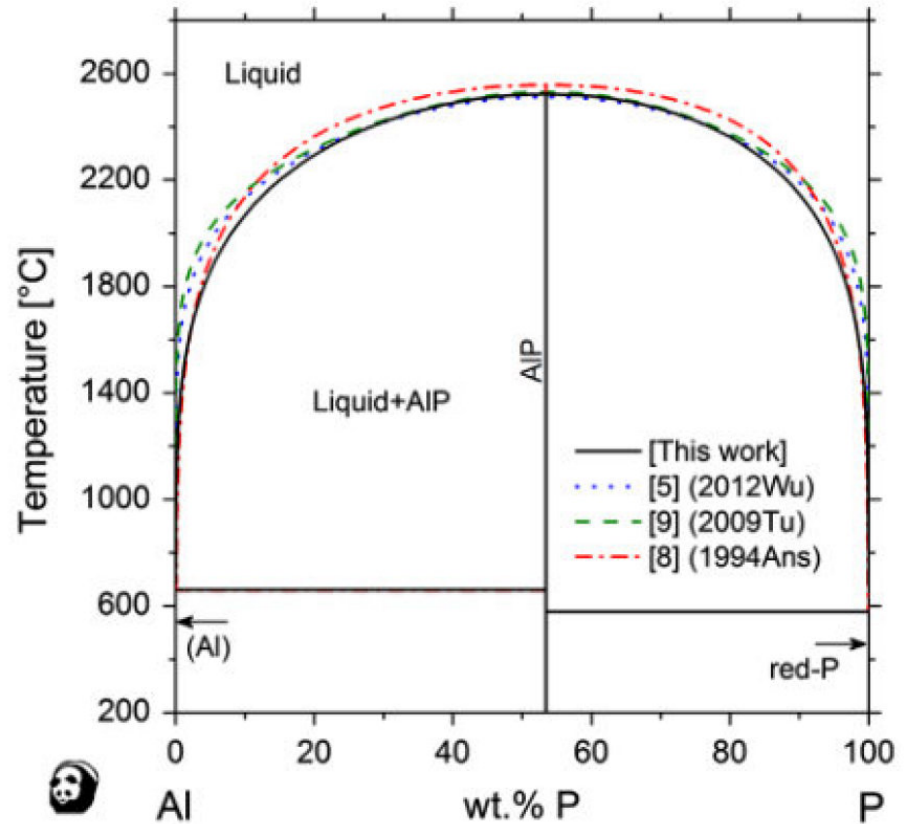
L. Ansara, C. Chatillon, H.L. Lukas,
T. Nishizawa, H. Ohtani, K. Ishida,
M. Hillert, B. Sundman, B.B. Argent,
A. Watson, T.G. Chart, T. Anderson,
Calphad 18 (1994) 177

System Al-P: Liang & Schmid-Fetzer

new thermodynamic assessment in:

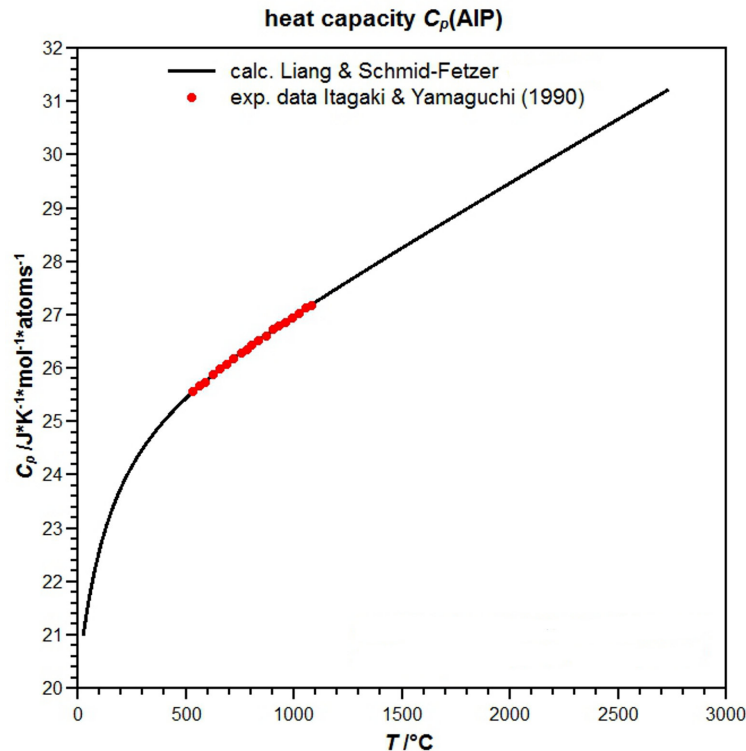
S.-M. Liang, R. Schmid-Fetzer, Calphad **42** (2013) 76-85

authors go back to original experimental data. Only external data used are from SGTE Unary. However, there are no gas data in SGTE Unary !



System Al-P: Liang & Schmid-Fetzer

new thermodynamic description of AlP:

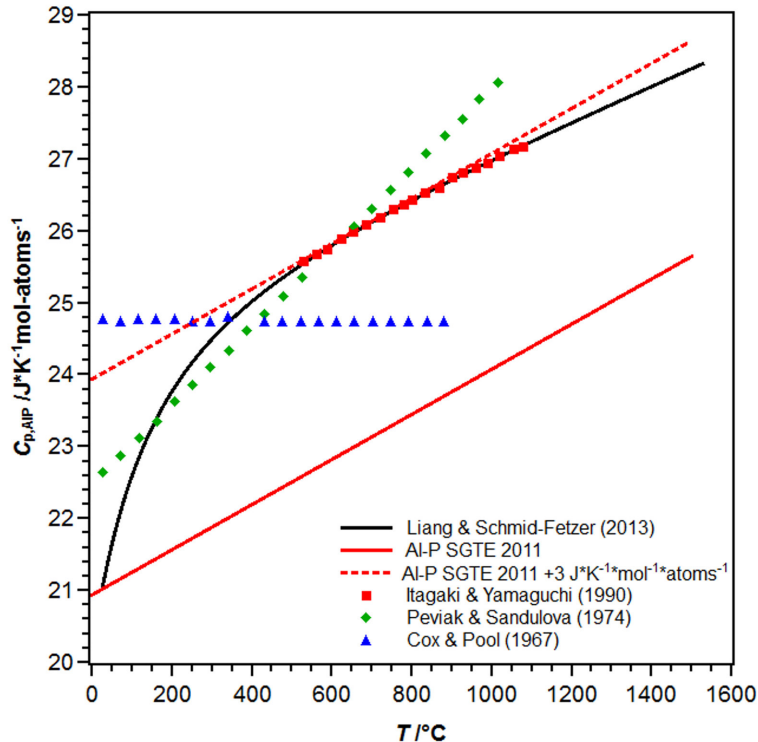


exp. data from
Itagaki & Yamaguchi
considered best by
Liang & Schmid-Fetzer,
curve fits data excellently

$$C_P^{\text{AlP}} = 48.4 + 4.7 \cdot 10^{-3} T - 690000 \cdot T^{-2}$$

System Al-P: Liang & Schmid-Fetzer

comparison of $c_p(\text{AIP})$



c_p - curves of Ansara & Schmid-Fetzer show similar shape

$c_p(\text{AIP}), \text{Ansara} + \text{const.},$
 $c_p(\text{AIP}), \text{SGTE 2011} + \text{const}'.$
fit well exp. data from Itagaki & Yamaguchi

