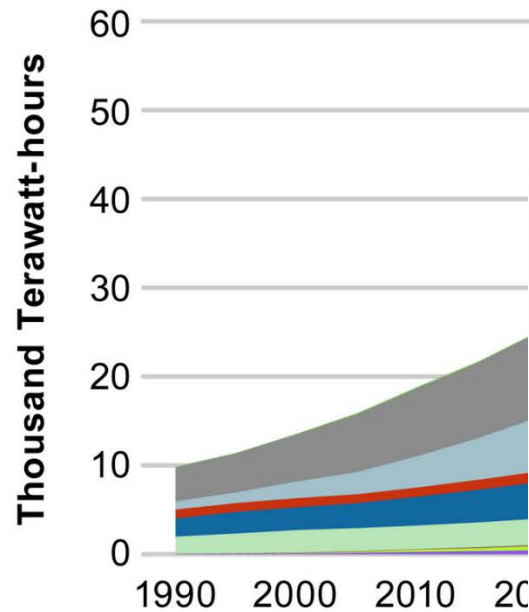


Further progress in modelling slag viscosities on the basis of the HotVeGas Oxide database

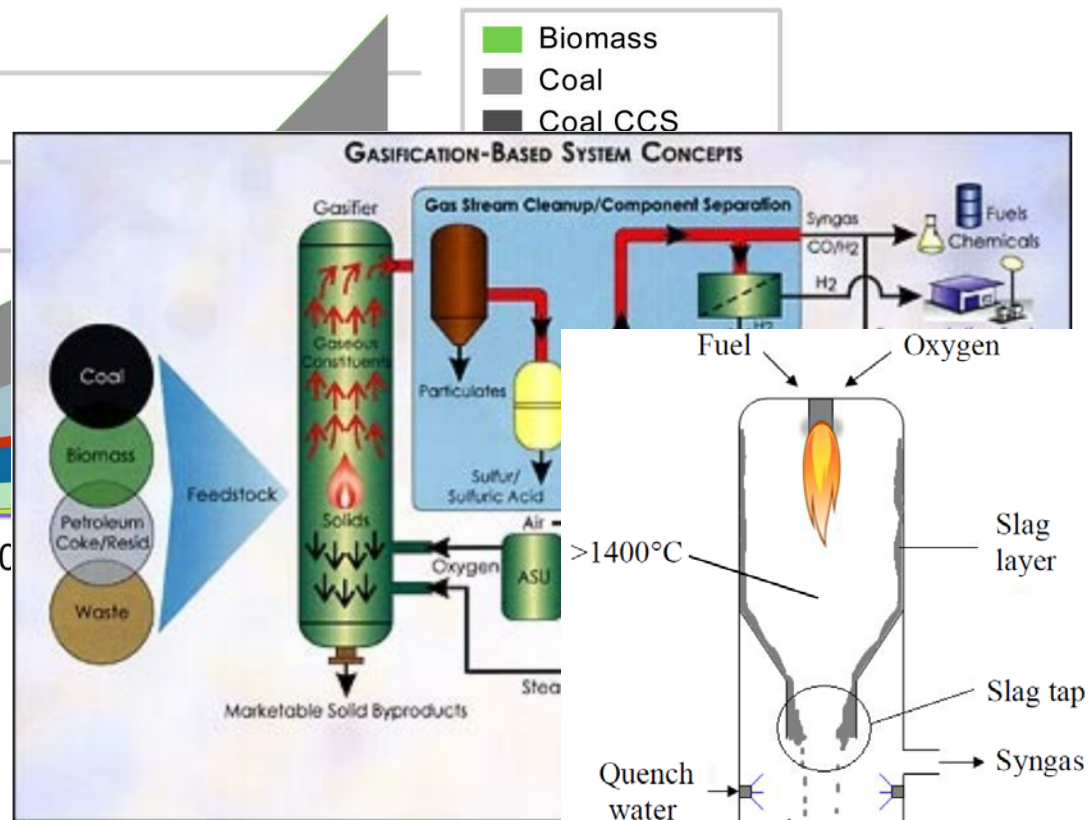
03.07.2014 Guixuan Wu

- Background and motivation
- Challenging viscosity behaviors
- Viscosity model development
- Results
- Application of 3-D viscosity surface
- Conclusions and outlook

Background and motivation



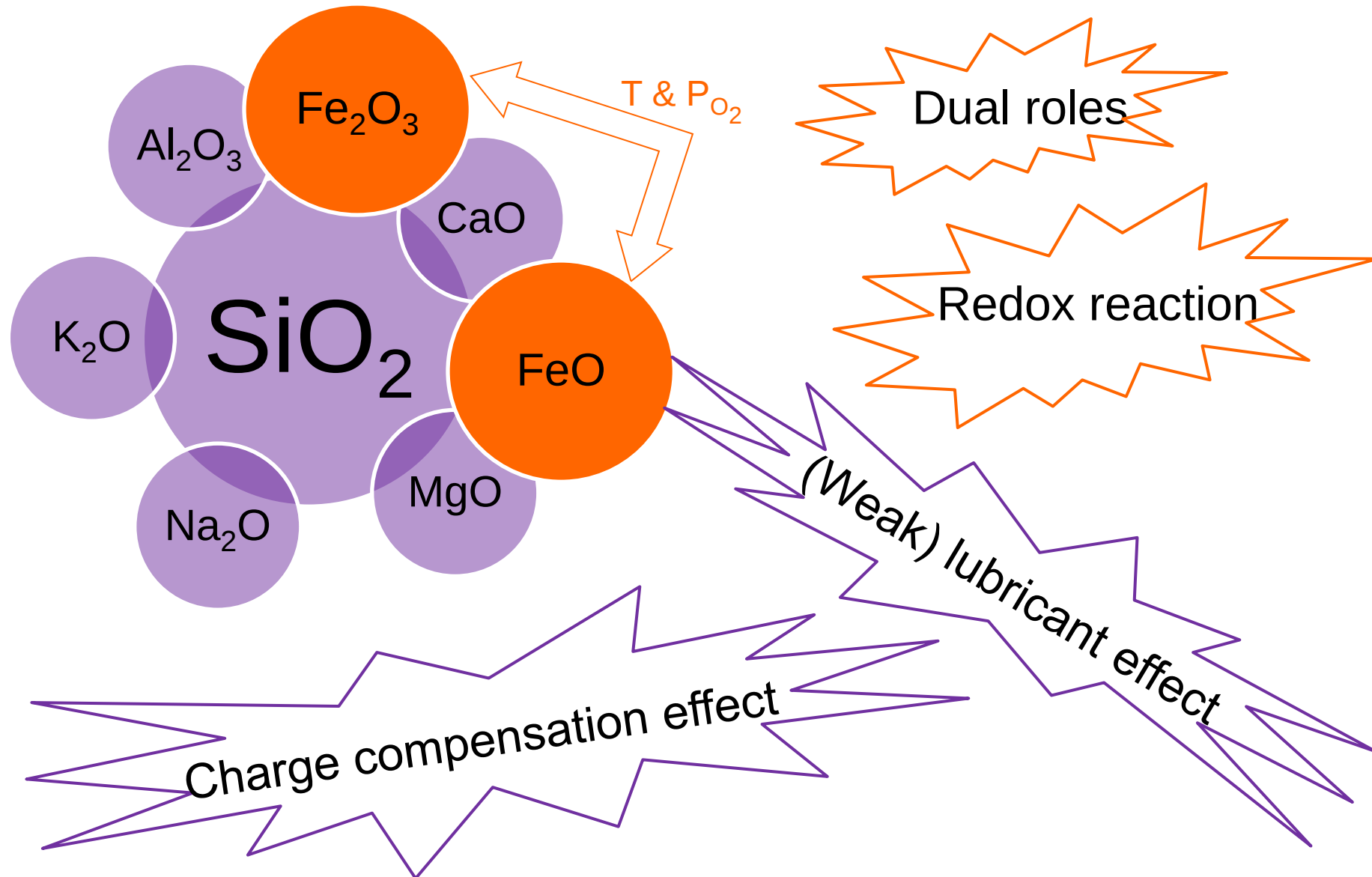
Source: SEI International



Source: HotVeGas

Source: Marc A. Duchesne, *Slagging in entrained-flow gasifiers*, 2012.

The challenging viscosity behaviors



The viscosity model

Classical model:



The story of current model :

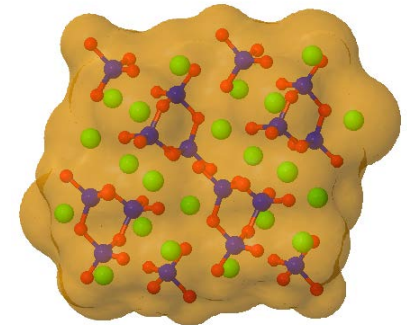


- For FeO/Fe₂O₃ containing systems, partial pressure of oxygen is also taken into account in the current model.

The current viscosity model I



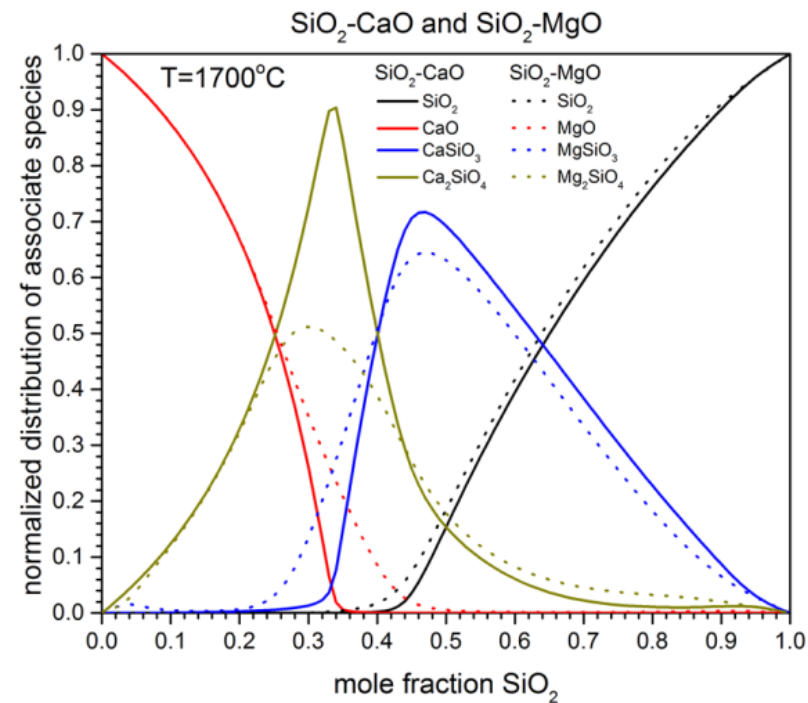
Partial pressure of oxygen
(for FeO/Fe₂O₃ containing system)



