

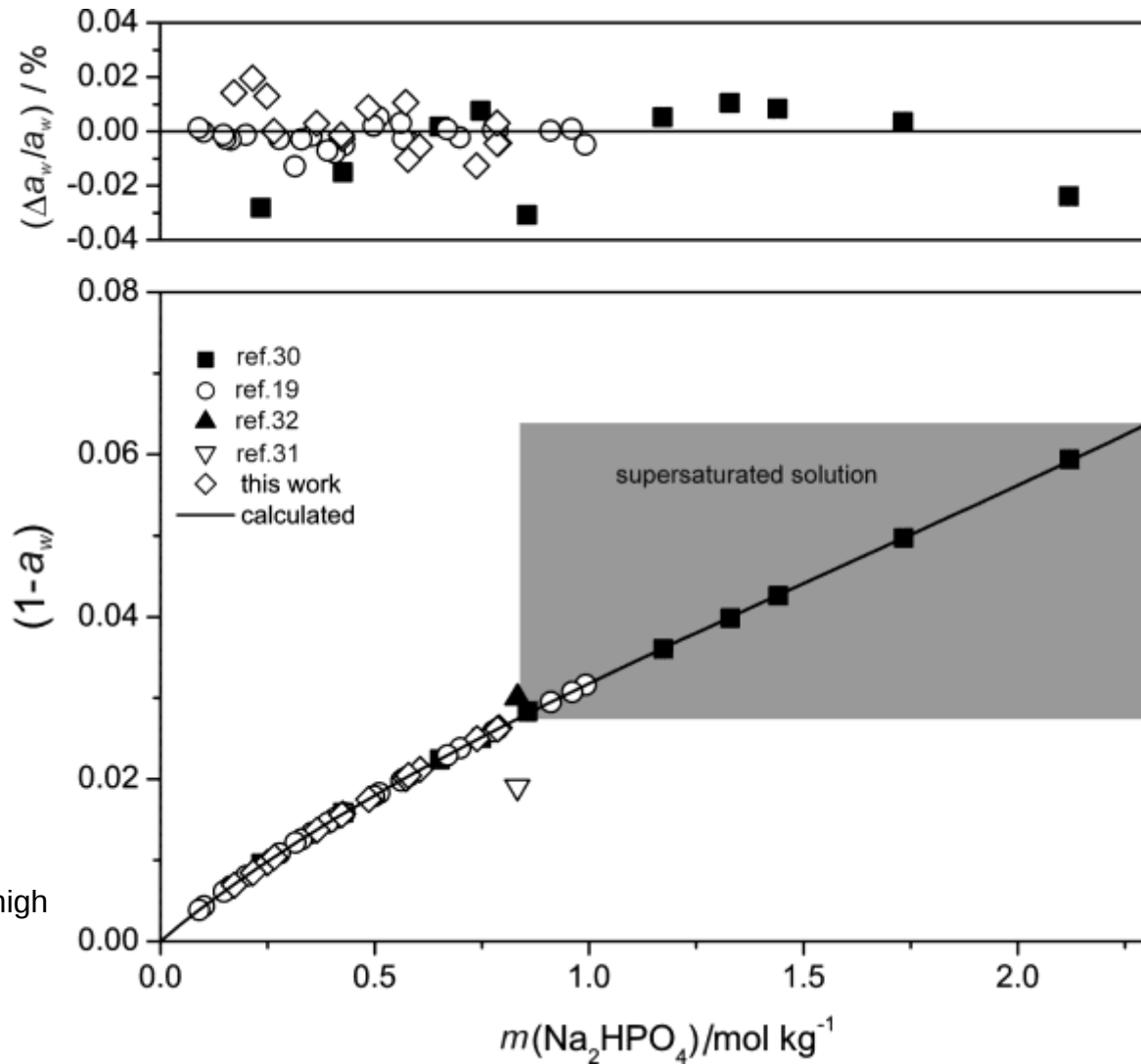


THEREDA Database Project: Extensions of the Pitzer database with respect to phosphate, alkaline earth metal sulfates, heavy metals, and fission products – first results

Helge C. Moog

Gesellschaft für Anlagen- und Reaktorsicherheit (GRS)

Na₂HPO₄, binary system, osmotic coefficient



Source:

T. Scharge, A.G. Muñoz, H.C. Moog
(2013): Thermodynamic model-ling of high
salinary phosphate solutions. I. Binary
systems.

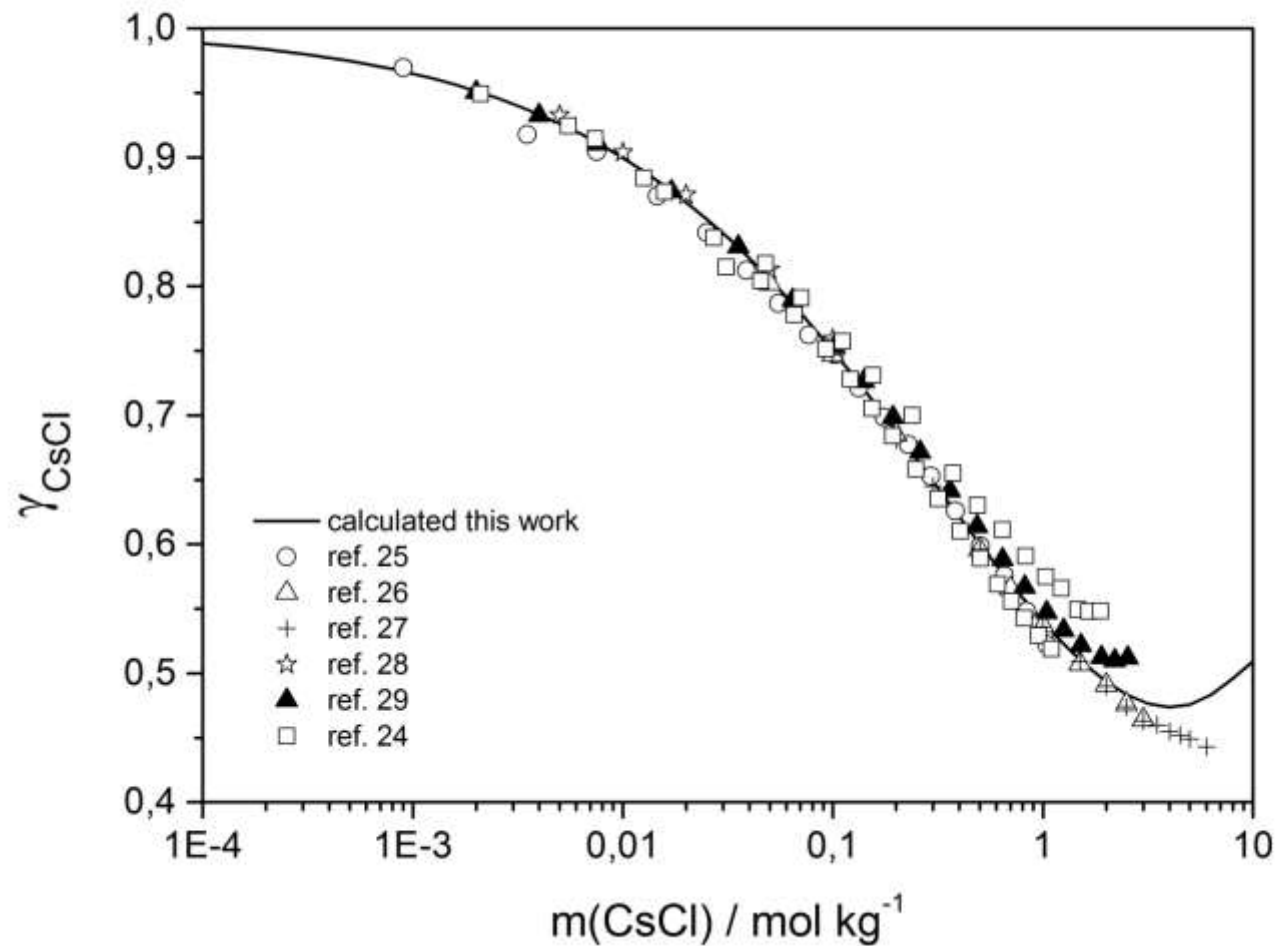
J. Chem. Thermodynamics 64 (2013)
249–256.