System Al-P: Liang & Schmid-Fetzer

thermodynamic modeling of **liquid phase**:

LIQUID (Al,P)₁:

$$G_i^{0,liq}(T) = G_i^{liq}(T) - H_i^{SER} \\ = a + b \cdot T + c \cdot T \ln T + d \cdot T^2 + e \cdot T^3 + f \cdot T^{-1} + g \cdot T^7 + h \cdot T^{-9}$$

$i = \text{Al,P}$; G -functions according to SGTE [91Din].

Regular liquid interaction using exp-function as proposed by Kaptay to prevent inverse miscibility-gap:

$${}^0L_{Al,P}^{liq} = -133862 \cdot e^{-\frac{T}{1000K}}$$

This T dependence is not used in any of the SGTE databases and is not permitted in FactSage

⇒ **L -parameter needs to be refitted !**



System Al-P: Liang & Schmid-Fetzer

thermodynamic modeling of **gas phase**:

$GAS (Al, Al_2, P, P_2, P_4)_1$ ideal mixing

$$G_i^{0,liq}(T) = G_i^{liq}(T) - H_i^{SER}$$
$$= a + b \cdot T + c \cdot T \ln T + d \cdot T^2 + e \cdot T^3 + f \cdot T^{-1} + RT \ln(10^{-5} \cdot p)$$

$i = Al, Al_2, P, P_2, P_4$;

G-functions not from SGTE Pure Substance database!

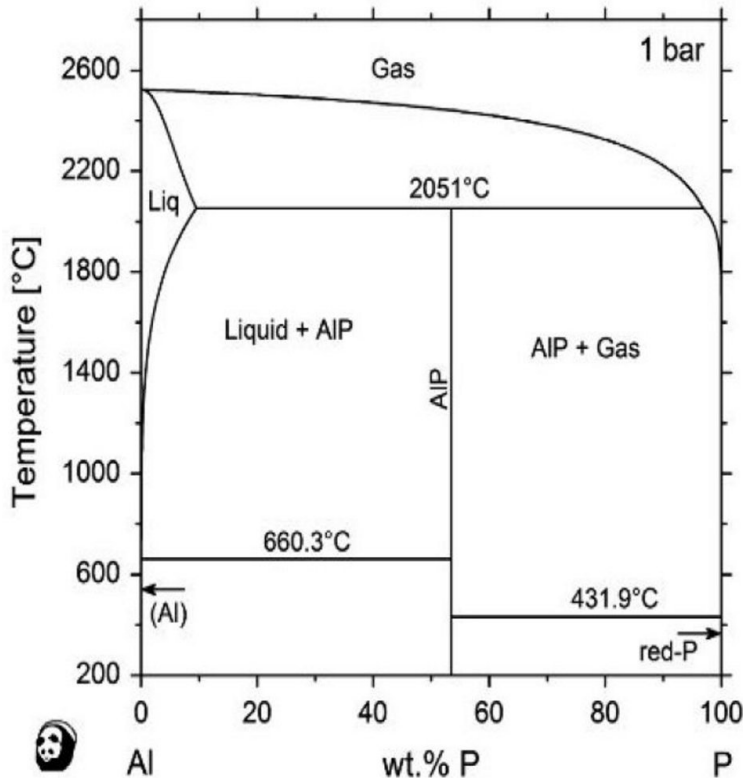
Instead, data were taken from literature:

M. Bennewies, E. Milke, *Thermochemical data of elements and compounds*, 2nd Ed., Wiley-VCH, Weinheim 2002

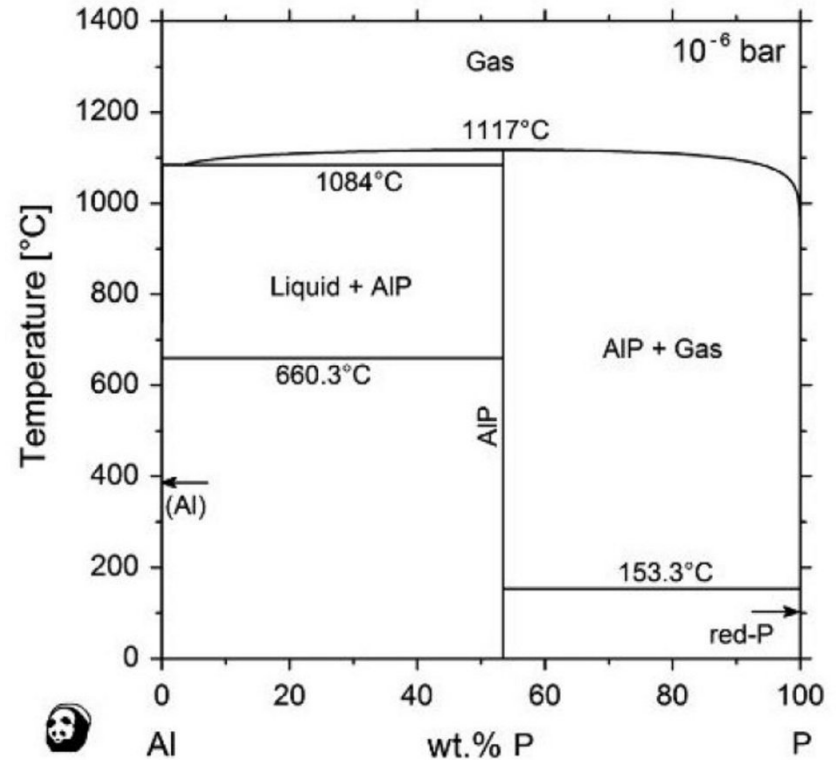


System Al-P: Liang & Schmid-Fetzer

original phase diagram from publ. Liang & Schmid-Fetzer
incl. gas phase for variable total pressure of gas phase (p_{tot})