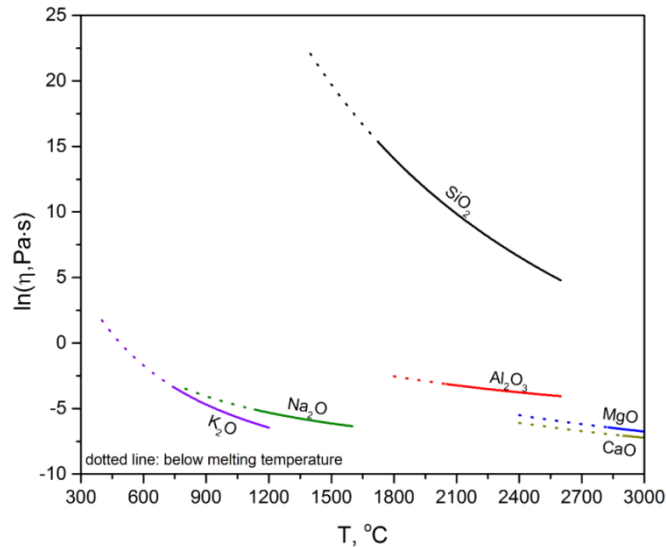
CaSiO₃

SiO₂-CaO-MgO

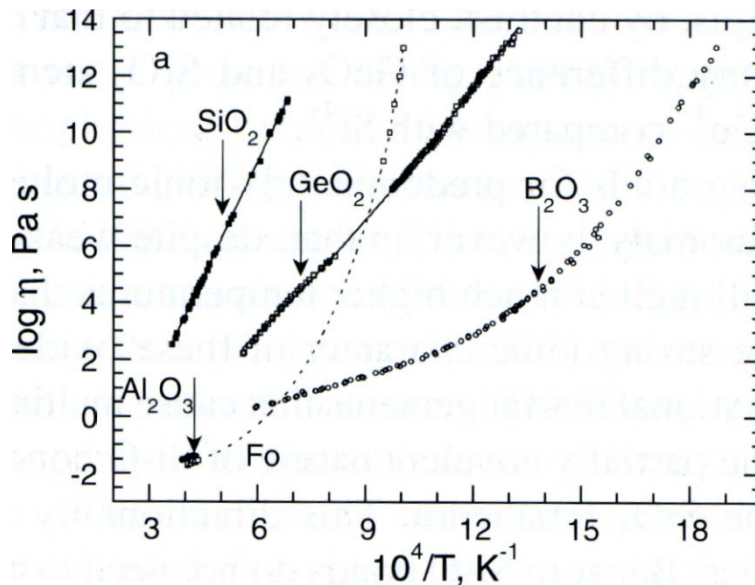
Compounds	Associate species
SiO ₂	Si ₂ O ₄
CaO	Ca ₂ O ₂
CaSiO ₃	CaSiO ₃
Ca ₂ SiO ₄	$\frac{2}{3} \cdot \text{Ca}_2\text{SiO}_4$
MgSiO ₃	MgSiO ₃
Mg ₂ SiO ₄	$\frac{2}{3} \cdot \text{Mg}_2\text{SiO}_4$



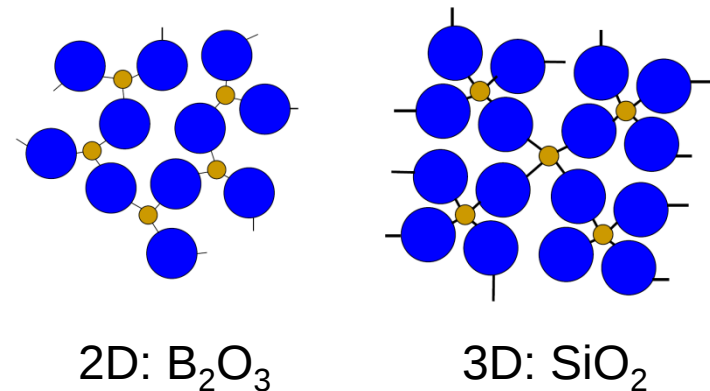
Pure oxides



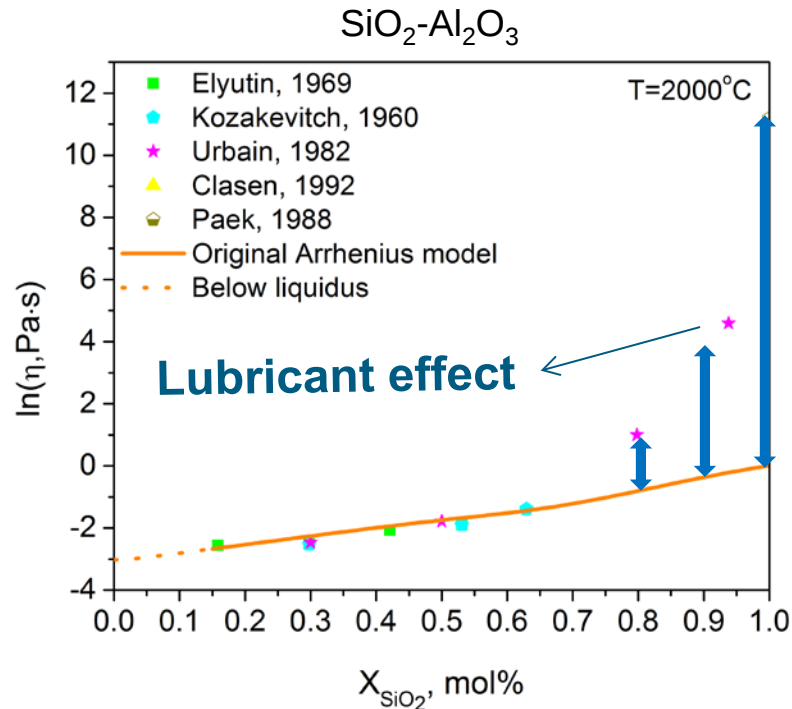
Sun's Bond Strength Model			
M in MO_x	Valence	Coordination number	Single-bond strength (kcal/mol)
B	3	3	119
Si	4	4	106
Al	3	6	53-67
Mg	2	6	37
Ca	2	8	32
Na	1	6	20
K	1	9	13



Network Dimensionality:



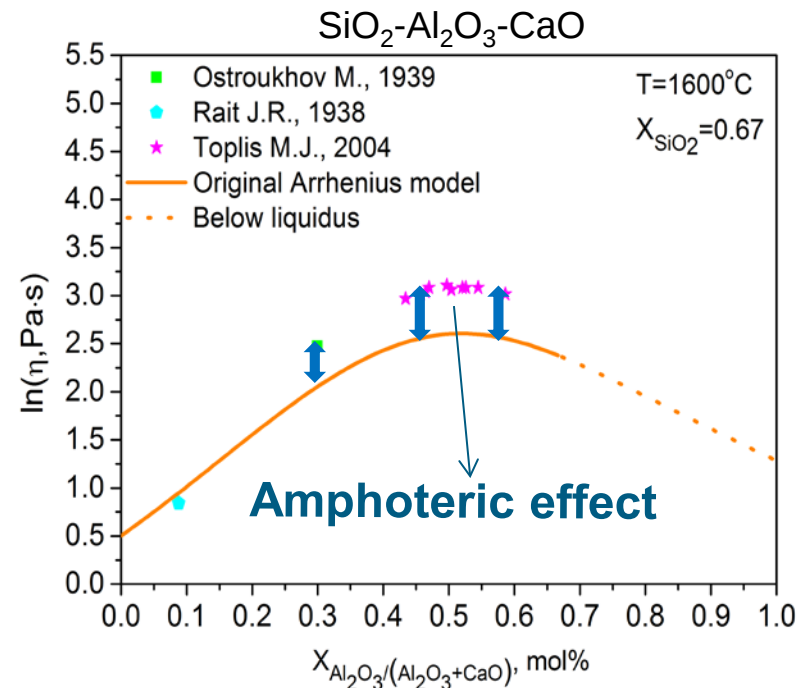
The results of the current viscosity model



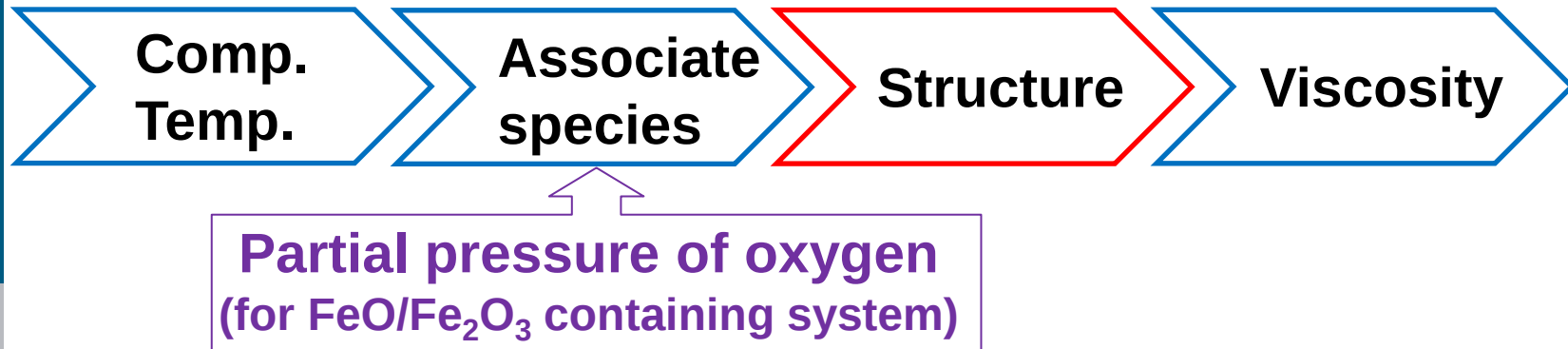
$$\ln \eta = (\sum X_i \cdot \ln \eta_i)$$

where: $\ln \eta_i = A_i + B_i/T$

i : associate species



The idea of current viscosity model II



SiO₂-CaO-MgO

Compounds	Associate species	Structural units
SiO ₂	Si ₂ O ₄	SiO ₂
CaO	Ca ₂ O ₂	CaO
CaSiO ₃	CaSiO ₃	CaSiO ₃
Ca ₂ SiO ₄	$\frac{2}{3} \cdot \text{Ca}_2\text{SiO}_4$	Ca ₂ SiO ₄
MgSiO ₃	MgSiO ₃	MgSiO ₃
Mg ₂ SiO ₄	$\frac{2}{3} \cdot \text{Mg}_2\text{SiO}_4$	Mg ₂ SiO ₄

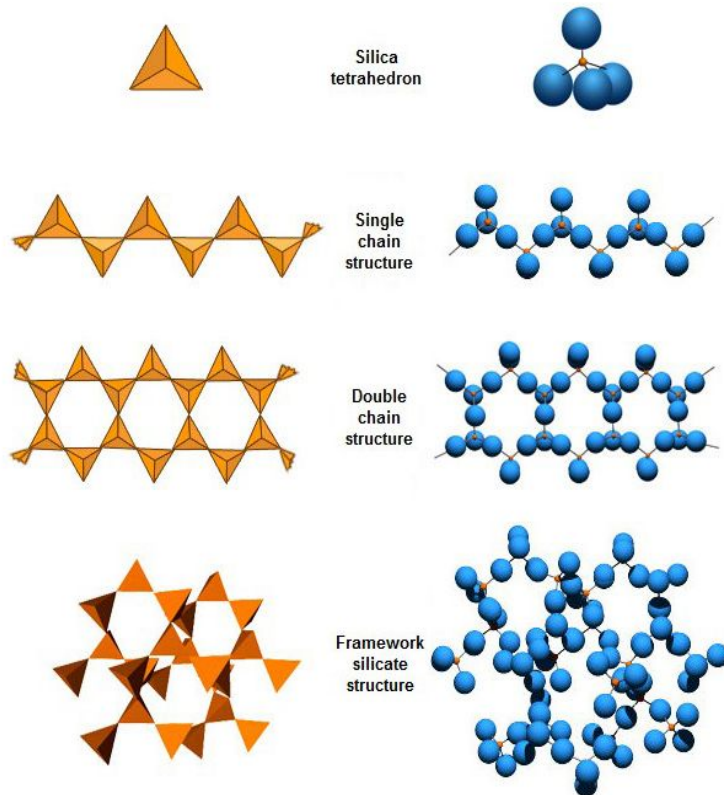
CaO-Fe₂O₃

Compounds	Associate species	Structural units
CaO	Ca ₂ O ₂	CaO
FeO	Fe ₂ O ₂	FeO
Fe ₂ O ₃	Fe ₂ O ₃	FeO _{1.5}
CaFe ₂ O ₄	$\frac{2}{3} \cdot \text{CaFe}_2\text{O}_4$	Ca _{0.5} FeO ₂