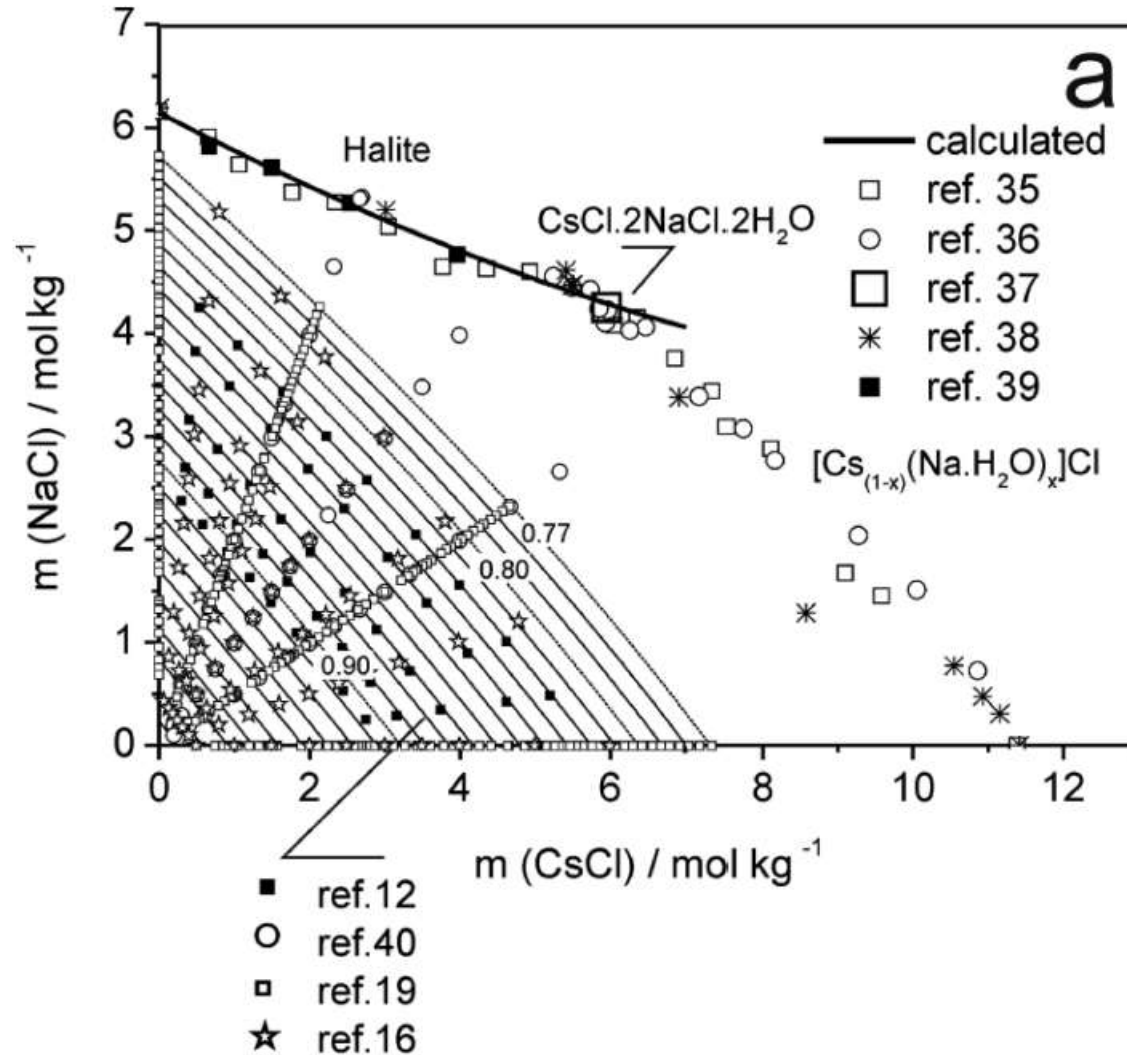
<http://dx.doi.org/10.1016/j.jct.2013.05.013>.

Phosphate, all data, summary

- PO_4^{3-} : relevant at $\text{pH} > 12$ only. Not very reliable data.
- HPO_4^{2-} , H_2PO_4^- : relevant species,
 - complete data for Na, K – Cl, SO_4
But: some data quality deterioration because of PO_4^{3-} as PrimaryMaster in THEREDA
 - With Ca, Mg: no data so far
- H_3PO_4 : not considered, relevant at $\text{pH} < 2$ only.

CsCl, binary system, low concentration



CsCl-NaCl-H₂O, all data

Cs, all data, summary

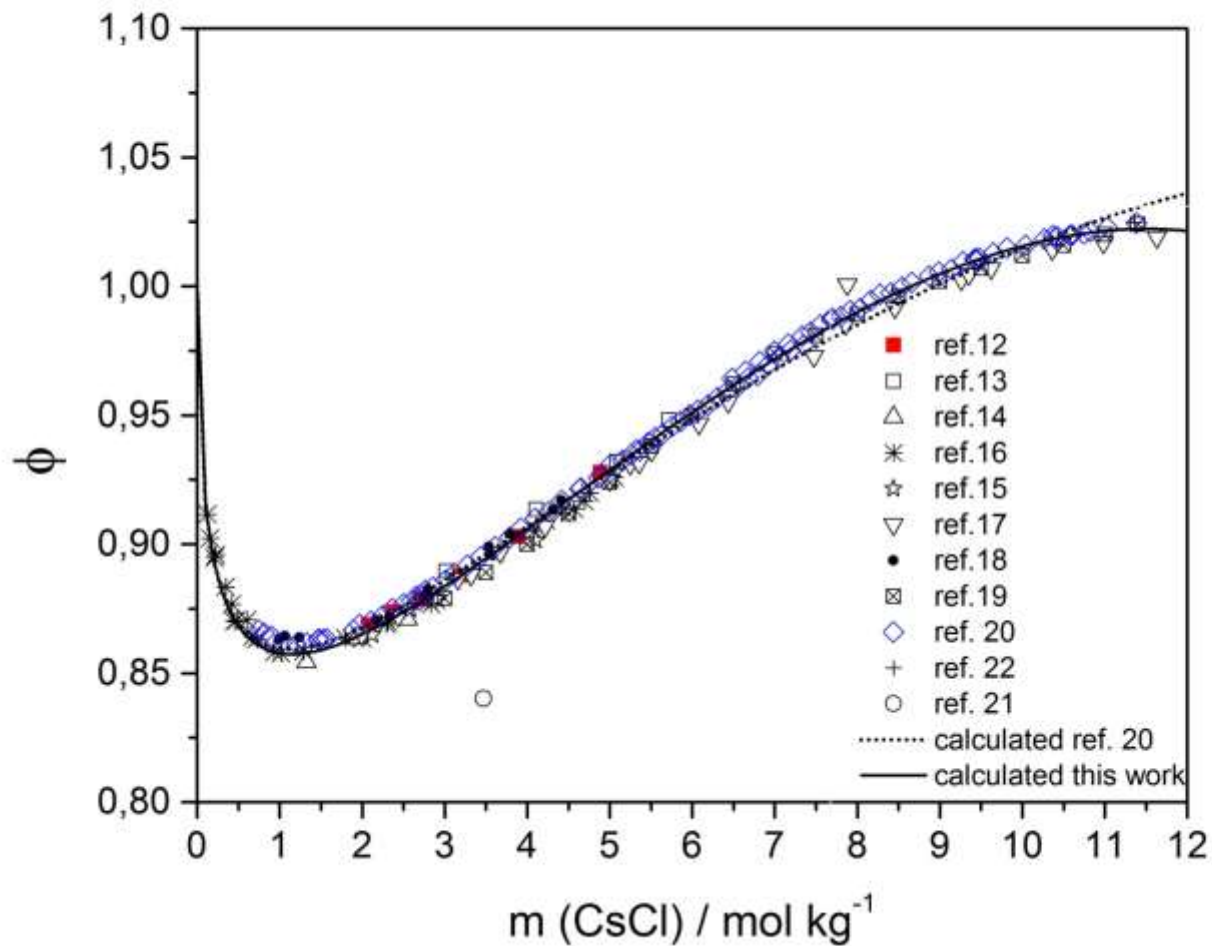
System			PP	logK
Cs	Cl		✓	✓
Cs	SO4		✓	✓
Cs	Cl	Na	✓	✓
Cs	Cl	K	✓	
Cs	Cl	Mg	✓	✓
Cs	Cl	Ca	✓	(✓)
Cs	SO4	Na	✓	✓
Cs	SO4	K	✓	(✓)
Cs	SO4	Mg	✓	✓
Cs	SO4	Ca		
Cs	Cl	SO4	✓	(✓)

Source:

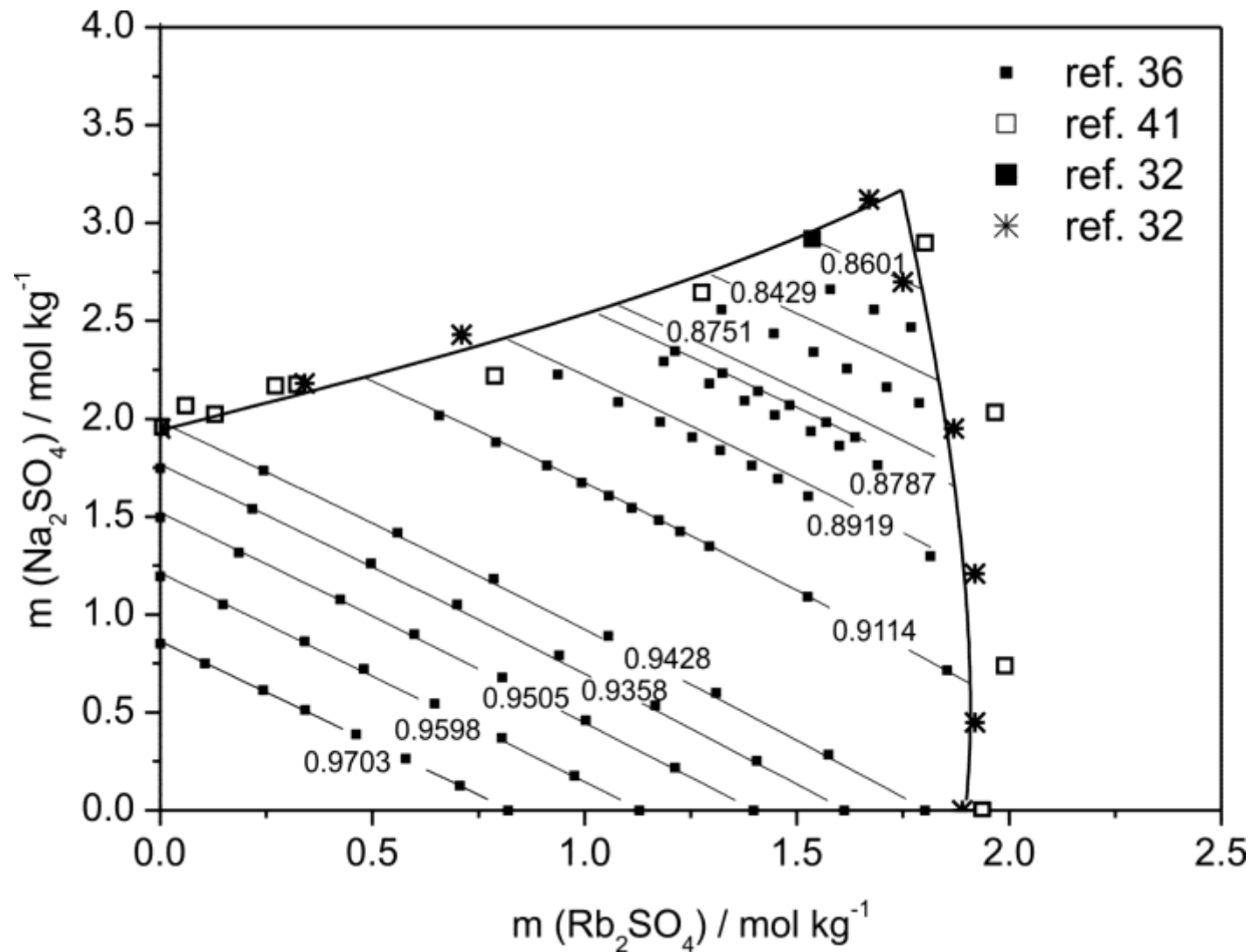
T. Scharge, A. G. Munoz, and H. C. Moog: Activity Coefficients of Fission Products in Highly Salinary Solutions of Na⁺, K⁺, Mg²⁺, Ca²⁺, Cl⁻, and SO₄²⁻: Cs⁺. J. Chem. Eng. Data 2012, 57, 1637-1647.
[dx.doi.org/10.1021/je200970v](https://doi.org/10.1021/je200970v).