no congruent subl. of
AIP for $p_{\text{tot}} = 1 \text{ bar}$



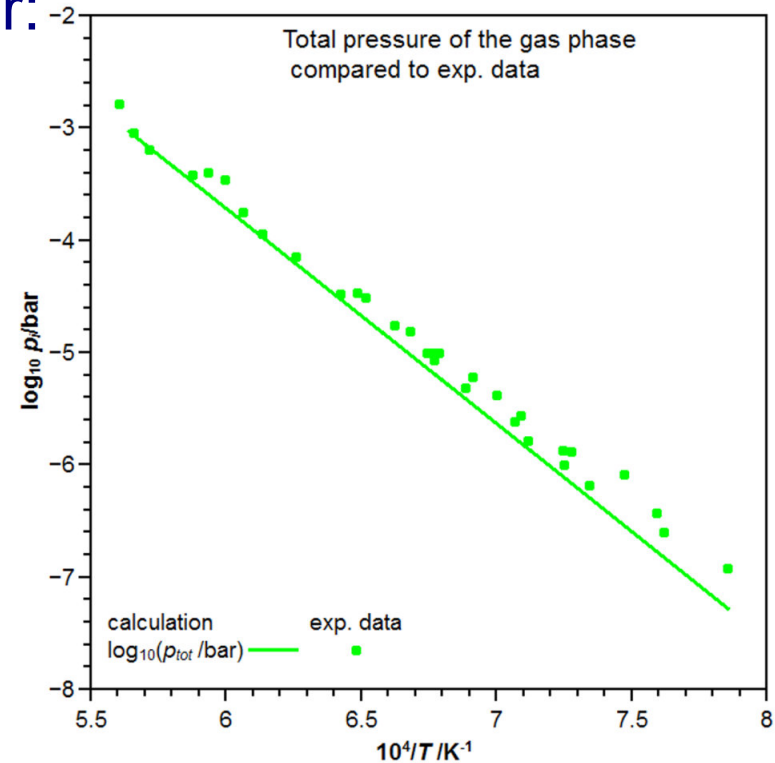
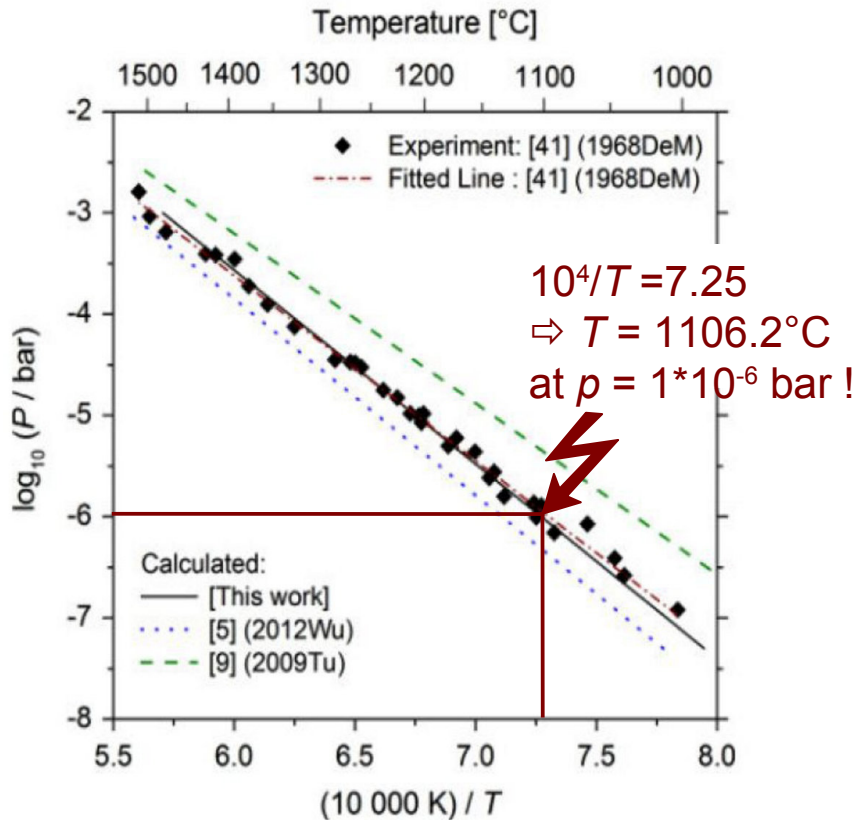
congruent subl. of AIP for
 $p_{\text{tot}} = 10^{-6} \text{ bar}$ at $T = 1117^\circ\text{C}$



System Al-P: Liang & Schmid-Fetzer

congruent sublimation of AlP for $p_{tot} = 10^{-6}$ bar:

vapour pressure curve calculated with data from Liang & Schmid-Fetzer:



issue: $T_{sub} = 1117^\circ\text{C}$

is not reproduced !

issue: mismatch of curve and exp. data !



Corrigendum: Liang & Schmid-Fetzer

corrigendum has been published by the authors:

S.-M. Liang, R. Schmid-Fetzer, Calphad **45** (2014) 251-253

reason for the shifted vapour pressure curve:
wrong entropy related parameter in $G^0(\text{AIP})$

$$G_{\text{AIP}}^0 = -180154 + \mathbf{293.45} \cdot T - 48.40 \cdot T \ln T - 2.35 \cdot 10^{-3} \cdot T^2 + 3.45 \cdot 10^5 \cdot T^{-1}$$

⇒ entropy S_{AIP}^{298} has to be corrected, too:

$$S_{\text{AIP}}^{298} = \mathbf{18} \text{ J} \cdot \text{K}^{-1} \cdot \text{mol}^{-1}$$

this value is significantly lower than all experimental and
calculated data from other groups