basic structural units

Larger structural units

S: SiO_2 , A: Al_2O_3 , N: Na_2O



$$\begin{aligned} S_1 + S_1 &= S_2 \\ S_1 + S_2 &= S_3 \\ &\dots \dots \\ S_1 + S_{k-1} &= S_k \end{aligned}$$

self-pol. of SiO_2

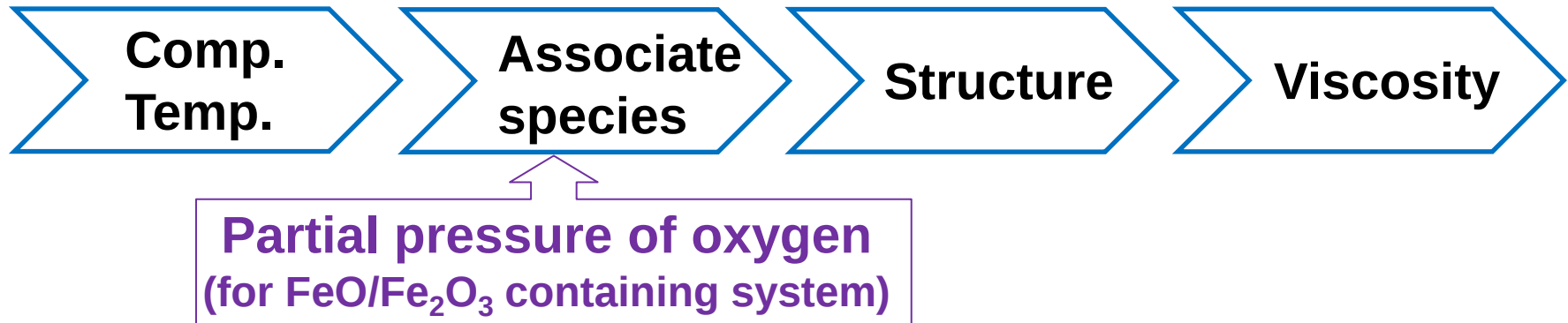
$$\begin{aligned} A_1 N_1 S_1 + S_1 &= A_1 N_1 S_2 \\ A_1 N_1 S_1 + S_2 &= A_1 N_1 S_3 \\ &\dots \dots \\ A_1 N_1 S_1 + S_{k-1} &= A_1 N_1 S_k \end{aligned}$$

inter-pol.

$$\begin{aligned} A_1 N_1 S_1 + A_1 N_1 S_1 &= A_2 N_2 S_2 \\ A_2 N_2 S_2 + A_1 N_1 S_1 &= A_3 N_3 S_3 \\ &\dots \dots \\ A_{k-1} N_{k-1} S_{k-1} + A_1 N_1 S_1 &= A_k N_k S_k \end{aligned}$$

**self-pol. of silicon-aluminum
based ternary associate species**

The current viscosity model II



Arrhenius model (modified)

$$\ln \eta = \ln \eta_{\text{ideal}} + \ln \eta_{\text{excess}}$$

$$= (\sum X_i \cdot \ln \eta_i) + (\ln \eta_{\text{self-pol.}} + \ln \eta_{\text{inter-pol.}})$$

where: $\ln \eta_i = A_i + B_i/T$ $\longrightarrow$ basic structural units

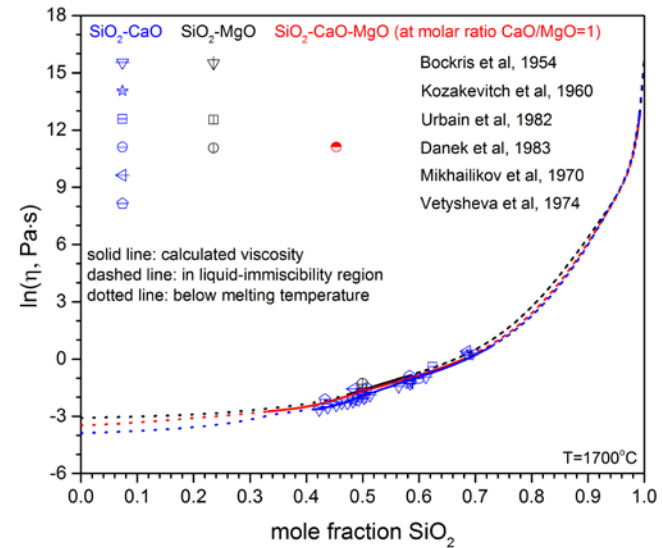
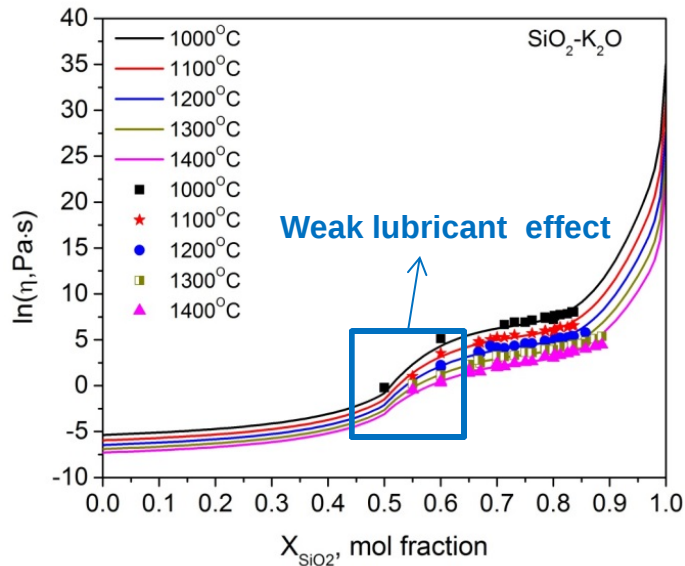
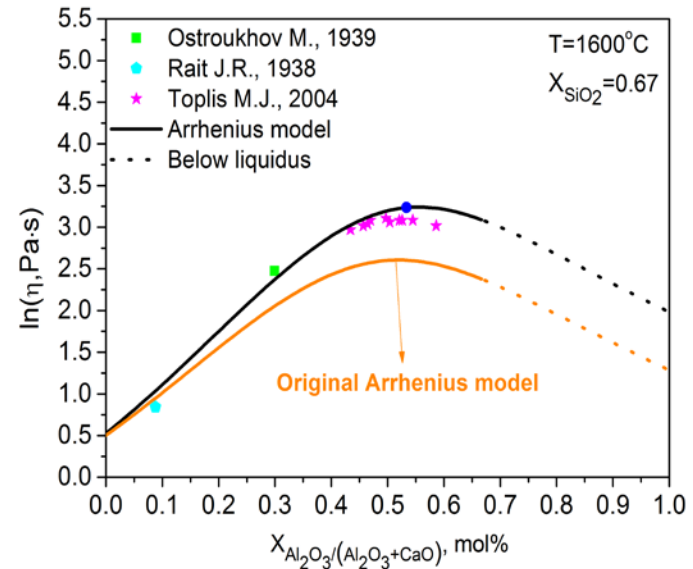
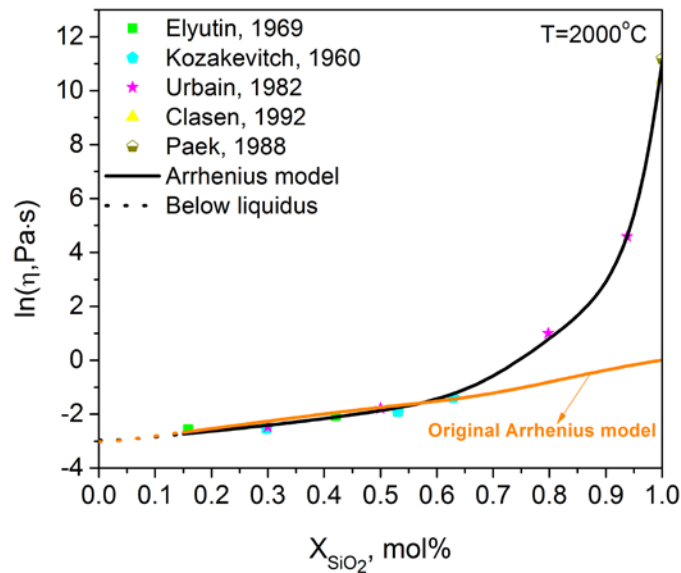
$$\ln \eta_{\text{self-pol.}} = \sum (A_{j,\text{SiO}_2}^* + B_{j,\text{SiO}_2}^*/T) \cdot (X_{\text{SiO}_2}^{n_j})$$

$$+ \sum (A_k^* + B_k^*/T) \cdot (X_k^{n_k})$$

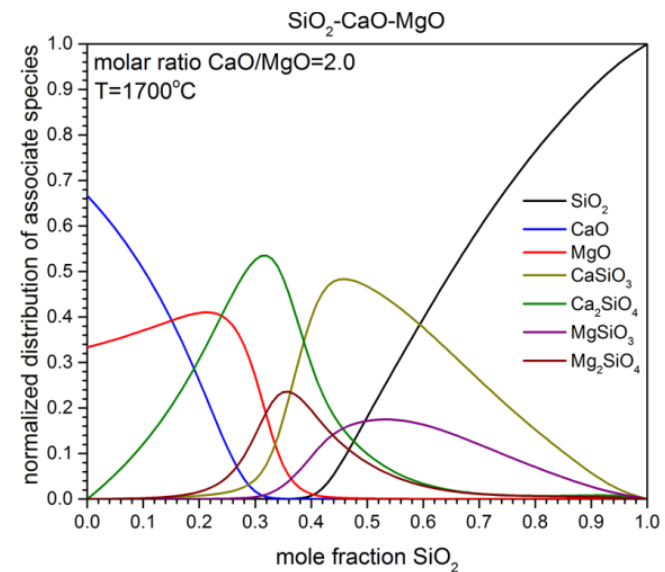
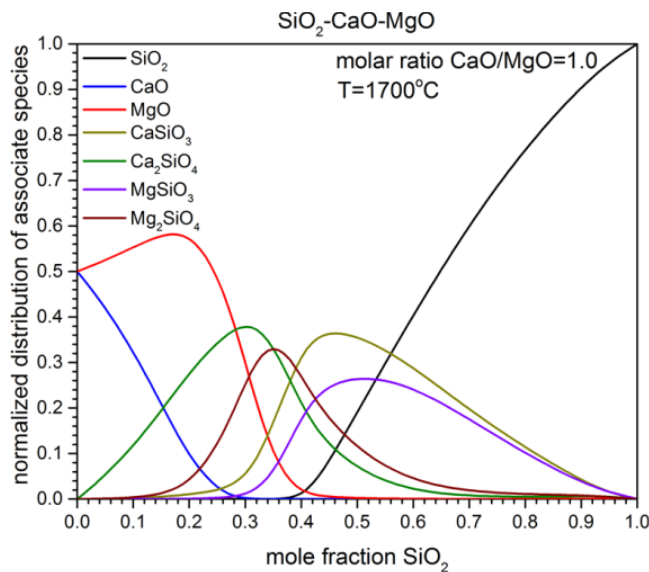
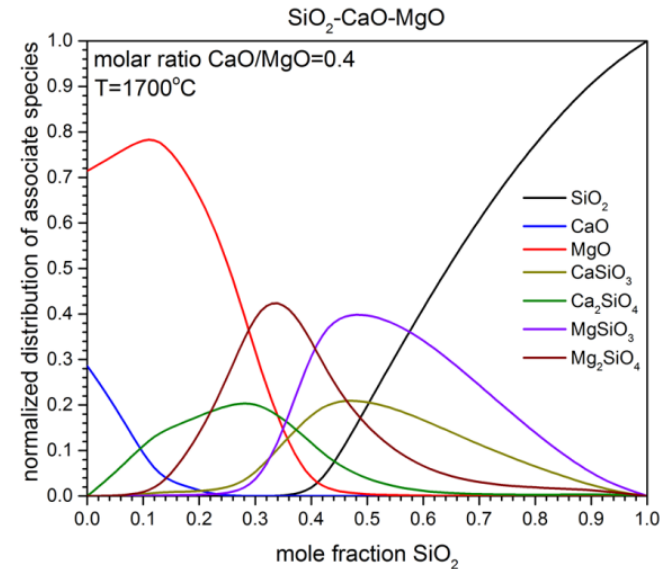
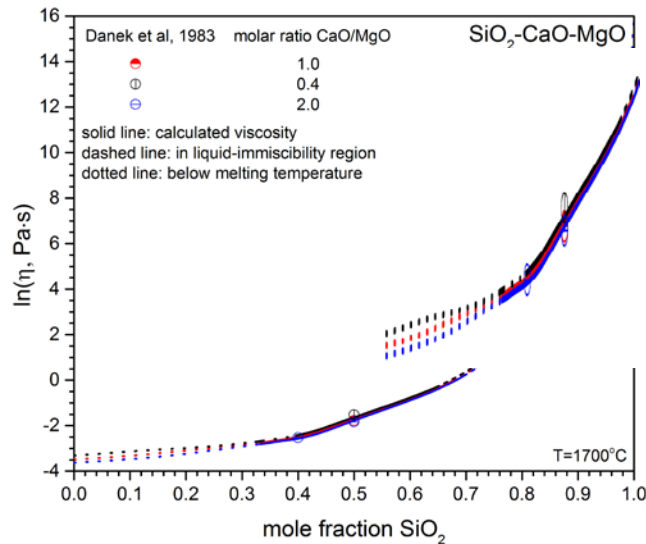
$$\ln \eta_{\text{inter-pol.}} = \sum (A_m^* + B_m^*/T) \cdot (X_m \cdot X_{\text{SiO}_2}^{n_m})$$