T. Scharge, A. G. Munoz, and H. C. Moog: Addition to "Activity Coefficients of Fission Products in Highly Salinary Solutions of Na⁺, K⁺, Mg²⁺, Ca²⁺, Cl⁻, and SO₄²⁻: Cs⁺". J. Chem. Eng. Data 2012, 57 (6), 1637-1647. DOI: 10.1021/je200970v.

www.thereda.de >> THEREDA Data Query >> Tailored databases >> 5th release

RbCl-H₂O, osmotic coefficient

Rb₂SO₄-Na₂SO₄-H₂O, solubilities and iso-activity lines



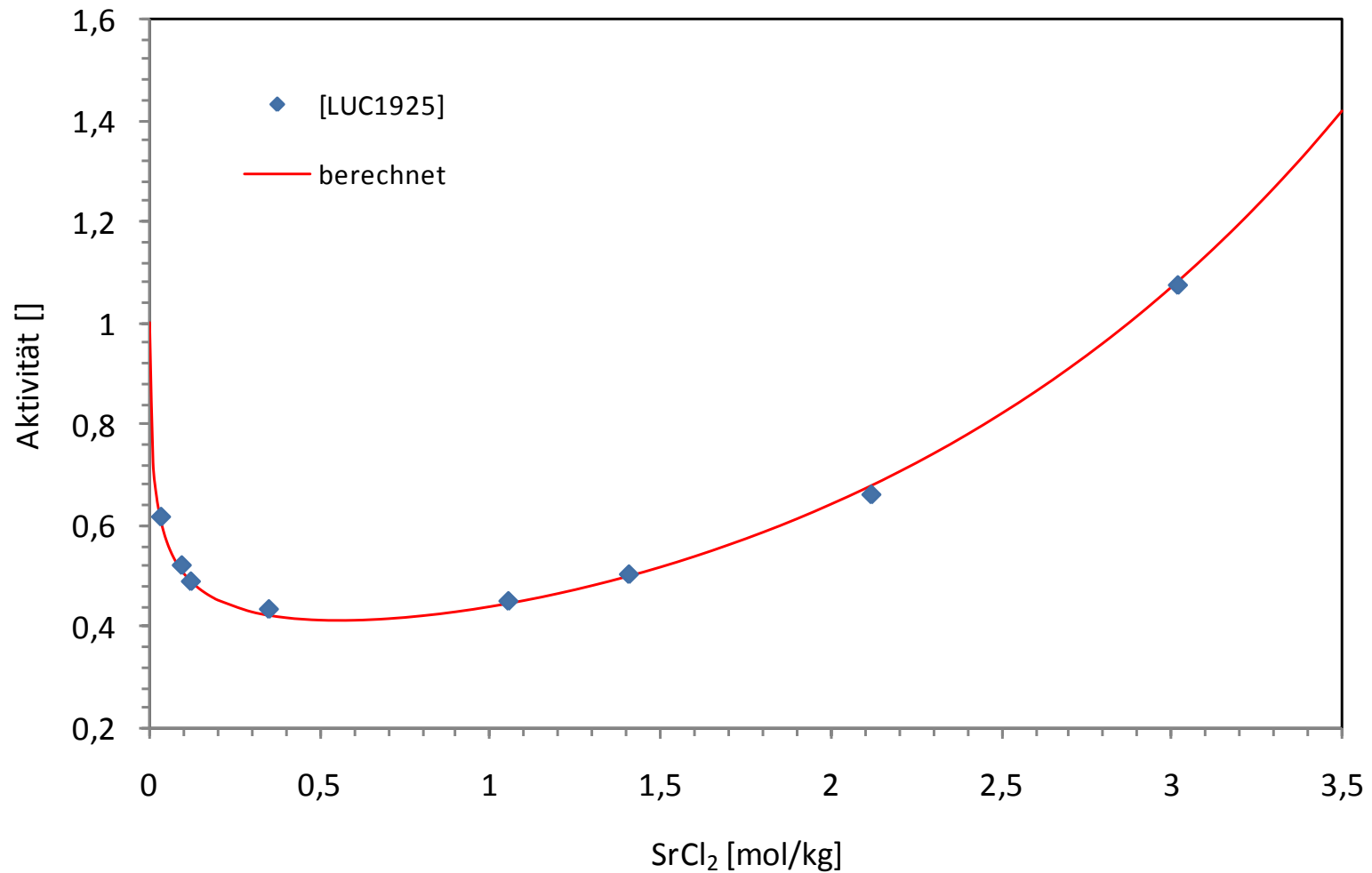
Rb, all data, summary

System			PP	logK
Rb	Cl		✓	✓
Rb	SO4		✓	✓
Rb	Cl	Na	✓	(✓)
Rb	Cl	K	(✓)	(✓)
Rb	Cl	Mg	✓	(✓)
Rb	Cl	Ca	-	-
Rb	SO4	Na	✓	(✓)
Rb	SO4	K	✓	-
Rb	SO4	Mg	-	✓
Rb	SO4	Ca	-	-
Rb	Cl	SO4	✓	(✓)

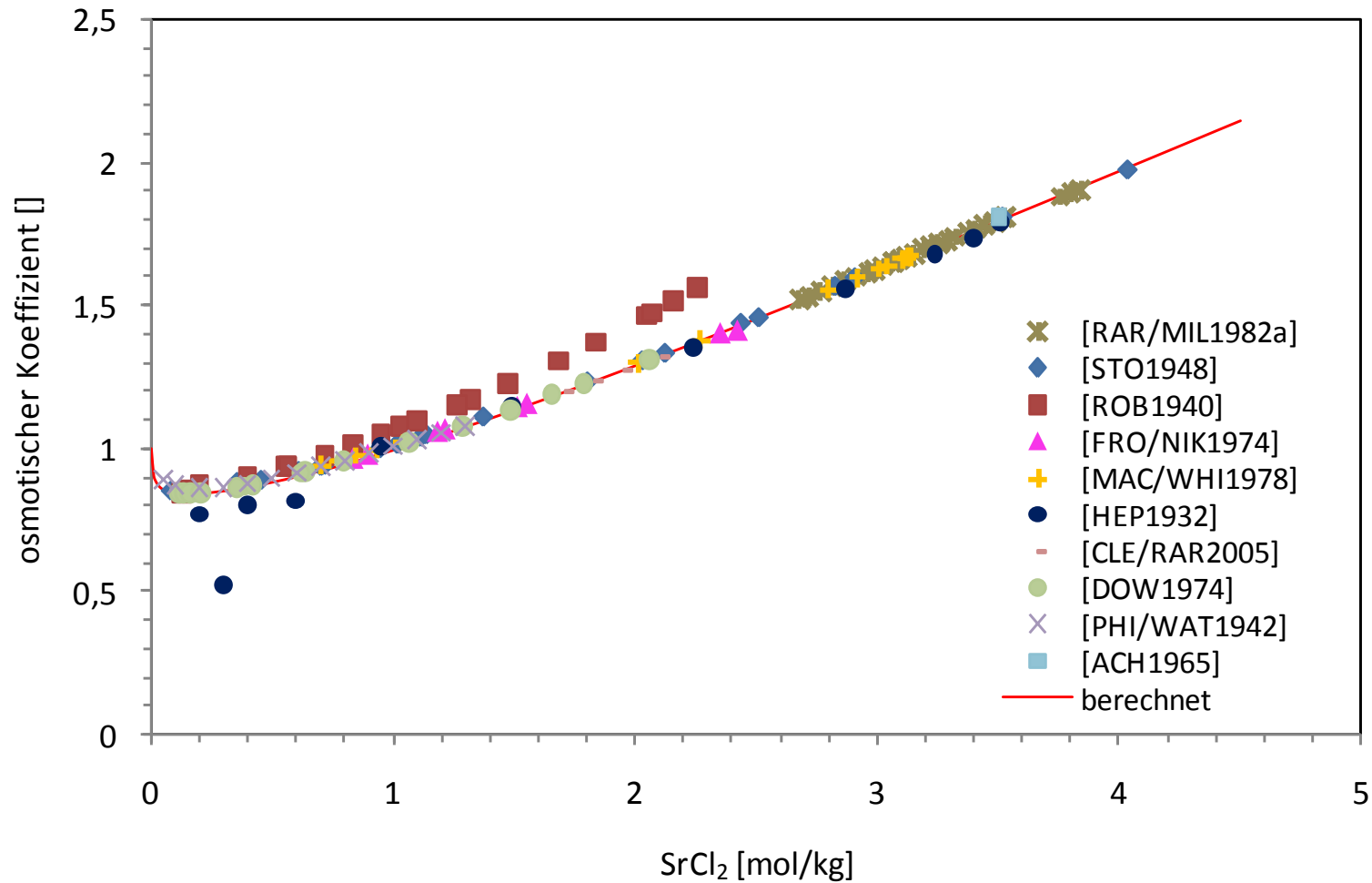
Source:

T. Scharge, A. G. Munoz, and H. C. Moog: Activity Coefficients of Fission Products in Highly Salinary Solutions of Na⁺, K⁺, Mg²⁺, Ca²⁺, Cl, and SO₄²⁻: Rb⁺. (in preparation)

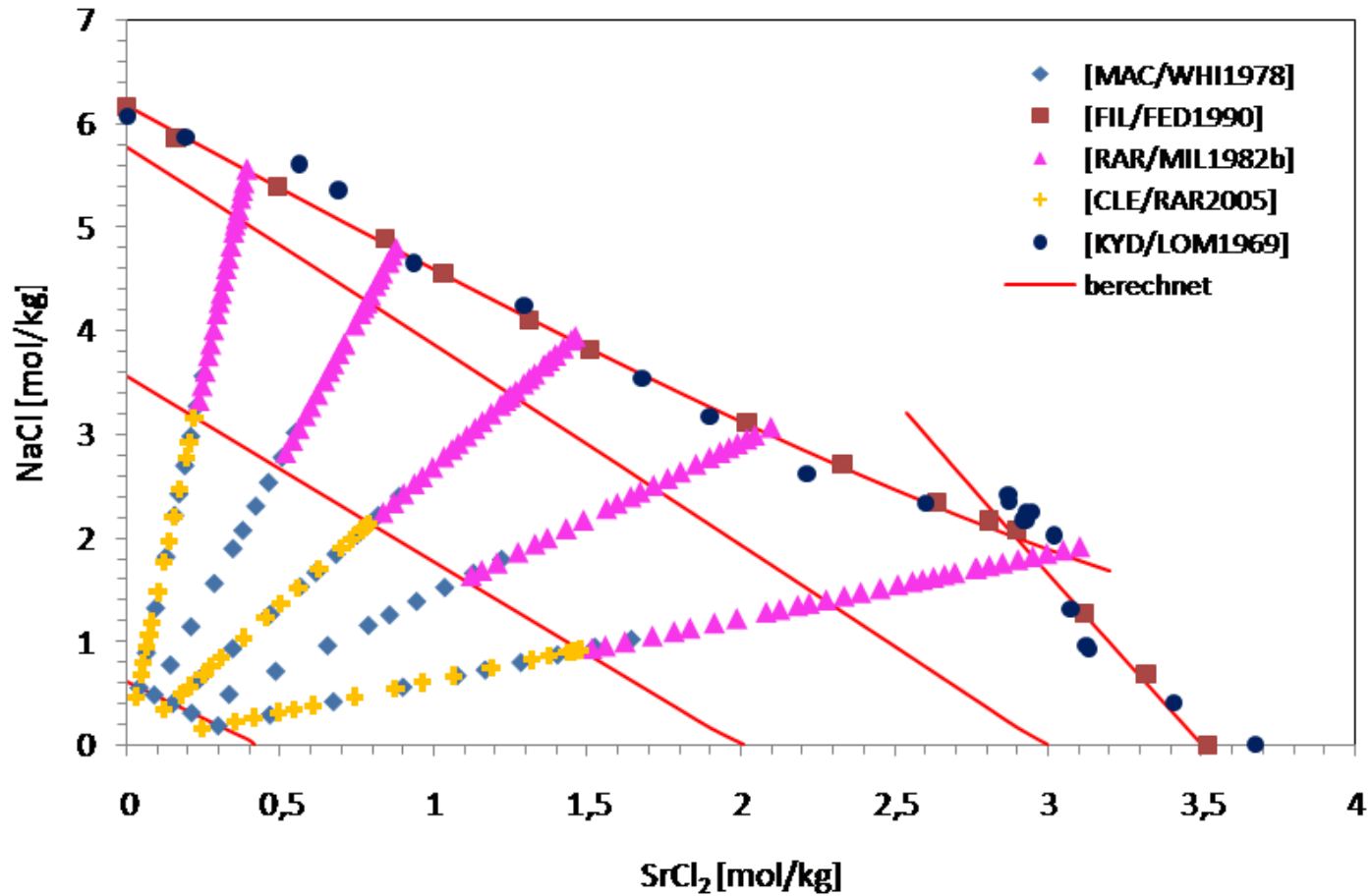
SrCl₂-H₂O, mean activity coefficient



SrCl₂-H₂O, osmotic coefficient



SrCl₂-NaCl-H₂O, 298.15K



Sr, all data, summary for 298.15K

System			PP	logK
Sr	Cl		✓	✓
Sr	SO4		✓	✓
Sr	Cl	Na	✓	(✓)
Sr	Cl	K	✓	(✓)
Sr	Cl	Mg	-	-
Sr	Cl	Ca	-	-
Sr	SO4	Na	✓	(✓)
Sr	SO4	K	-	-
Sr	SO4	Mg	-	-
Sr	SO4	Ca	-	-
Sr	Cl	SO4	-	-

Source:

T. Schrage, A. G. Munoz, and H. C. Moog: Activity Coefficients of Fission Products in Highly Salinary Solutions of Na⁺, K⁺, Mg²⁺, Ca²⁺, Cl⁻, and SO₄²⁻: Sr²⁺. (in preparation)

Number or processed sources

Element	Number of sources	Number of binary data points	Number of ternary data points
Cs	77	377	830
Rb	51	235	271
Sr	49	147	406
P	249 (111 Na/K) (138 Ca/Mg/H ₃ PO ₄)	400	1251

High-temperature extensions for Sr, Ba, Ra, Pb - Motivation

- Some interest arose because of modeling of scale formations in geothermal power plants
- Depending on the particular site these scales may contain (Sr, Ba, Ra)-Sulfates/Carbonates, PbSO_4 (Anglesite), PbCO_3 (Cerussite) or Pb(OH)Cl (Laurionite), Sulfides, or even elemental Pb, Cu.
- Temperatures typically 150-250°C, pressure up 450 bar
- Geothermal power plants already in operation, therefore quick answers required!

Temperature- und Pressure dependence of chemical equilibria

$$\Delta_r G(T) = \underbrace{\Delta_r H(T_0)}_{\boxed{\Delta_f H(T_0)}} + \int_{T_0}^T \underbrace{\Delta_r C_p(T)}_{\boxed{C_p(T)}} dT - T \left(\underbrace{\Delta_r S(T_0)}_{\boxed{S(T_0)}} + \int_{T_0}^T \frac{\Delta_r C_p(T)}{T} dT \right) + \underbrace{\Delta_r V(T_0)}_{\boxed{V(T_0)} = \text{const. (Assumption)}} \int_{T_0}^T dp$$

Need to be known for all educts and products

$$\Delta_r G(T) = -RT \ln \boxed{K(T)}$$

- = Primary data which need to be looked for in the literature
- The equilibrium constant $\ln K(T)$ is an integral quantity which contains H , S , and $C_p(T)$ for all educts and products
- Upon creation of the database basic thermodynamic rules for internal calculation need to be obeyed (internal numerical consistency of data)

Present state and workflow

- At present

- Na, K, Mg, Ca – Cl, SO₄ – H₂O (up to 120°C)
- Na, K, Mg, Ca – HCO₃ – H₂O (for 25°C only)
- Dissociation constant for silicic acid (up to 100°C)



- Extension, due summer 2013

- Na, K, Mg, Ca – Cl, SO₄ – H₂O (up to 200°C)
- Na, K, Mg, Ca – HCO₃ – H₂O (up to 160°C)
- Calcite und Anhydrite
 - 25 – 160°C
 - 1 – 450 bar
 - NaCl 0 – 4M, CaCl₂ 0 – 2M