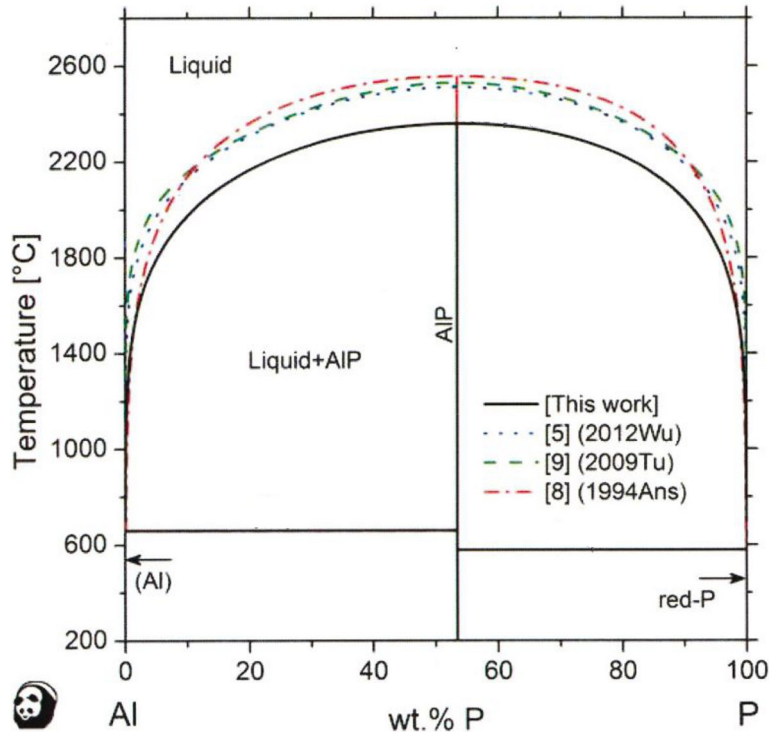


Corrigendum: Liang & Schmid-Fetzer

Adjustment of the phases LIQUID and FCC_A1 as well:

$${}^0L_{Al,P}^{liq} = -151900 \cdot e^{-\frac{T}{800K}}$$

$${}^0L_{Al,P}^{fcc} = -25500 \text{ to } -51500$$



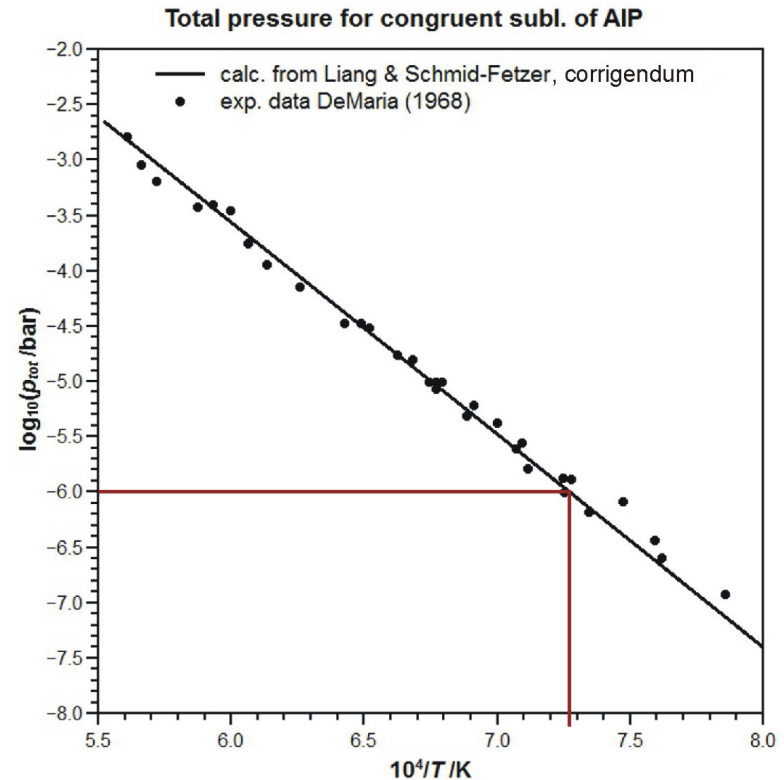
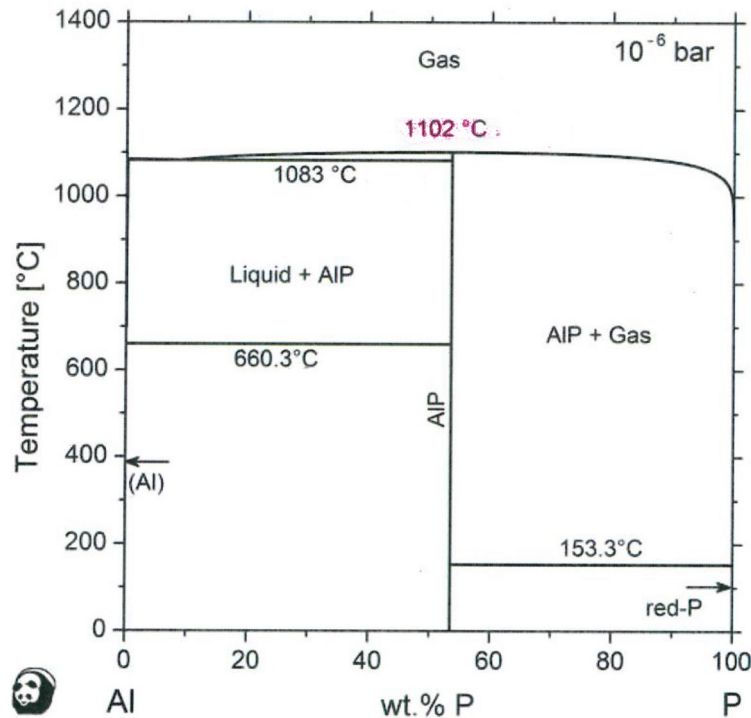
Al-P phase diagram, calculated by Liang & Schmid-Fetzer after correction, gas phase suppressed

congruent melting temperature
 $T_L(AIP) = 2359^\circ\text{C}$ now considerably lower than before



Corrigendum: Liang & Schmid-Fetzer

Al-P phase diagram with gas phase for $p_{\text{tot}} = 10^{-6}$ bar:



$p_{\text{tot}} = 10^{-6}$ bar; $10^4/T = 7.2714 \cdot 10^{-4} \text{ K}^{-1} \Rightarrow T = 1102^\circ\text{C}$,
now in accordance with vapour pressure curve

Adaptation for FactSage

1. Refit of the 0L -Parameter:

interaction parameter Al,P for LIQUID: ${}^0L_{Al,P}^{liq} = -151900 \cdot e^{-\frac{T}{800K}}$
needs to be refitted

first test was made with series expansion of *exp*-function
⇒ at least 7 parameters needed for appropriate precision

therefore:

fitting ${}^0L_{Al,P}^{liq}$ with standard Gibbs-Energy function

$${}^0L_{Al,P}^{liq} = a + b \cdot T + c \cdot T \ln T + d \cdot T^2 + e \cdot T^3 + f \cdot T^{-1}$$