larger structural units

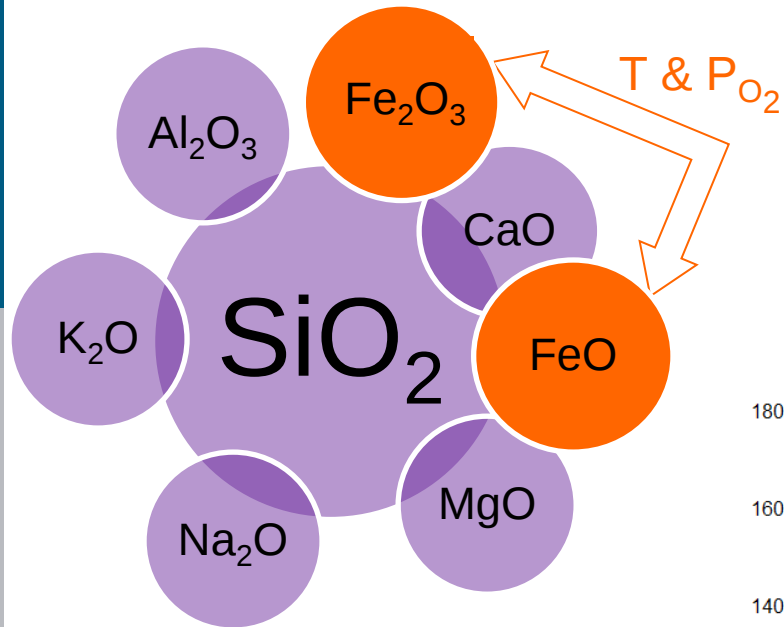
The results of the current viscosity model II



The distribution of structural units

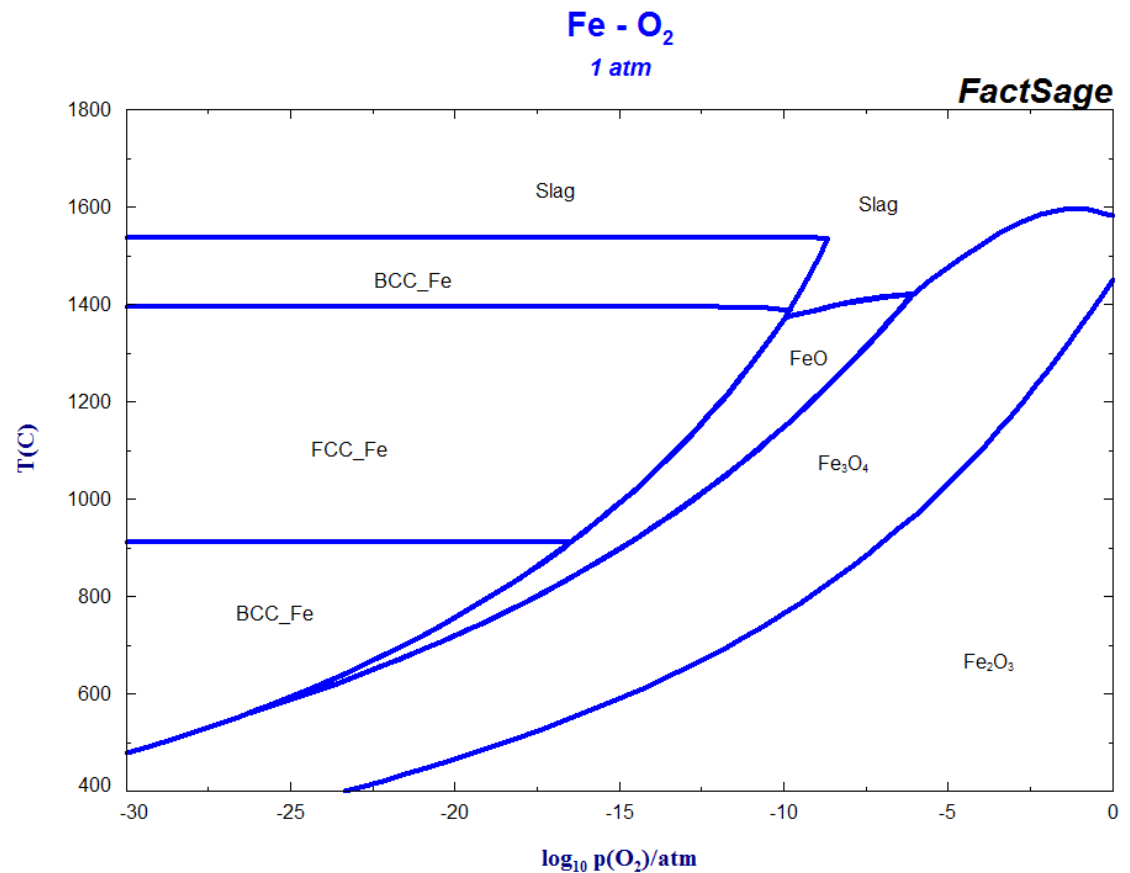


Influence of the T and P_{O_2}

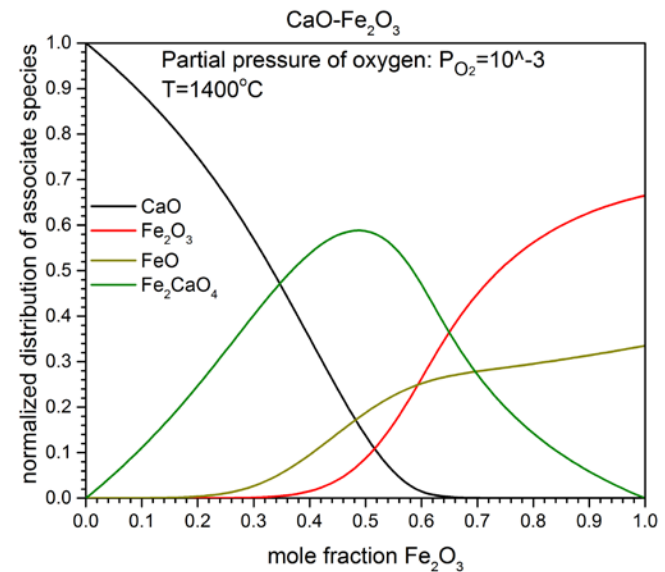
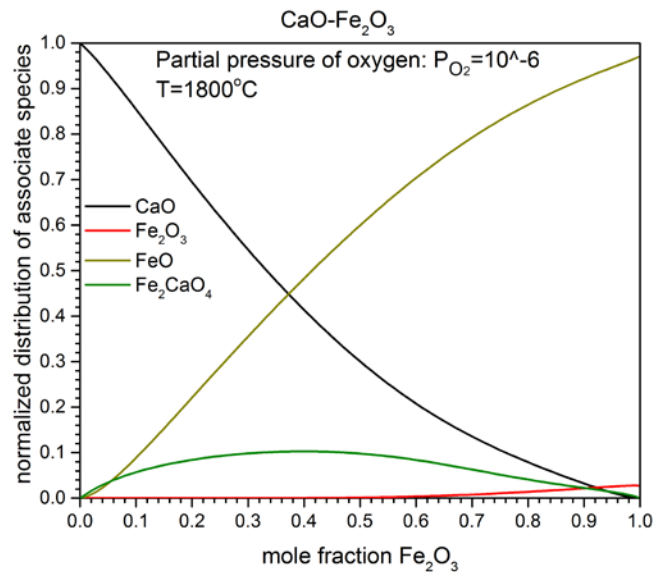
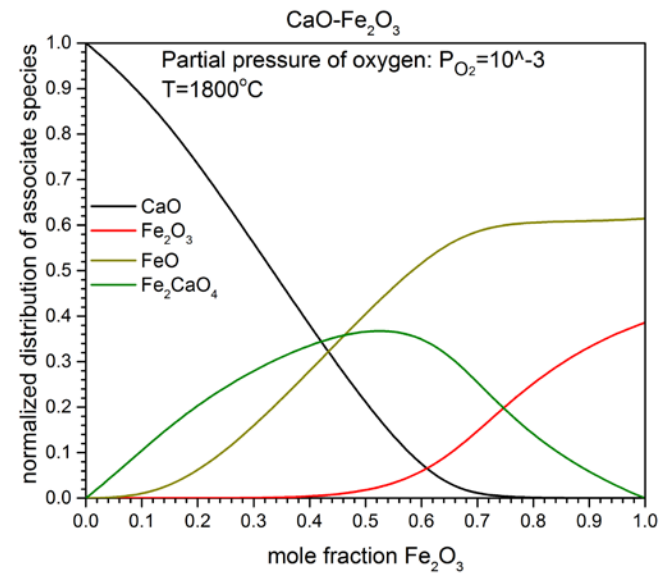
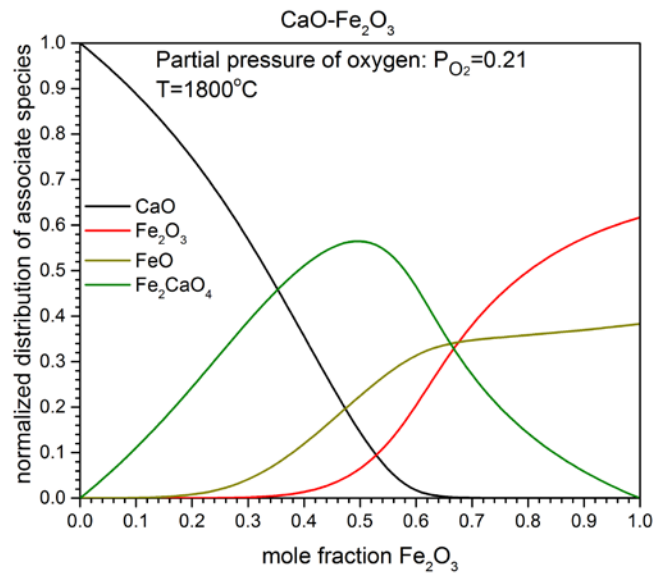


Dual roles

Redox reaction



Influence of the T and P_{O_2}



The modified Urbain model

$$\eta = A \exp(B/RT),$$

$$\ln(\eta) = \ln(A) + \ln(T) + B/RT,$$

$$\begin{aligned} \ln(\eta) = & a_0 + a_1y + a_2y^2 + a_3x + a_4xy + a_5xy^2 + a_6x^2 + a_7x^2y \\ & + a_8x^2y^2 + a_9x^3 + a_{10}x^3y + a_{11}x^3y^2, \end{aligned}$$

where: x and y are the normalized mole fractions $m_s/(m_s + m_a + m_c + m_f)$ and $(m_c + m_f)/(m_a + m_c + m_f)$, respectively.

s: SiO₂, a: Al₂O₃, c: CaO, f: FeO

Source: Hurst, H. J.; Novak, F.; Patterson, J. H., *Fuel* **1999**, 78, 1831-1840.