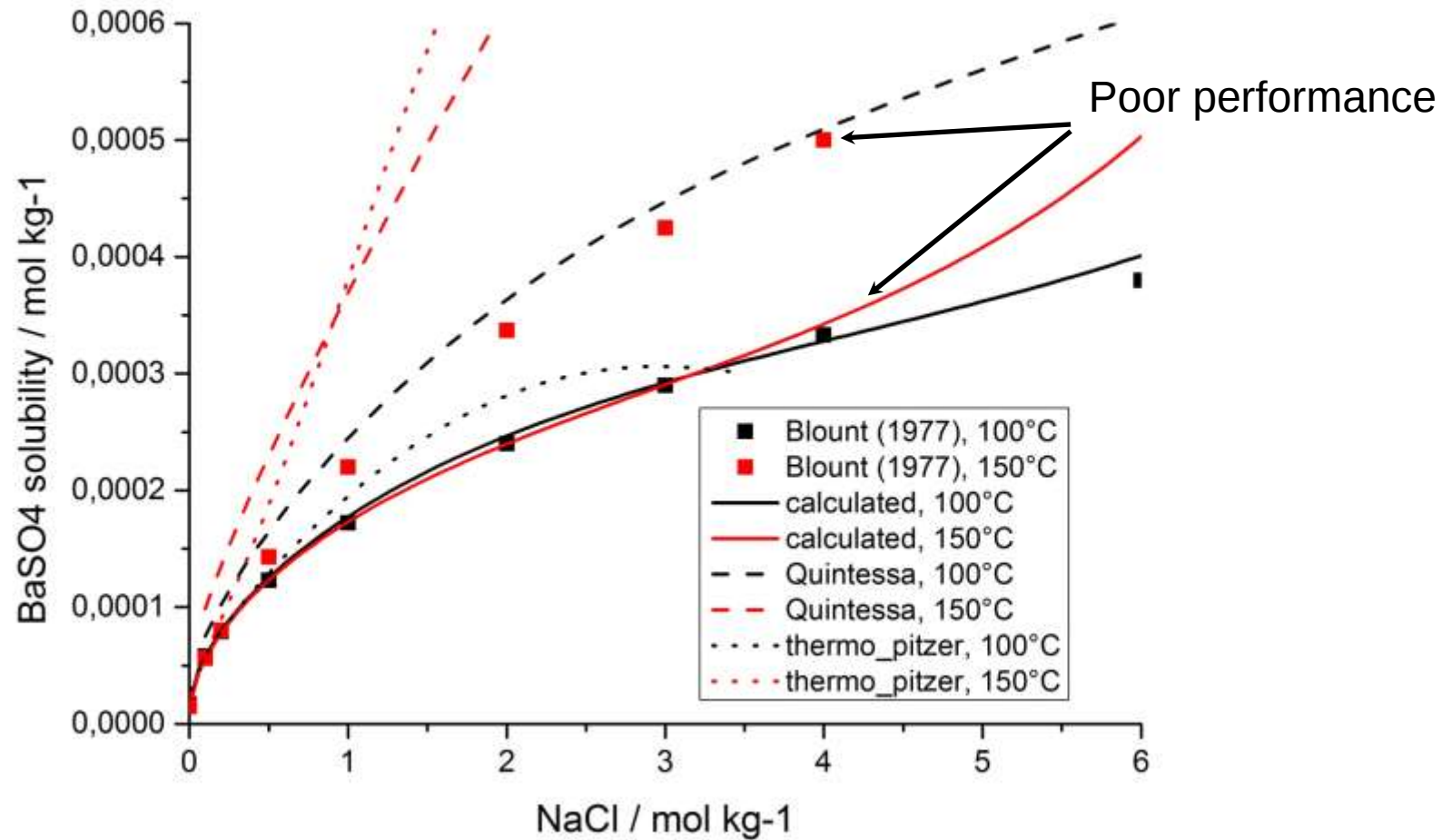


- EA-Sulfates: Ba, Sr, Ra

- Lead

- Pb(OH)Cl(cr) (Laurionite)
- PbSO₄(cr) Anglesite
- ...?

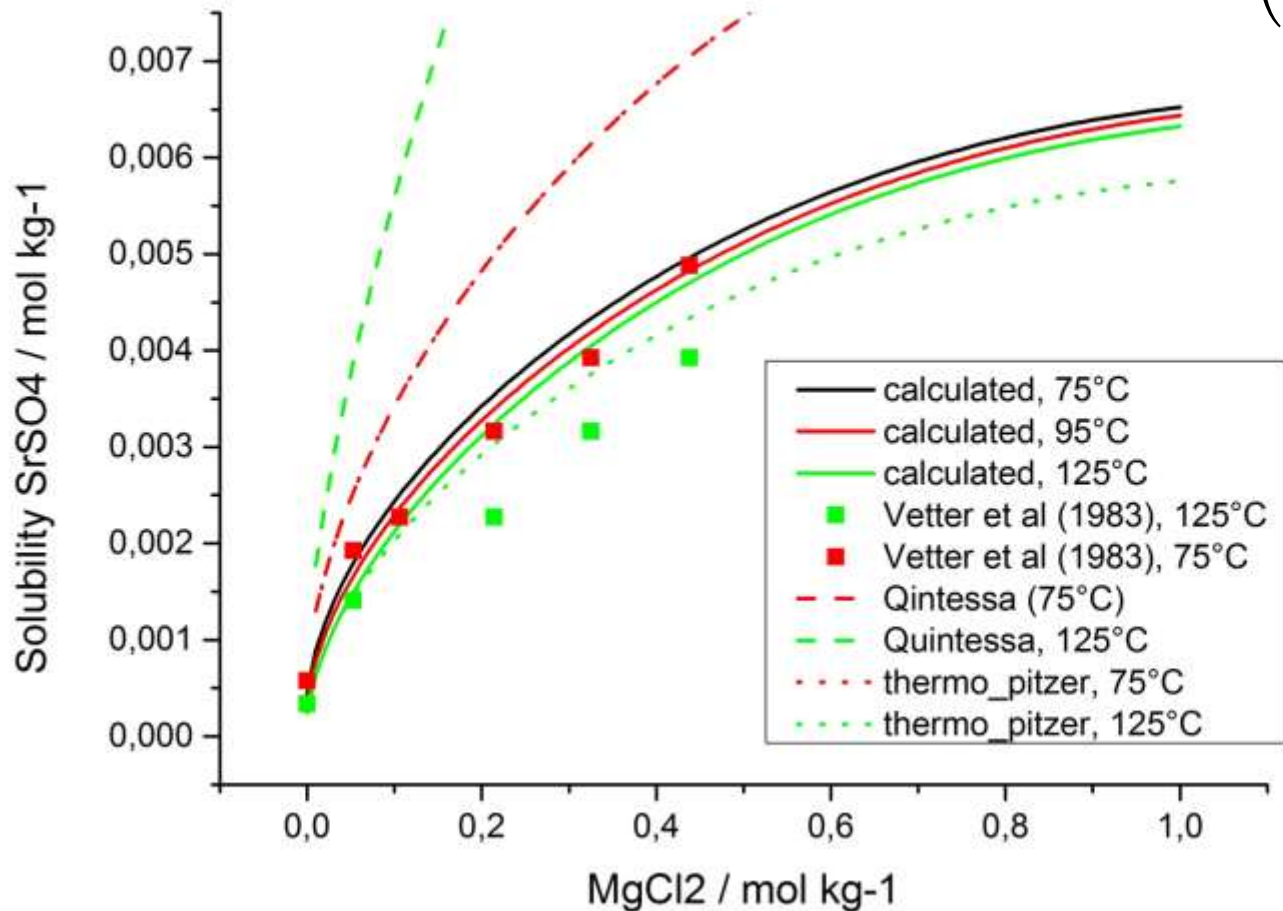
Polythermal BaSO₄-solubility in NaCl-solution



Polythermal SrSO₄-solubility in MgCl₂-solution

Estimation of $\log K(\text{SrSO}_4(\text{aq})(T))$:

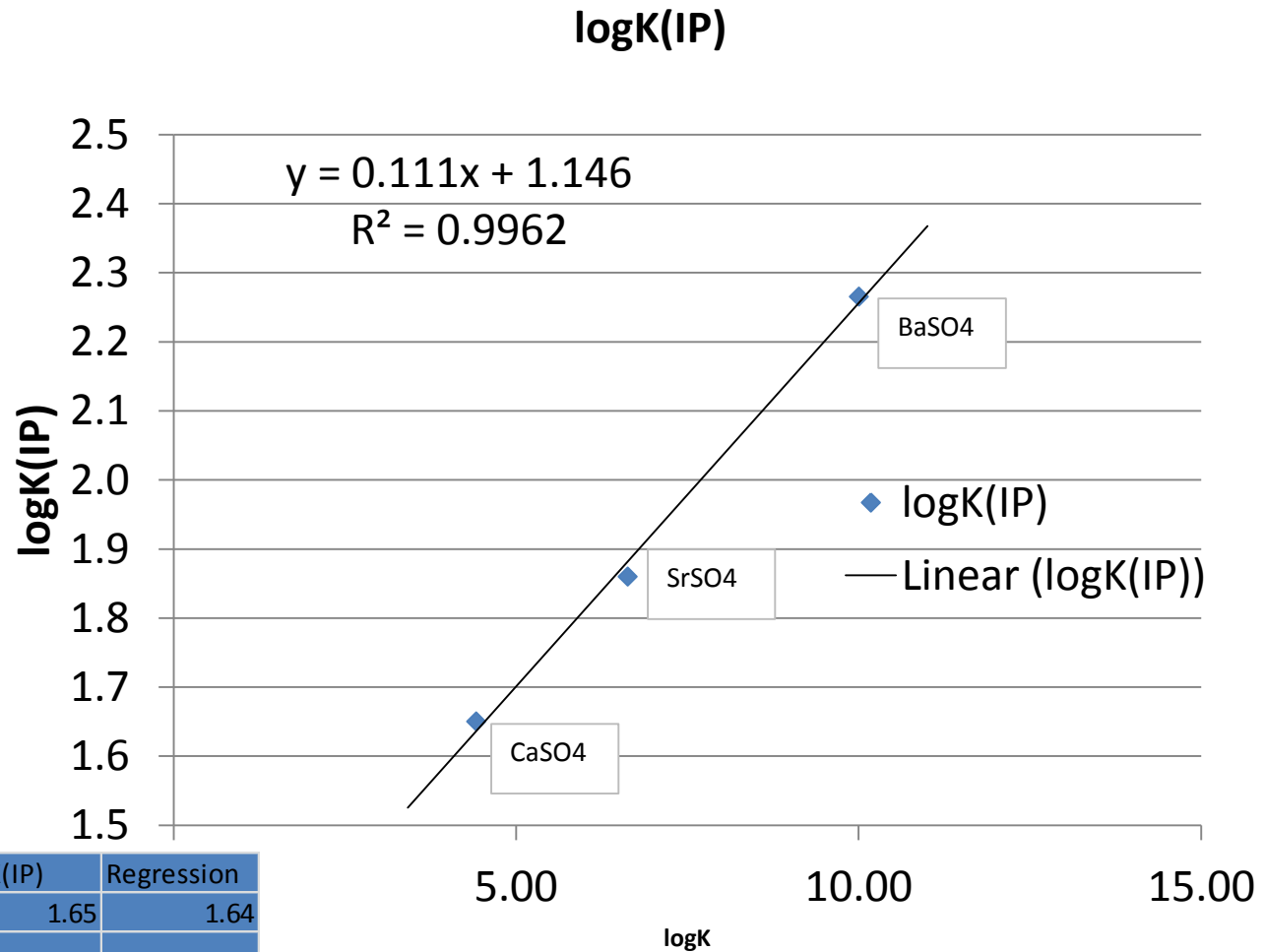
$$\ln K(T) = \left(\ln K^0 - \frac{\Delta_r H}{RT^0} \right) + \frac{\Delta_r H}{R} \left(\frac{1}{T} \right)$$