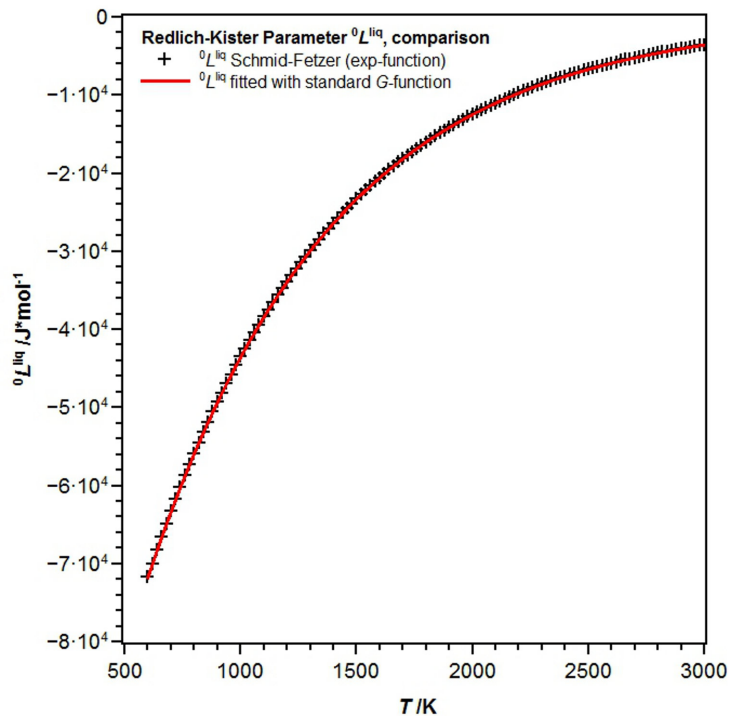
All 6 parameters used for high precision
of (weighted!) least square fit.



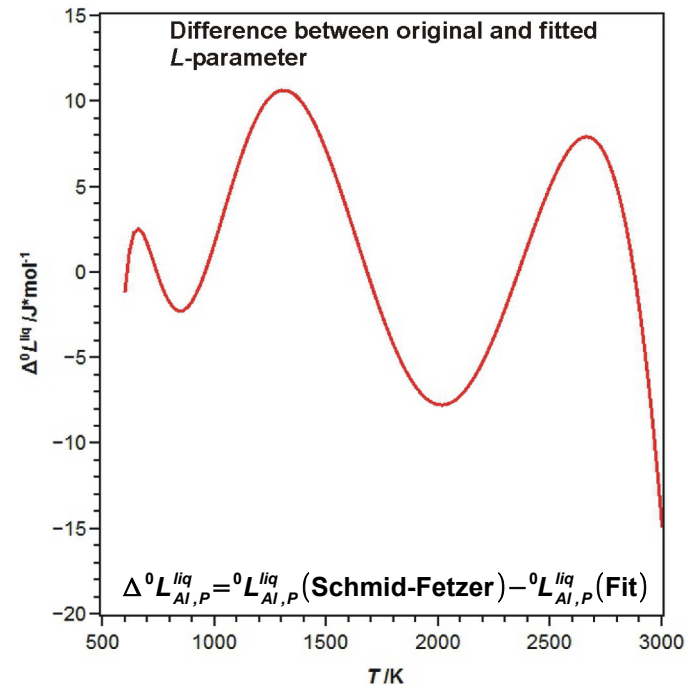
Adaptation for FactSage

1. Refit of the 0L -Parameter:

Difference between the original L -parameter and the fitted one:



no difference visible on this scale !

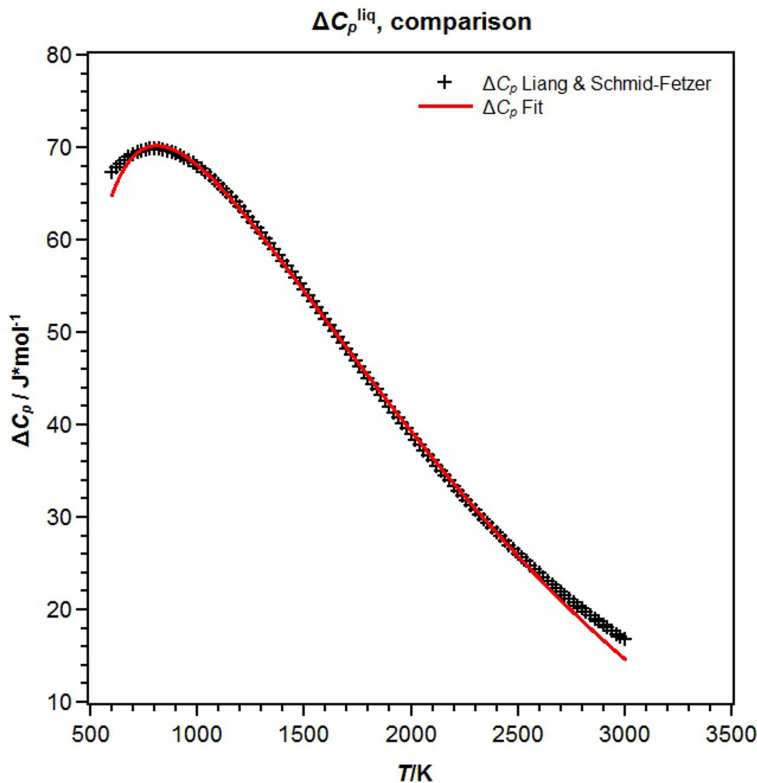


max. difference $+11 \text{ J}^* \text{mol}^{-1} \cdot \text{atoms}^{-1}$
($1000 \text{ K} < T < 1700 \text{ K}$)

Adaptation for FactSage

1. Refit of the 0L -Parameter:

L -parameter \Rightarrow additional heat capacity (Δc_p^{liq}) for LIQUID:



Difference increasing for $T < 600$ K
and $T > 2800$ K

L -parameter from fit:

$$\begin{aligned}
 {}^0L_{Al,P}^{liq} = & -213970.46 \\
 & + 1033.2727 \cdot T \\
 & - 129.64175 \cdot T \ln T \\
 & + 2.7606318 \cdot 10^{-2} \cdot T^2 \\
 & - 9.6312894 \cdot 10^{-7} \cdot T^3 \\
 & + 6065980 \cdot T^{-1}
 \end{aligned}$$