Parameters for the modified Urbain model

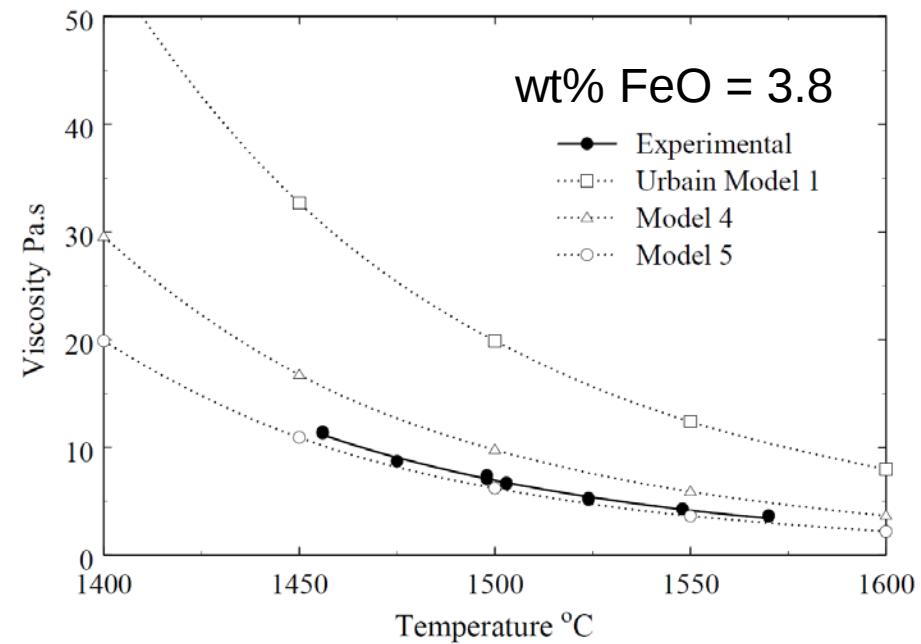
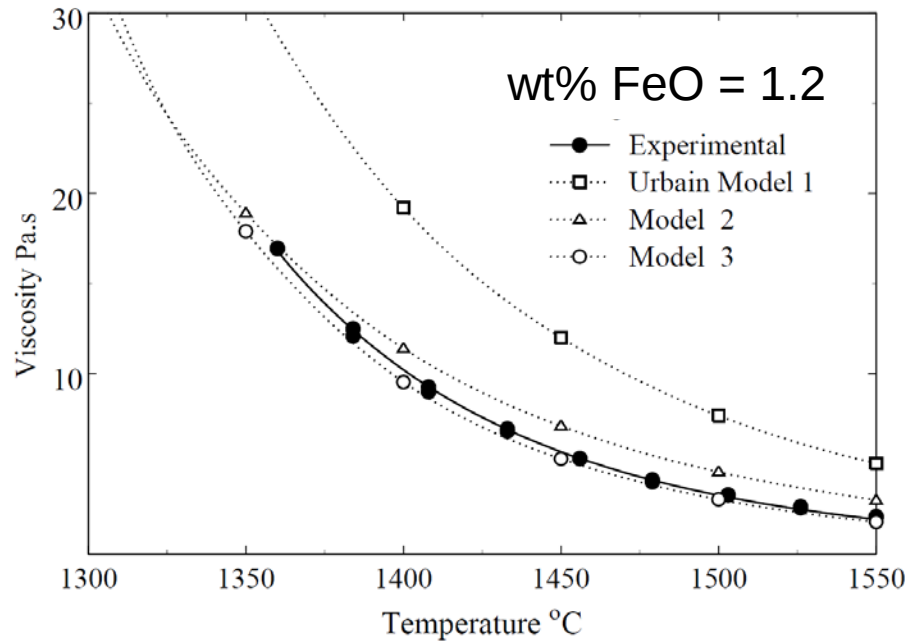
Model 1	Urbain model [4]
Model 2	Synthetic slag SAC model [3]
Model 3	Coal ash slag model for <2.5% FeO
Model 4	Synthetic slag SACF model for 5% FeO [5]
Model 5	Coal ash slag SACF model for 2.5–5% FeO
Model 6	Coal ash slag SACF model for 5–7.5% FeO
Model 7	Synthetic slag SACF model for 10% FeO [5]
Model 8	Coal ash slag SACF model for 7.5–10% FeO

Coeff.	Model 3, < 2.5 wt% FeO	
	1450°C	1500°C
a_0	$-7.402775E + 03$	$-7.817323E + 03$
a_1	$2.133864E + 04$	$2.241419E + 04$
a_2	$-1.539507E + 04$	$-1.607130E + 04$
a_3	$4.133813E + 04$	$4.361551E + 04$
a_4	$-1.190597E + 06$	$-1.248887E + 05$
a_5	$8.582252E + 04$	$8.941590E + 04$
a_6	$-7.623803E + 04$	$-8.039671E + 04$
a_7	$2.193927E + 04$	$2.298908E + 05$
a_8	$-1.580125E + 04$	$-1.643712E + 05$
a_9	$4.651861E + 04$	$4.903991E + 04$
a_{10}	$-1.336966E + 04$	$-1.399871E + 05$
a_{11}	$9.619190E + 04$	$9.994213E + 04$
s^2	0.44	0.51

Slag	Ash	Model	Normalised composition			
			SiO ₂	Al ₂ O ₃	CaO	FeO
1	1	3	62.7	11.6	25.6	0.1
2	2	3	50.1	23.6	26.1	0.2
3	2	3	52.1	24.7	22.9	0.2
4	1	3	71.1	13.2	15.3	0.4
5	3	3	61.7	9.1	28.7	0.5
6	3	3	55.9	9.8	33.8	0.5
7	1	3	71.0	13.3	14.8	0.9
8	4	3	40.8	20.1	38.1	1.0
9	5	3	48.1	25.3	25.4	1.2
10	5	3	51.6	27.9	19.2	1.3
11	5	3	54.7	28.6	15.3	1.4
12	6	3	46.4	18.2	33.8	1.5
13	7	3	39.3	26.9	32.3	1.6
14	6	3	49.4	26.9	29.4	1.7
15	8	3	49.2	22.6	26.4	1.8
16	7	3	43.8	29.7	24.7	1.8
17	7	3	50.3	33.0	14.7	1.9
18	9	3	40.9	30.7	26.5	1.9
19	6	3	53.0	21.0	24.1	1.9
20	10	3	47.5	28.1	22.	2.0
21	11	3	57.0	17.0	23.9	2.1
22	12	3	65.2	14.0	19.3	1.55
23	13	3	60.8	17.9	19.0	2.2
24	14	3	55.2	17.7	24.6	2.5

Source: Hurst, H. J.; Novak, F.; Patterson, J. H., *Fuel* **1999**, 78, 1831-1840.

Some results



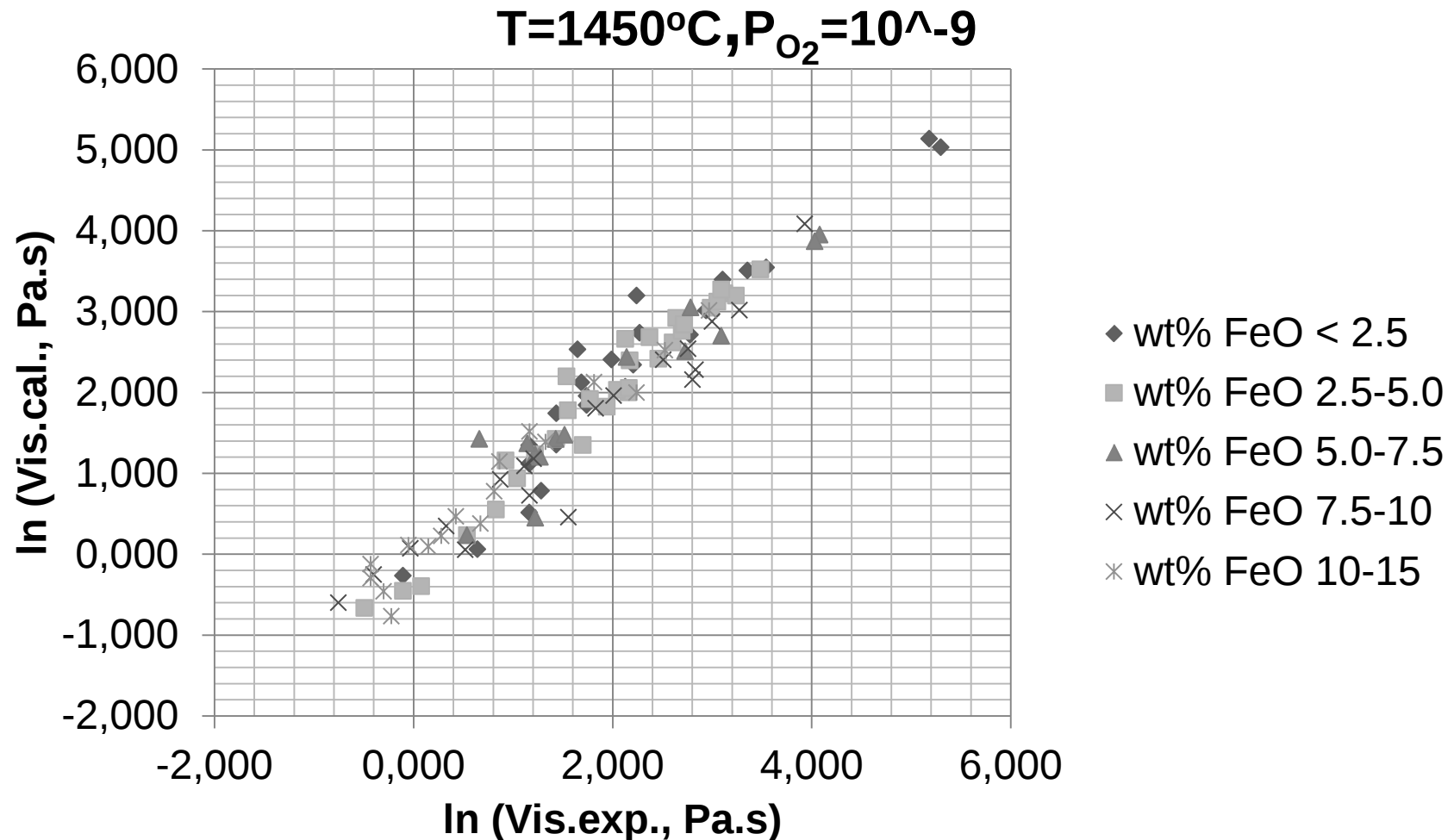
Source: Hurst, H. J.; Novak, F.; Patterson, J. H., *Fuel* **1999**, 78, 1831-1840.