Estimates for Ra (summary)

- Association constant: linear correlation of $\log K$ (ion pair) and $\log$ (anhydrous sulfate)
- T-dependence of $\log K$ ($\text{RaSO}_4(\text{cr})$) in analogy to $\text{BaSO}_4(\text{cr})$
- T-dependence of Pitzer parameters in analogy to those for BaCl_2

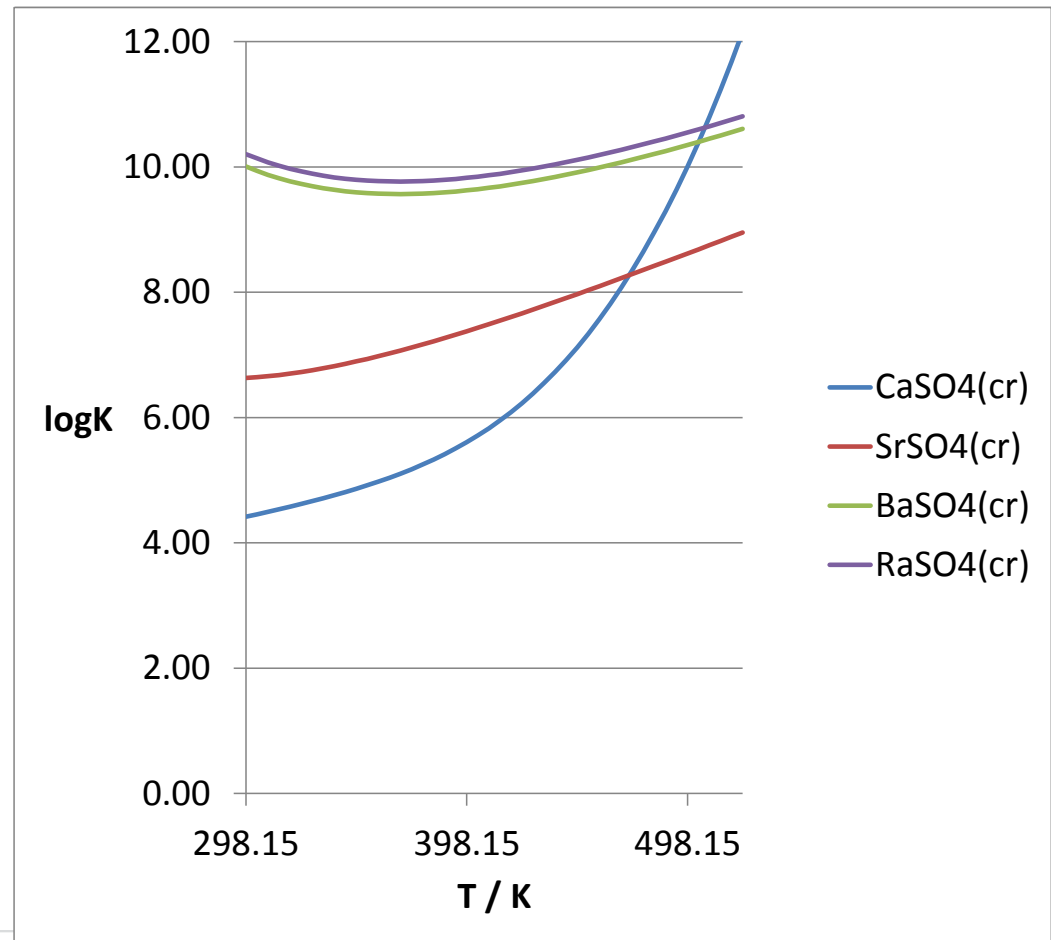
Estimate of the association constant for the reaction
 $\text{Ra}^{2+} + \text{SO}_4^{2-} \rightarrow \text{RaSO}_4$



	logK	logK(IP)	Regression
CaSO4	4.42	1.65	1.64
MgSO4			
SrSO4	6.63	1.86	1.88
BaSO4	10.01	2.27	2.26
RaSO4	10.21		2.28

Estimate of the temperature dependence of the solubility constant for $\text{RaSO}_4(\text{cr})$

logK ($\text{RaSO}_4(\text{cr})$): Paige C. R., Kornicker W. A., Hileman O. E. and Snodgrass W. J. (1998) Solution equilibria for uranium ore processing: the $\text{BaSO}_4\text{--H}_2\text{SO}_4\text{--H}_2\text{O}$ system and the $\text{RaSO}_4\text{--H}_2\text{SO}_4\text{--H}_2\text{O}$ system. *Geochim. Cosmochim. Acta* 62, 15–23.



	LOGK298	log10K(T) (absolut)	T	T2	T-1	T-2	log10(T)
CaSO4(cr)	4.42	-4186.19902	-2.47533492	0.00130507	85377.6407	0	1829.21353
SrSO4(cr)	6.63	-97.3119303	0	0	4474.24073	0	35.9422
BaSO4(cr)	10.01	-119.454	0	0	6864.58887	0	43.014
RaSO4(cr)	10.21	-119.254			6864.58887		43.014

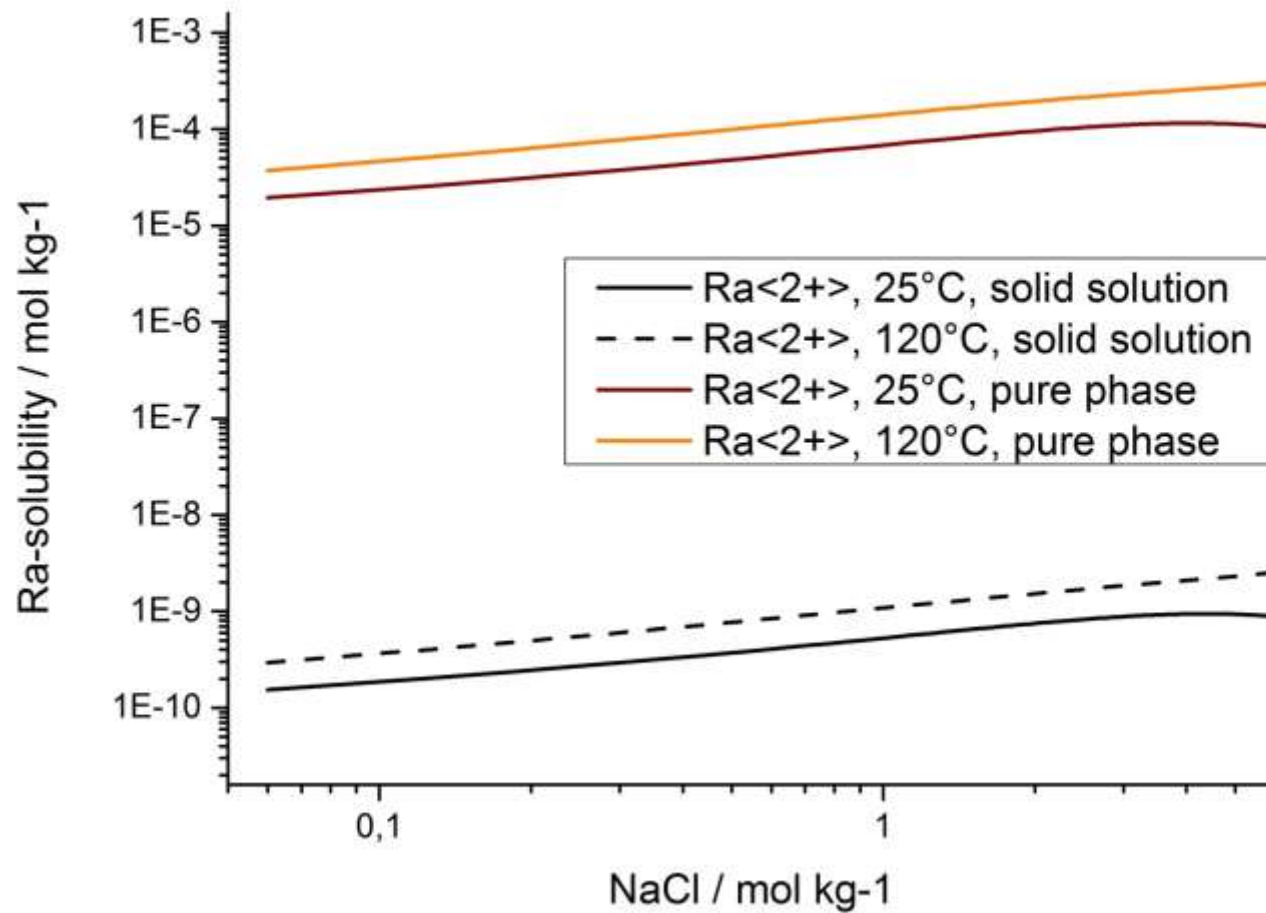
Estimate of the temperature dependence of Pitzer parameters for the binary interaction Ra-Cl