Adaptation for FactSage

2. Exchange of the gas phase

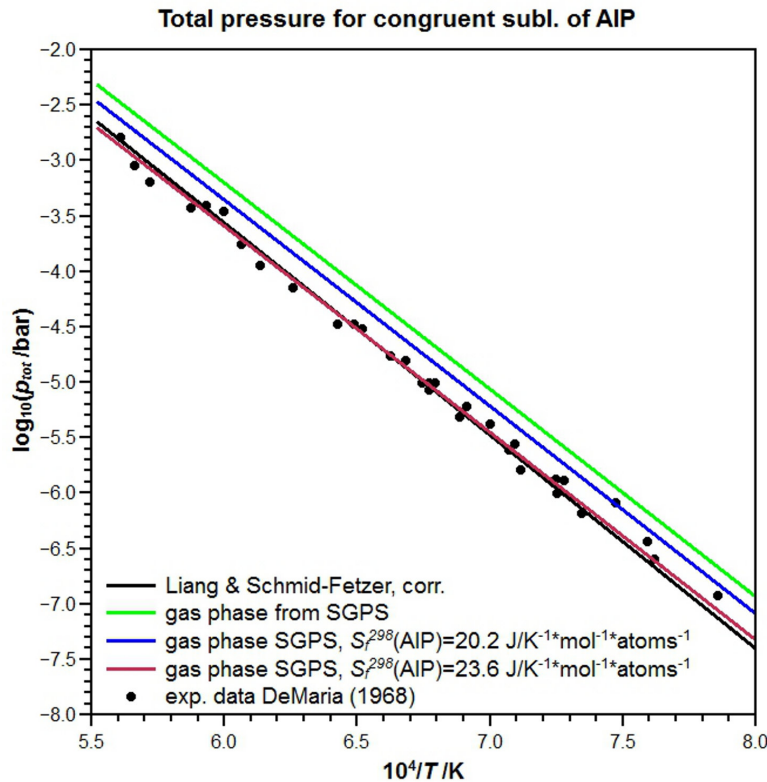
if the system Al-P is incorporated into SGTE solution database

- ⇒ gas phase based on data from Bennewies and Milke cannot be used !
- ⇒ gas phase must be exchanged against description in SGTE Pure Substance Database (SGPS) , vapour pressure curves for sublimation of AlP have to be recalculated to fit the experimental data



Adaptation for FactSage

2. Exchange of the gas phase recalculation of vapour pressure curves for sublimation of AIP:



standard entropy of AIP:

$$S_{\text{AIP}}^{298} = 18.0 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}\cdot\text{atoms}^{-1}$$

⇒ green line

$$S_{\text{AIP}}^{298} = 20.2 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}\cdot\text{atoms}^{-1}$$

⇒ blue line

$$S_{\text{AIP}}^{298} = \mathbf{23.6 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}\cdot\text{atoms}^{-1}}$$

⇒ red line

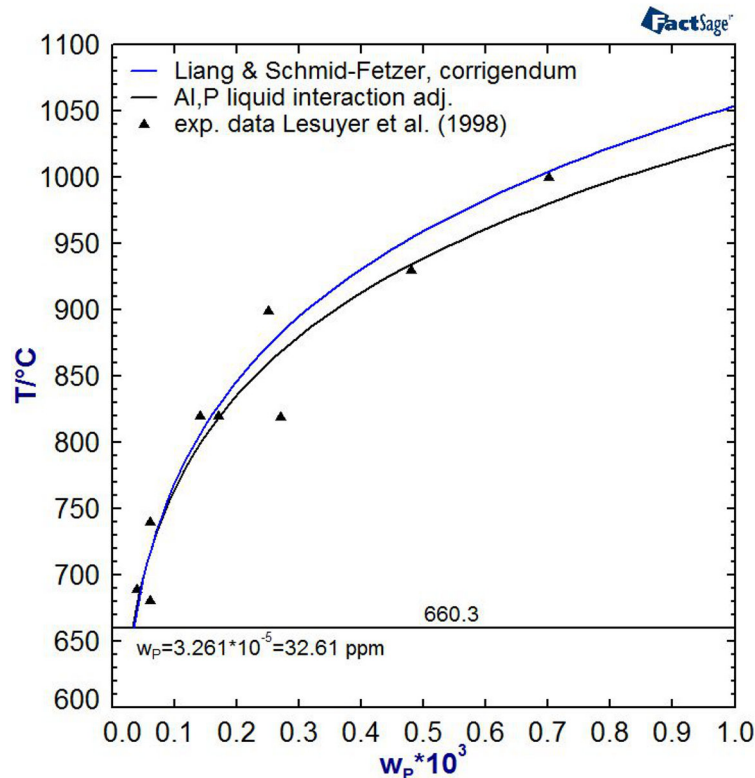
good correspondence with exp.
and calc. data from other
authors

Adaptation for FactSage

3. Adjustment of Al,P interaction in liquid

changed entropy value \Rightarrow adjustment of Al,P interaction in liquid phase to fit solubility of P in Al_{liq}

$$S_{AlP}^{298} = 23.6 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}\cdot\text{atoms}^{-1}$$



Solubility of P in Al_{liq} :

$w_P = 3.42 \cdot 10^{-5}$ (34.2 ppm)
(Liang & Schmid-Fetzer)

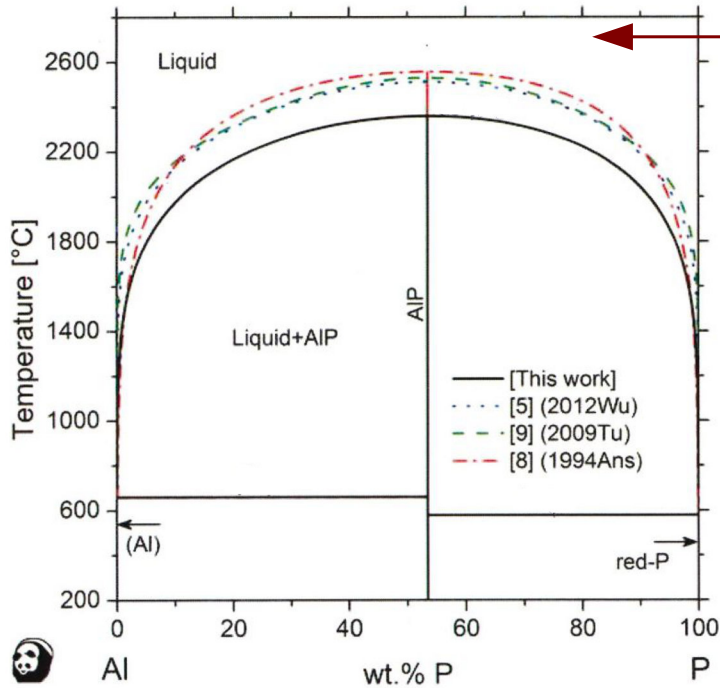
$w_P = 3.26 \cdot 10^{-5}$ (32.6 ppm)
(present work)