Associate species employed for $\text{FeO}/\text{Fe}_2\text{O}_3$ containing systems

Compounds	Associate species	Structural units
FeO	Fe_2O_2	FeO
Fe_2O_3	Fe_2O_3	$\text{FeO}_{1.5}$
FeAl_2O_4	$\frac{2}{3} \cdot \text{FeAl}_2\text{O}_4$	$\text{Fe}_{0.5}\text{AlO}_2$
CaFe_2O_4	$\frac{2}{3} \cdot \text{CaFe}_2\text{O}_4$	$\text{Ca}_{0.5}\text{FeO}_2$
MgFe_2O_4	$\frac{2}{3} \cdot \text{MgFe}_2\text{O}_4$	$\text{Mg}_{0.5}\text{FeO}_2$
Fe_2SiO_4	$\frac{2}{3} \cdot \text{Fe}_2\text{SiO}_4$	Fe_2SiO_4
NaFeO_2	NaFeO_2	NaFeO_2
Na_2FeO_2	$\frac{2}{3} \cdot \text{Na}_2\text{FeO}_2$	Na_2FeO_2
KFeO_2	KFeO_2	KFeO_2
$\text{FeSi}_2\text{MgO}_6$	$\frac{1}{2} \cdot \text{FeSi}_2\text{MgO}_6$	$\text{Fe}_{0.5}\text{SiMg}_{0.5}\text{O}_3$
$\text{FeSi}_2\text{CaO}_6$	$\frac{1}{2} \cdot \text{FeSi}_2\text{CaO}_6$	$\text{Fe}_{0.5}\text{SiCa}_{0.5}\text{O}_3$
FeSiO_3	FeSiO_3	FeSiO_3
$\text{Fe}_2\text{Si}_5\text{Al}_4\text{O}_{18}$	$\frac{2}{11} \cdot \text{Fe}_2\text{Si}_5\text{Al}_4\text{O}_{18}$	$\text{Fe}_{0.4}\text{SiAl}_{0.8}\text{O}_{3.6}$
$\text{FeSiNa}_2\text{O}_4$	$\frac{1}{2} \cdot \text{FeSiNa}_2\text{O}_4$	$\text{FeSiNa}_2\text{O}_4$

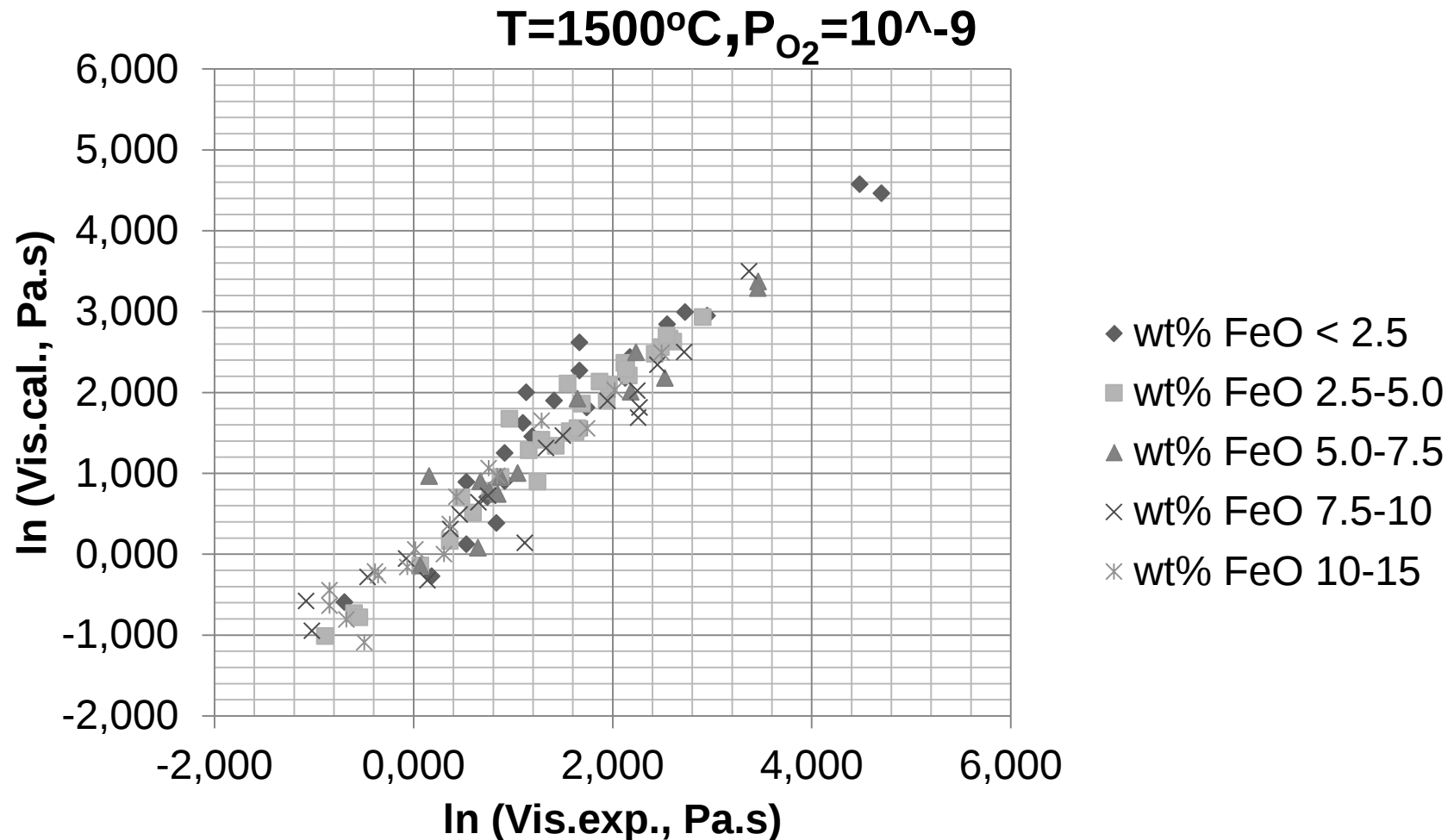
First result

The source of the experimental data: Hurst et al., Fuel 1999 & 2000

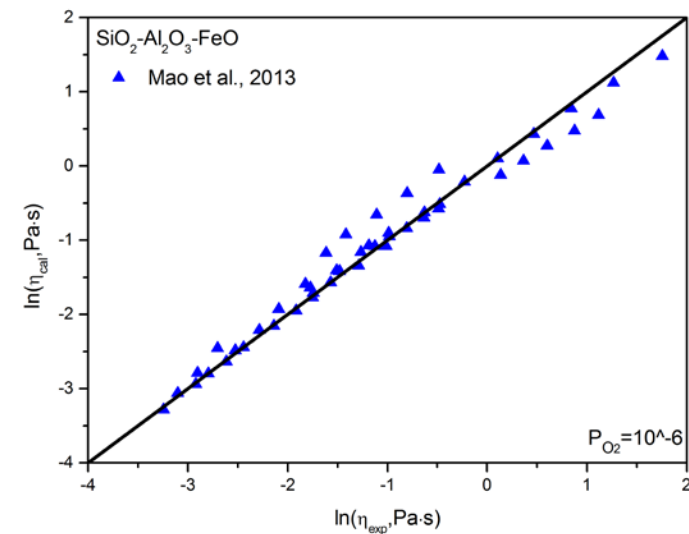
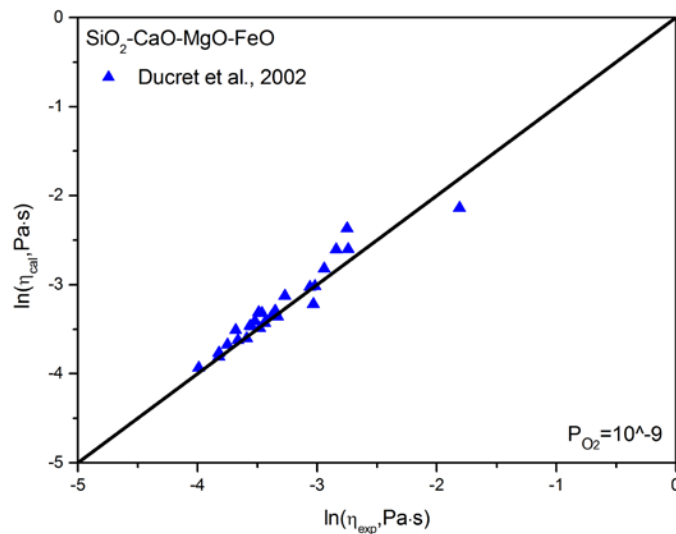
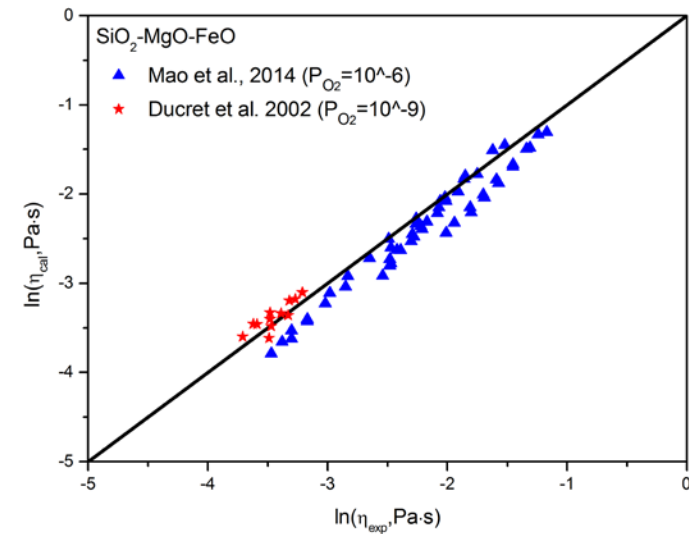
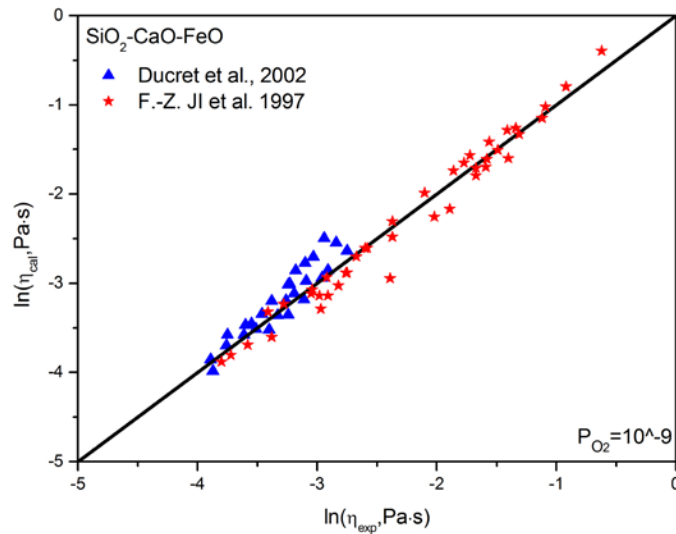