- Adopting the temperature dependence from BaCl₂ (MON1999)
- Complying with the exact 298.15K-values from ROS2011

BaCl ₂								298.15K
Pk-Art	A/T	B	ClnT	DT	ET2	F/T2		
beta0	-1336.53	34.38314	-5.302131	0.0006375	4.6087E-06	0		0.291
beta1	4374.11	-104.2305	15.87517	0.003225	-6.774E-06	0		1.250
cphi	3457.27028	-103.868976	18.156877	-0.03800148	1.3972E-05	-99531.2556		-0.030
RaCl ₂								
beta0	0	0.248	0	0	0	0		
beta1	0	1.477	0	0	0	0		
cphi	0	-0.023	0	0	0	0		
RaCl ₂ neu								
beta0	-1336.53	34.340	-5.302131	0.0006375	4.6087E-06	0		0.248
beta1	4374.11	-104.004	15.87517	0.003225	-6.774E-06	0		1.477
cphi	3457.27028	-103.862	18.156877	-0.03800148	1.3972E-05	-99531.2556		-0.023

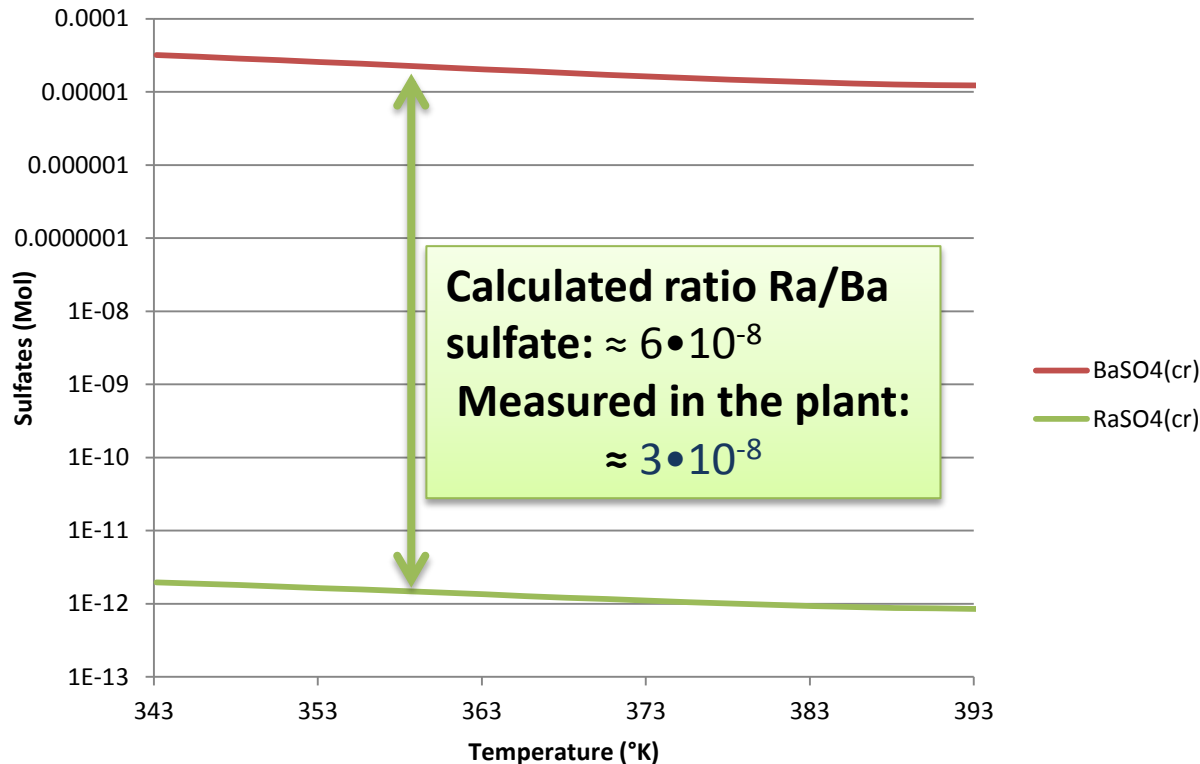
PP Ra-Cl: Yoav O. Rosenberg, Volker Metz, Jiwchar Ganor: Co-precipitation of radium in high ionic strength systems: 1. Thermodynamic properties of the Na–Ra–Cl–SO₄–H₂O system – Estimating Pitzer parameters for RaCl₂. *Geochimica et Cosmochimica Acta* 75 (2011) 5389–5402.

Polythermal solubility of Ba-Ra-SO₄ solid solution and RaSO₄ (pure phase)



Application: geothermal site Soultz-sous-Forêt / France

Radium Sulfate = in ideal solid solution ([Ra] very low) with barite



Composition of the solution:

[Ca] = 6,9 g/l

[Na] = 25,7 g/l

[Cl] = Charge balance

[Ba] = 10 mg/l

[Sr] = 450 mg/l

[SO₄²⁻] = 150 mg/l

[Ra] = 3,5E-12 mol/l

Calculated ratio between Ra-Sulfates and Barite close to the measured value
 Quite promising, but we need more data on partitioning to support our model!

Now for the lead

- Well-founded database for 298.15K available.
- For PbSO_4 and $\text{Pb}(\text{OH})\text{Cl}$ no temperature-dependent solubility
- However, for PbSO_4 standard formation data available
- Speciation of lead relevant

Model for lead in saline solutions

Species

Pb^{2+}
 PbCl^-
 PbCl_2^0
 PbCl_3^-
 PbCl_4^{2-}
 $\text{Pb}(\text{SO}_4)^0$
 $\text{Pb}(\text{SO}_4)_2^{2-}$
 $\text{Pb}(\text{OH})^+$
 $\text{Pb}(\text{OH})_2^0$
 $\text{Pb}(\text{OH})_3^-$
 $\text{Pb}(\text{CO}_3)^0$
 $\text{Pb}(\text{CO}_3)_2^{2-}$

Solid phases

$\text{Pb}(\text{OH})\text{Cl}$ - Laurionit
 $\text{PbSO}_4(\text{cr})$ - Anglesit
 $\text{Pb}(\text{cr})$

Interactions

Pb^{2+}	Cl^-
Pb^{2+}	SO_4^{2-}
PbCl^+	Cl^-
PbCl^+	SO_4^{2-}
PbCl_3^-	Na^+
PbCl_3^-	K^+
PbCl_3^-	Mg^{2+}
PbCl_3^-	Ca^{2+}
PbCl_4^{2-}	Na^+
PbCl_4^{2-}	K^+
PbCl_4^{2-}	Mg^{2+}
PbCl_4^{2-}	Ca^{2+}
$\text{Pb}(\text{SO}_4)_2^{2-}$	Na^+
$\text{Pb}(\text{SO}_4)_2^{2-}$	K^+
$\text{Pb}(\text{SO}_4)_2^{2-}$	Mg^{2+}
PbCl_2^0	K^+
PbCl_2^0	Mg^{2+}
PbCl_2^0	Ca^{2+}
PbCl_2^0	Cl^-
PbCl_2^0	SO_4^{2-}
PbCl_4^{2-}	SO_4^{2-}
PbCl_3^-	SO_4^{2-}
PbCl_4^{2-}	SO_4^{2-}
$\text{Pb}(\text{OH})_3^-$	Na^+
$\text{Pb}(\text{OH})_3^-$	K^+

Thermodynamische Eigenschaften des Bleis
in Lösungen der ozeanischen Salze

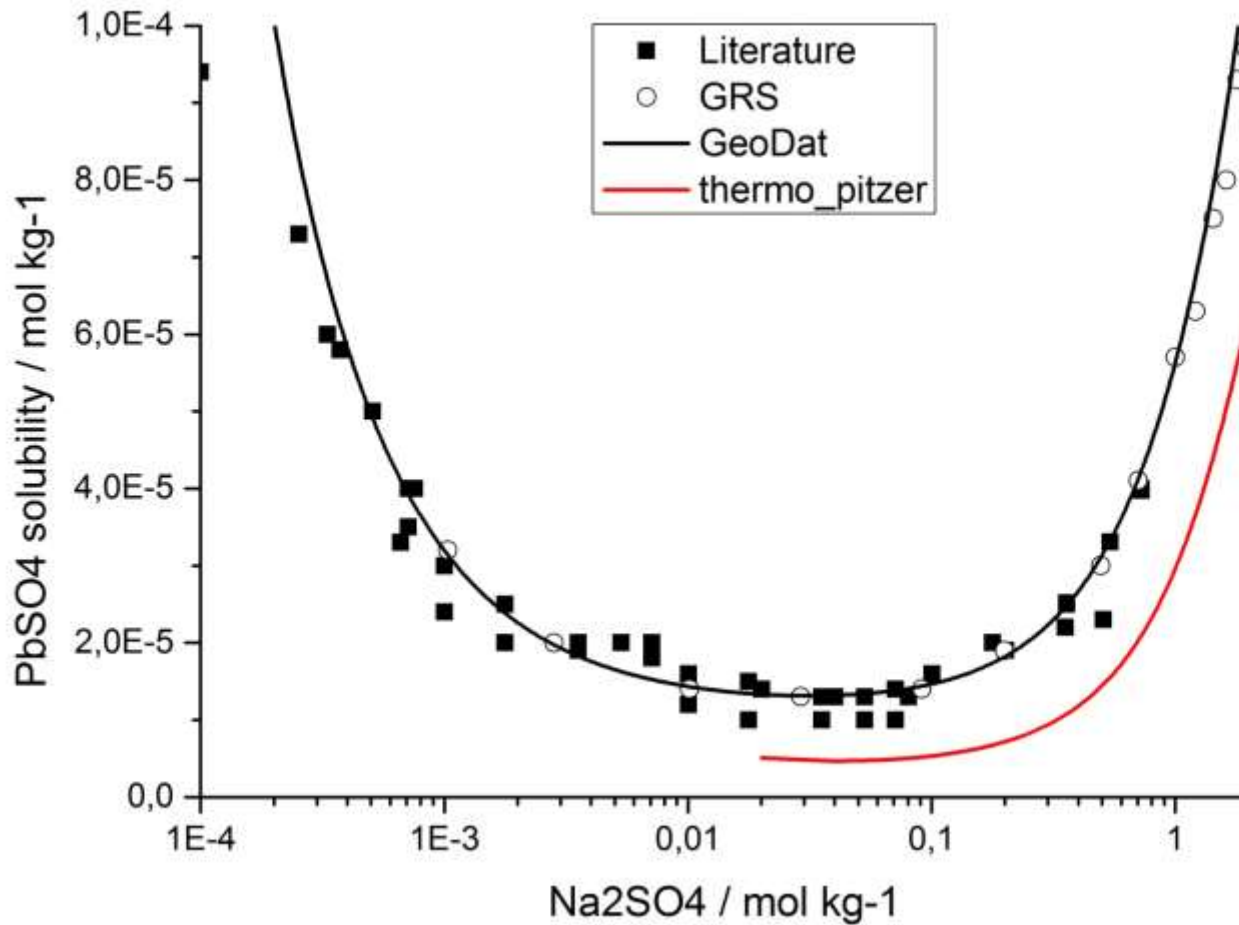
Der Gemeinsamen Naturwissenschaftlichen Fakultät
der Technischen Universität Carolo-Wilhelmina
zu Braunschweig