Adaptation for FactSage

4. Final comparison

binary phase diagram, gas phase deactivated

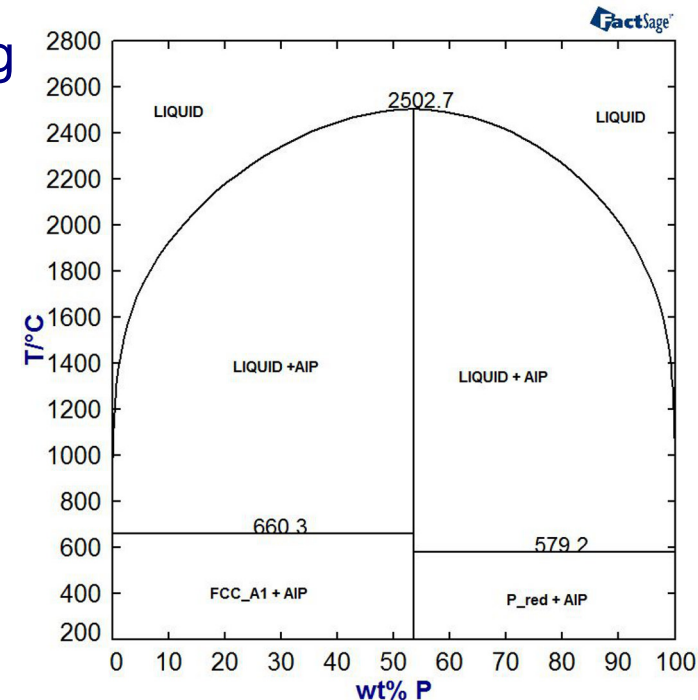
original image in Liang & Schmid-Fetzer's corrigendum



Congruent melting temperature AIP ($T_L = 2359^\circ\text{C}$) much lower than before (2522°C) reason: low

$$S_{AIP}^{298}$$

calculated with data after adaptation

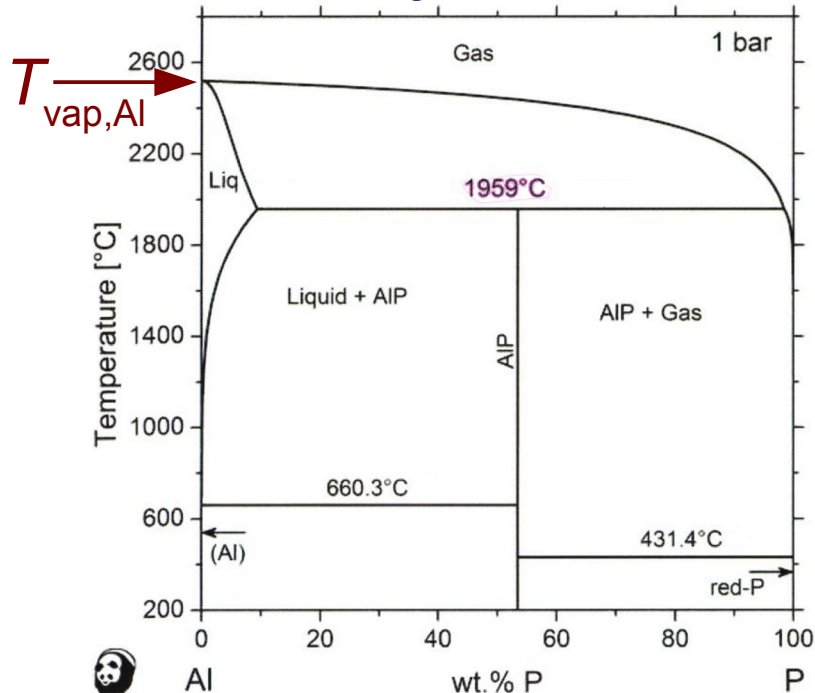


Adaptation for FactSage

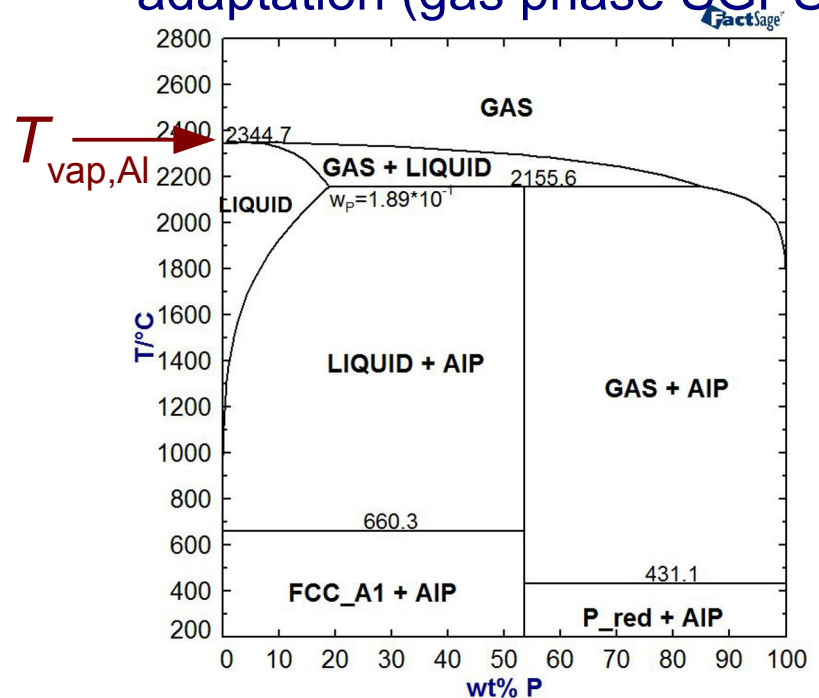
4. Final comparison

binary phase diagram including gas phase, $p_{\text{tot}}=1$ bar

original image in Liang & Schmid-Fetzer's corrigendum



calculated with data after adaptation (gas phase SGPS)