First result

The source of the experimental data: Hurst et al., Fuel 1999 & 2000

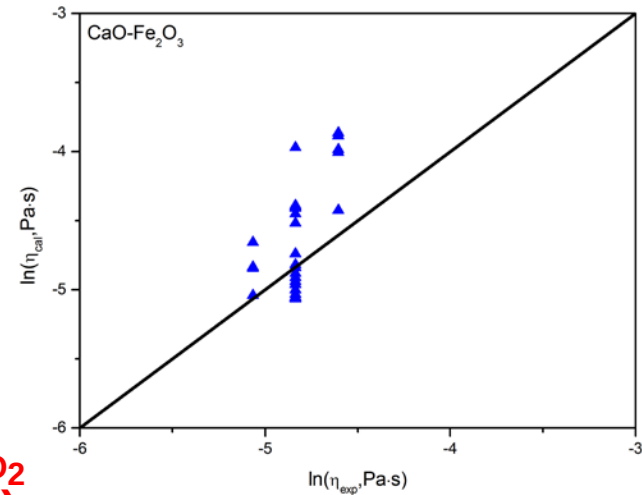
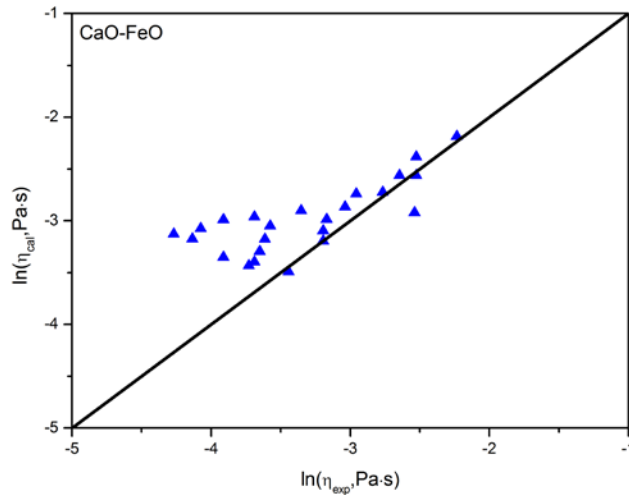


First result (known P_{O_2})

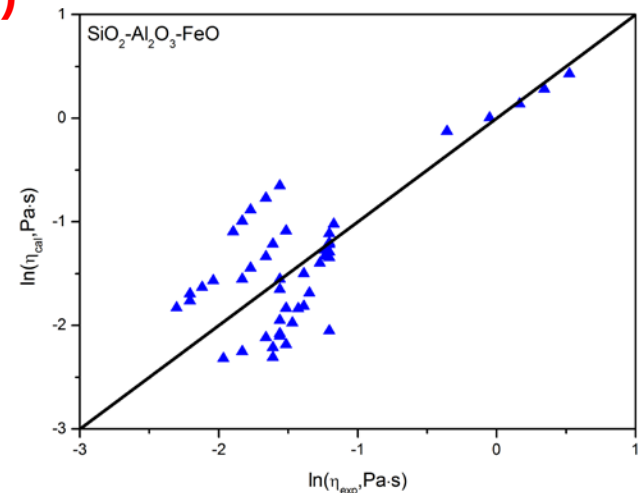
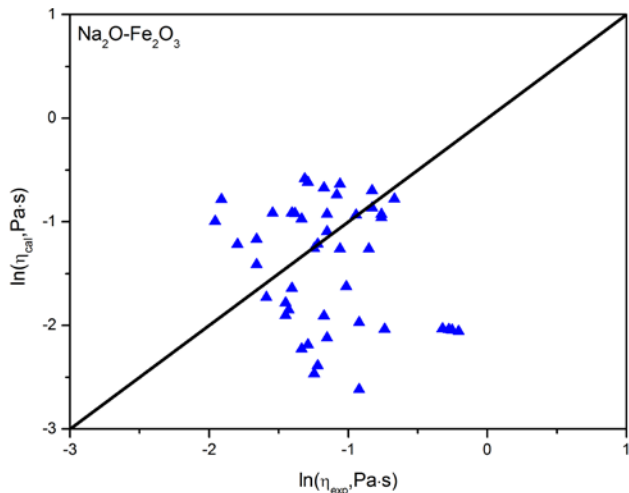


First result (unknown P_{O_2})

The source of the experimental data: SciGlass database



**Fix the P_{O_2}
(assumed)**



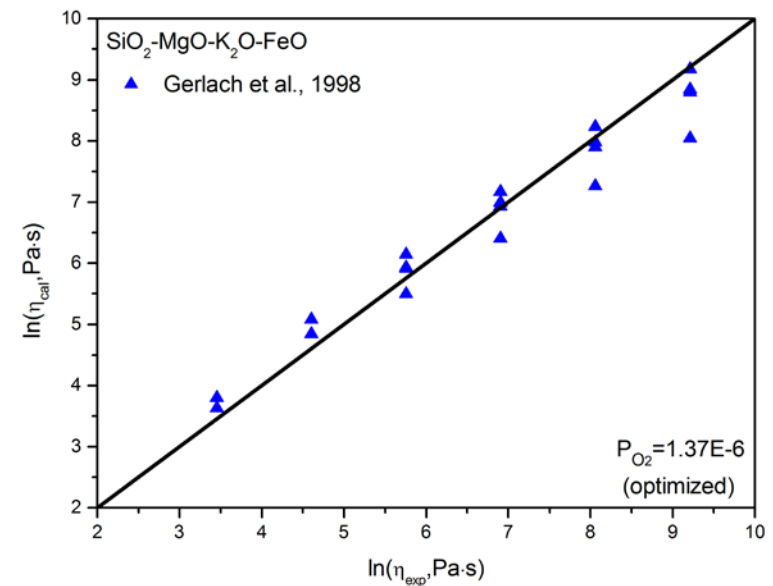
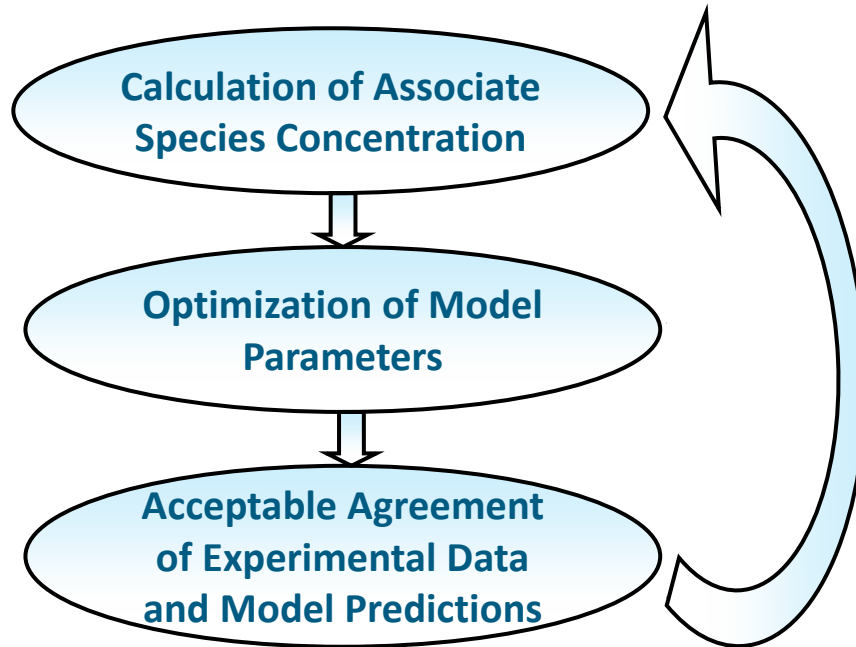
Estimated P_{O_2}

➤ Dealing with unclear atmospheres as follows:

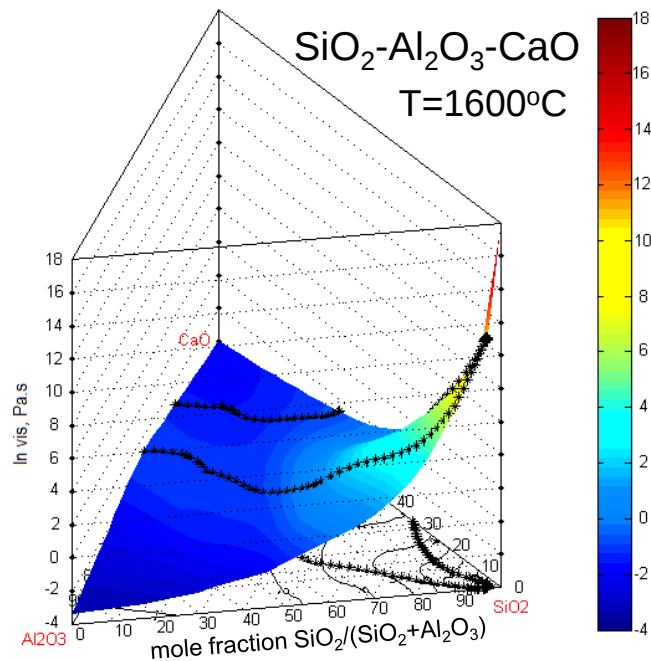
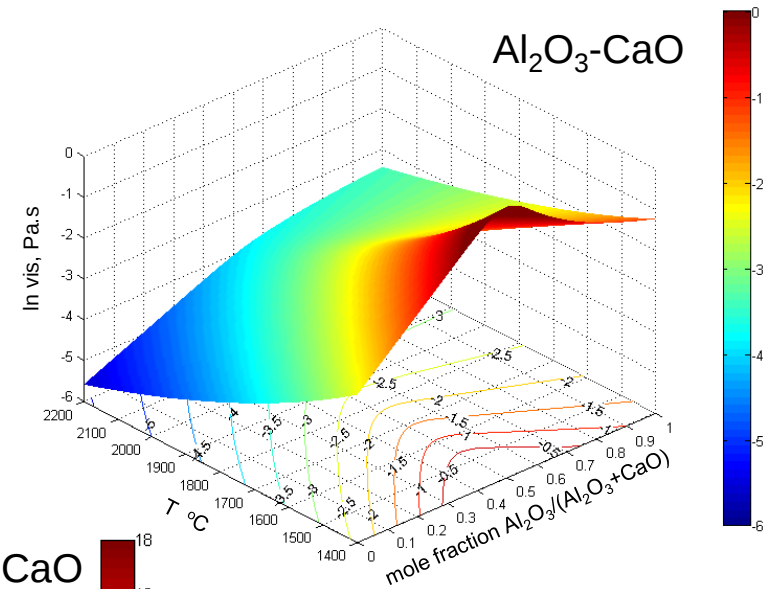
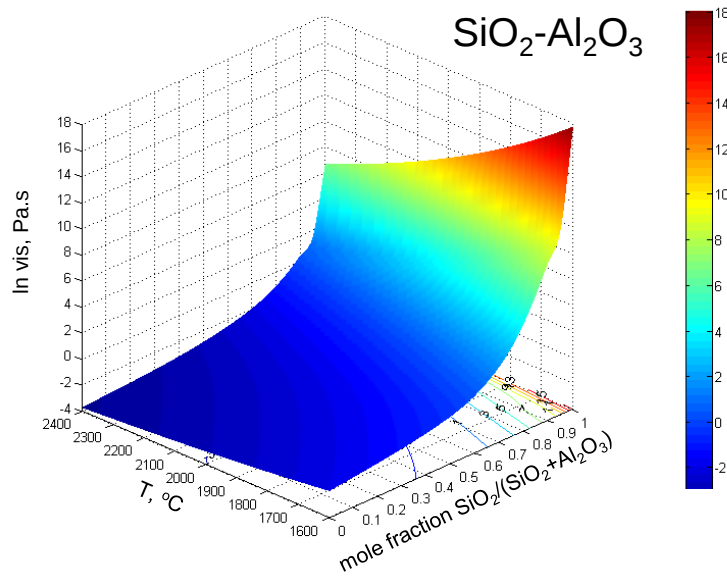
$$\left. \begin{array}{l} \bullet Fe^{2+}/\sum Fe \\ \bullet Fe^{3+}/\sum Fe \end{array} \right\} = \frac{Fe^{2+} \text{ or } Fe^{3+} \text{ based associate species}}{Fe \text{ based associate species}} \rightarrow P_{O_2} \text{ (Calculated)}$$