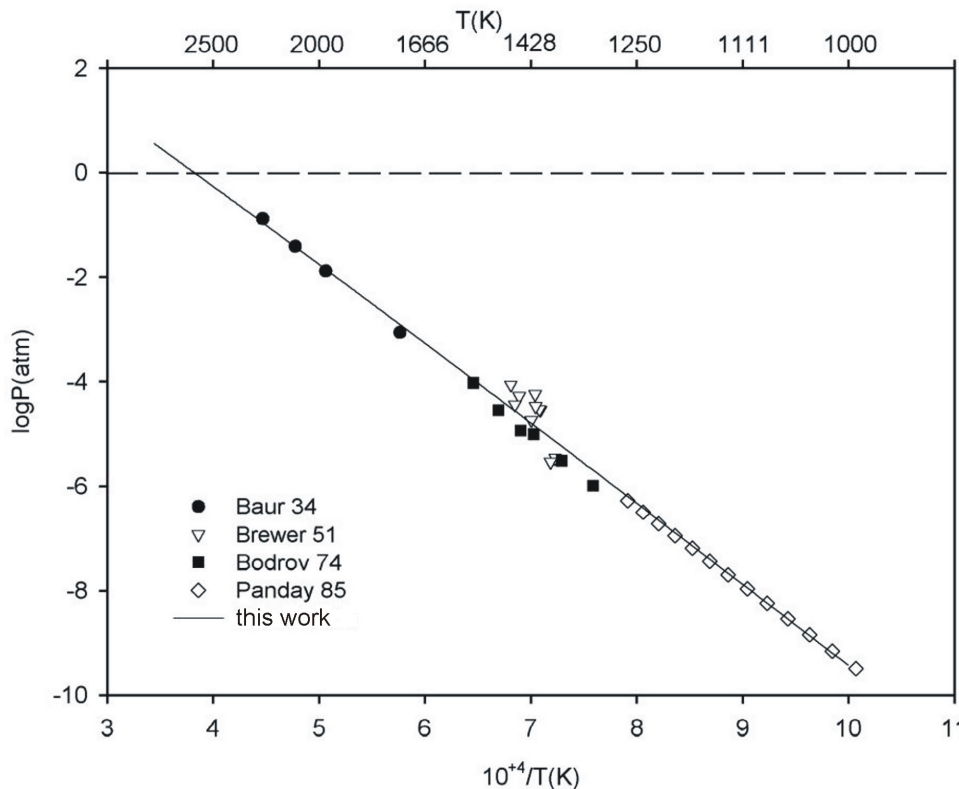


next **issue**: boiling temp. for pure Al very high ($T_{\text{vap}}=2520^\circ\text{C}$) in Liang & Schmid-Fetzer comp. to literature !



Adaptation for FactSage

4. Final comparison



Source of data for SGPS:

Fit of experimental data from various authors and extrapolation to standard pressure $\log p = 0$ by **Cheyne & Chaud**

$$\Rightarrow T_{\text{vap}}^{\text{Al}} = 2345^\circ\text{C}$$



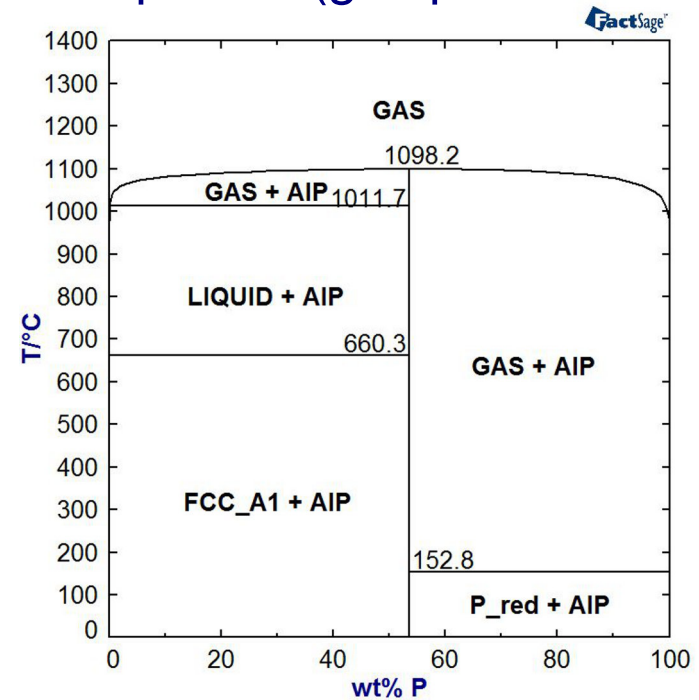
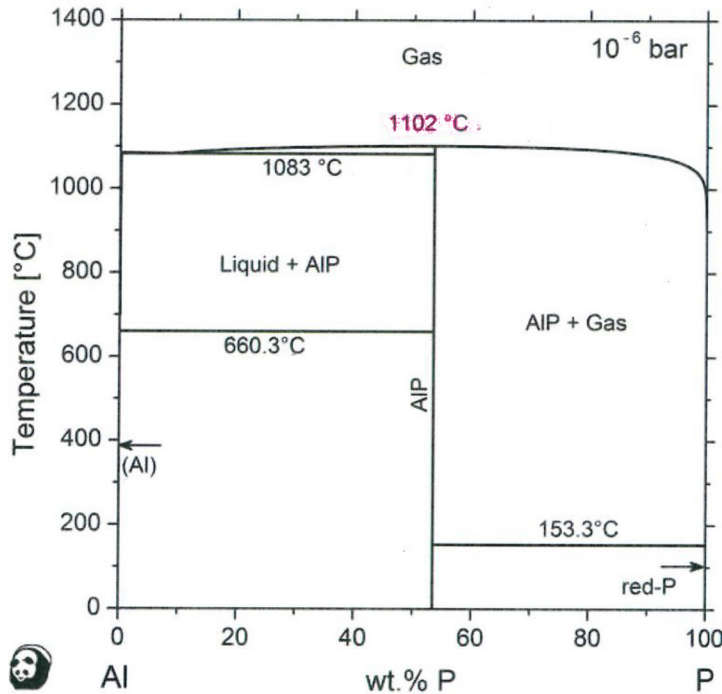
Adaptation for FactSage

4. Final comparison

binary phase diagram including gas phase, $p_{\text{tot}} = 10^{-6}$ bar

original image in Liang & Schmid-Fetzer's corrigendum

calculated with data after adaptation (gas phase SGPS)



Conclusion

- ⇒ fit of the interaction parameter $A_{I,P}$ for the liquid phase ${}^0L_{Al,P}^{liq}$ by standard Gibbs polynomial function is sufficiently precise
- ⇒ gas phase in SGTE Pure Substance database (SGPS) based on data from Cheynet & Chaud is consistent with data from Liang & Schmid-Fetzer, allows use of $S_{AIP}^{298} = 23.6 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}\cdot\text{atoms}^{-1}$, which is in better agreement with exp. data



Thank you for your
attention !