- | | | | |
|------------------------|---|-----------------------------------|---------------------------------------|
| • Reducing atmosphere | → | $P_{O_2} (10^{-12} \sim 10^{-6})$ | }
Treating P_{O_2} as a variable |
| • Oxidizing atmosphere | → | $P_{O_2} (10^{-6} \sim 0.21)$ | |
| • Neutral atmosphere | → | $P_{O_2} (10^{-12} \sim 10^{-6})$ | |

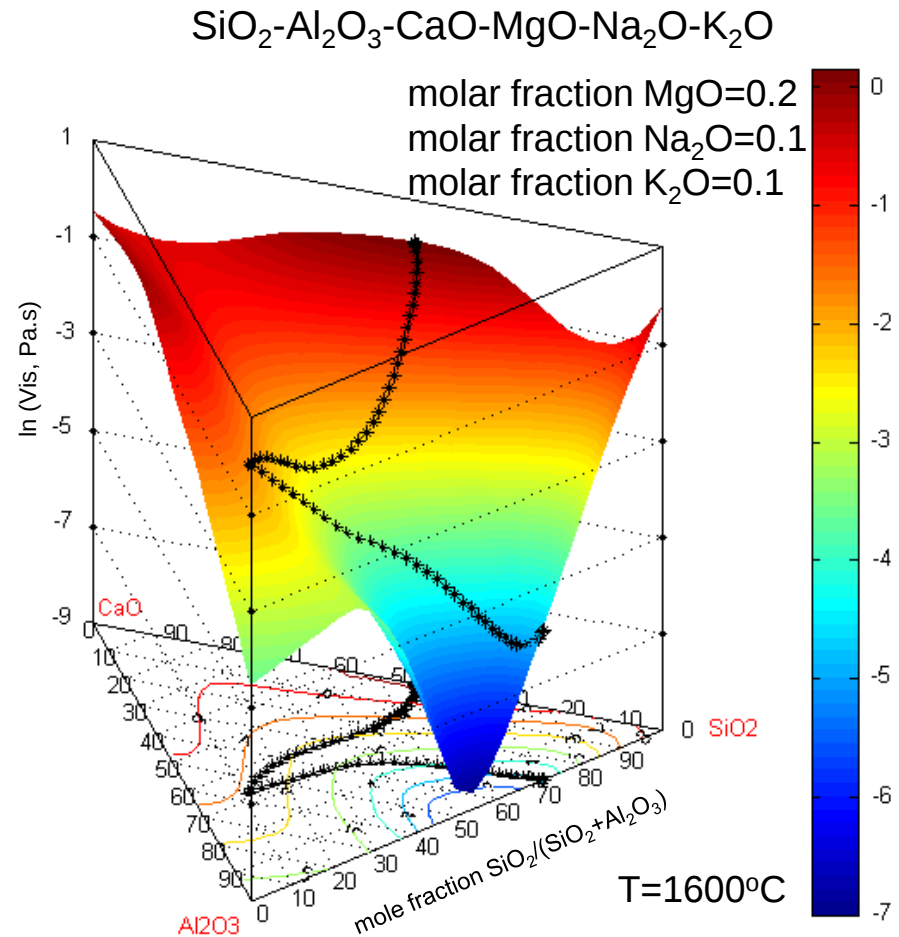
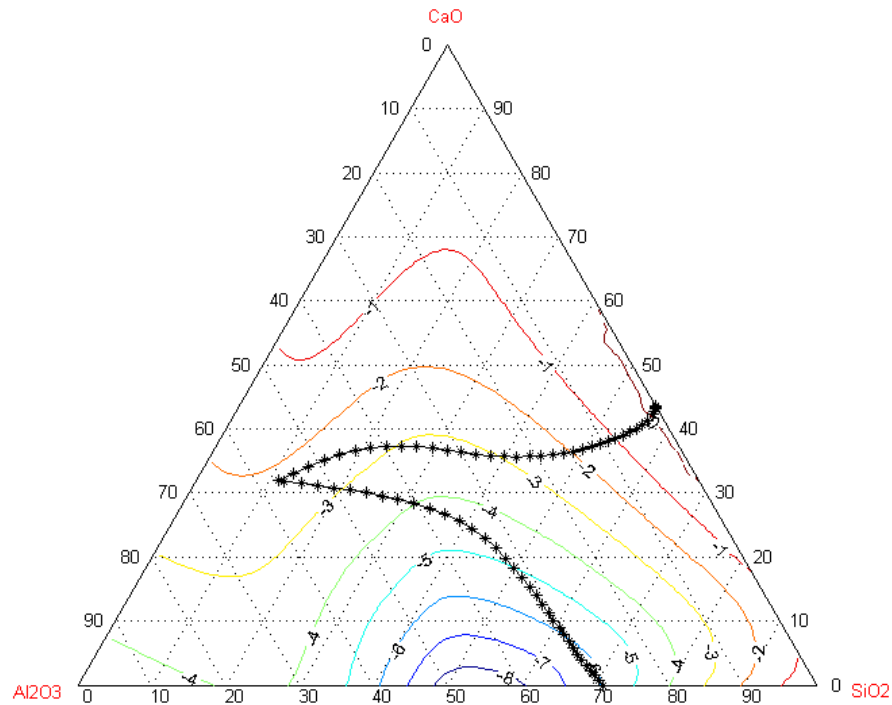
Modified optimization process



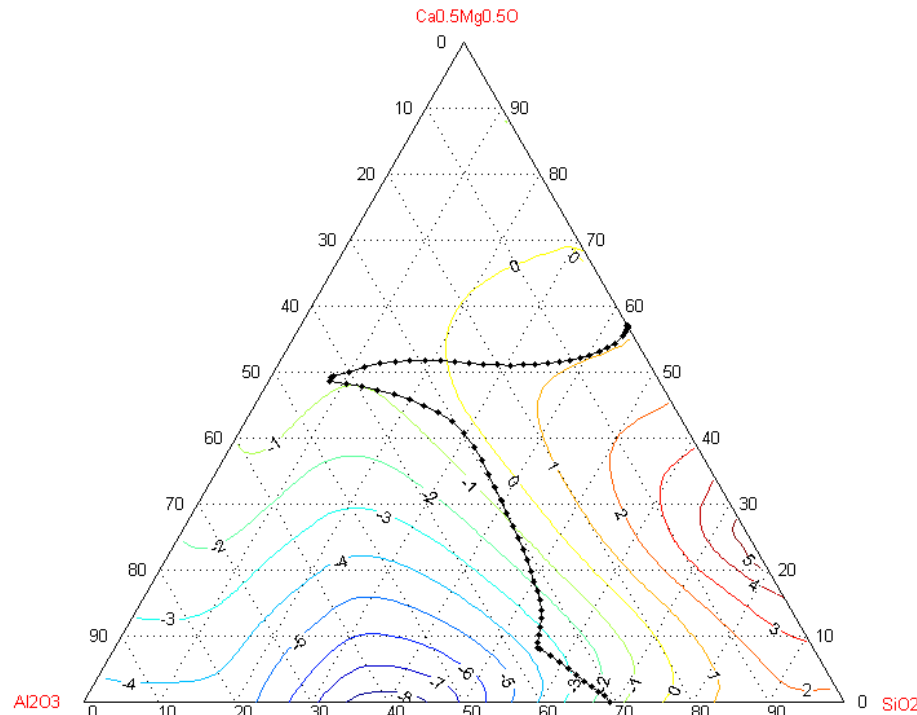
Viscosity surface I



Viscosity surface II



Viscosity surface III

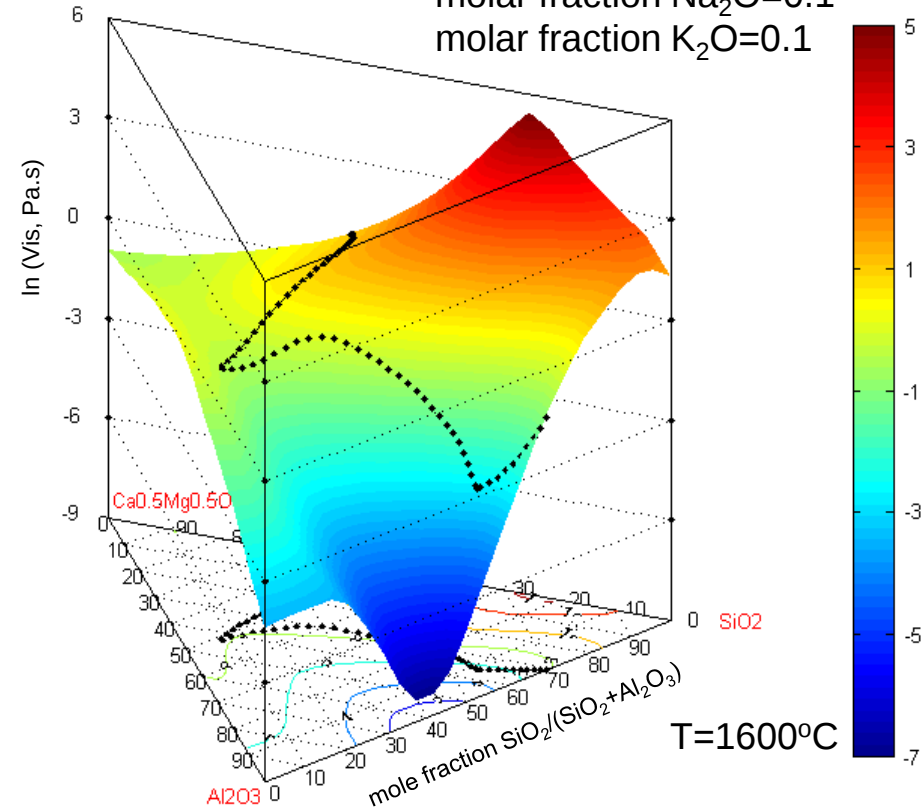


SiO_2 - Al_2O_3 - CaO - MgO - Na_2O - K_2O

molar ratio $\text{CaO}/\text{MgO}=1$

molar fraction $\text{Na}_2\text{O}=0.1$

molar fraction $\text{K}_2\text{O}=0.1$



Conclusions:

- The current structurally-based viscosity model is capable of predicting the viscosity for the fully liquid system $\text{SiO}_2\text{-Al}_2\text{O}_3\text{-CaO-MgO-Na}_2\text{O-K}_2\text{O-FeO-Fe}_2\text{O}_3$ and its subsystems;
- The partial pressure of oxygen is taken into account for the viscosity modelling of $\text{FeO/Fe}_2\text{O}_3$ containing system.

Outlook:

- Further analyzing available experimental data for $\text{FeO/Fe}_2\text{O}_3$ containing systems;
- Further optimizing the model parameters of the $\text{FeO/Fe}_2\text{O}_3$ containing systems;
- Considering the potential polymerization of Fe^{3+} -based quasi-tetrahedron structure units;
- Extending the current viscosity model from the fully liquid to the mixture of liquid and solid.

Thank you very much for your attention!