Zur Erlangung des Grades eines
Doktors der Naturwissenschaften
(Dr. rer. nat.)

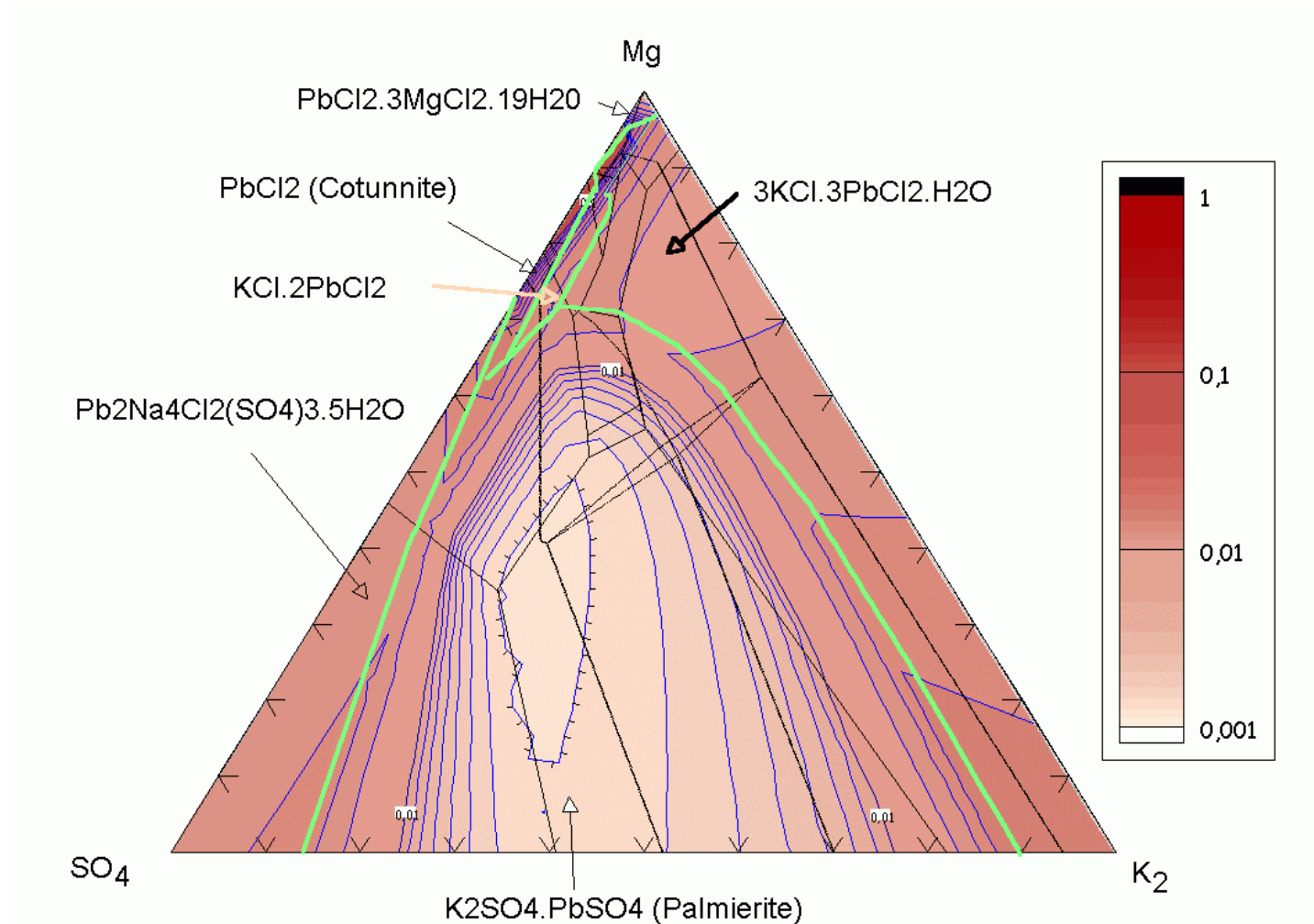
genehmigte
Dissertation

von
Sven Hagemann
aus Harderberg (Osnabrück)

Solubility of $\text{PbSO}_4(\text{cr})$ in Na_2SO_4 -solutions (298.15 K)



Solubility of lead in complex salinar solutions (entire diagram: NaCl-saturation)



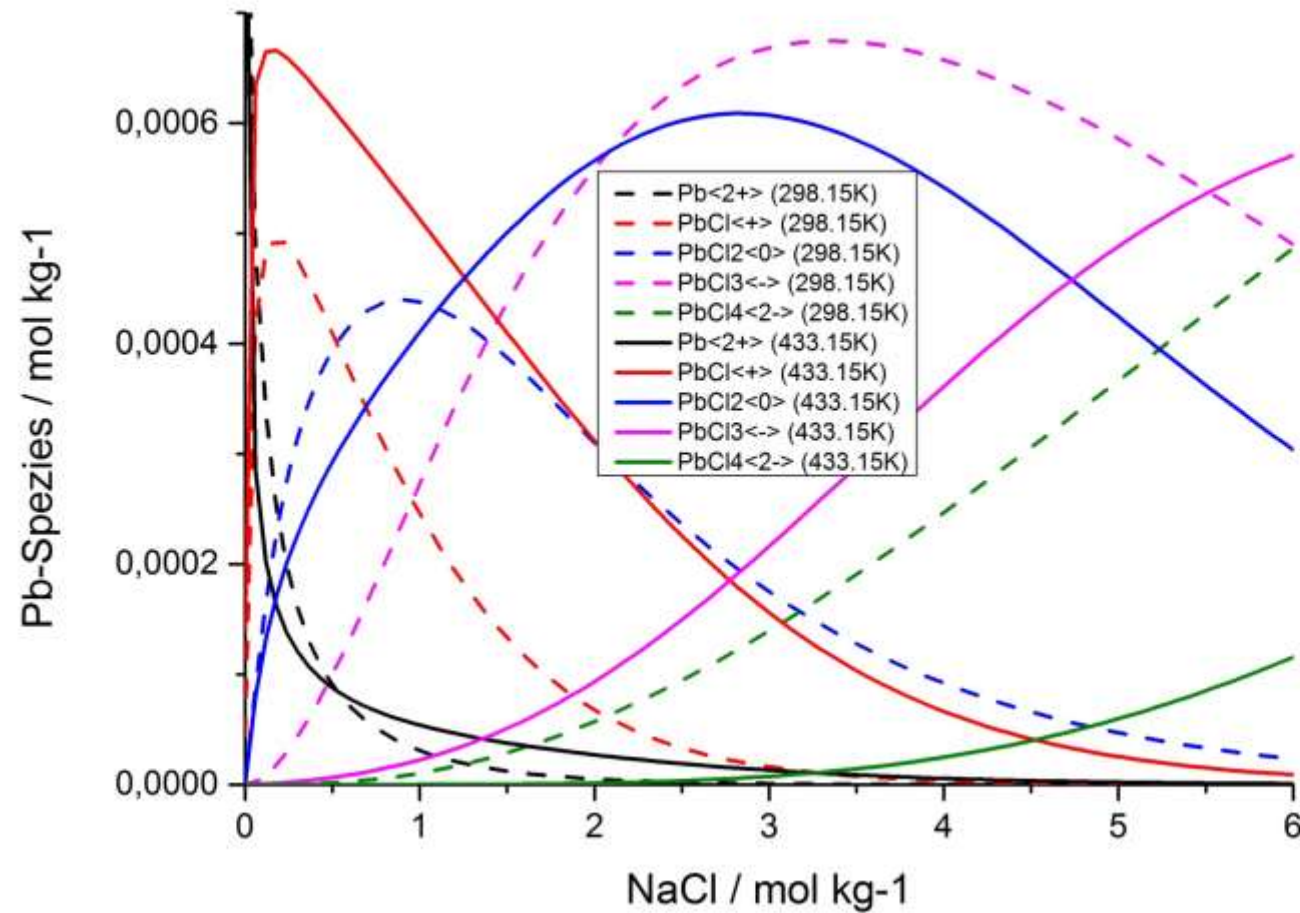
Estimate for the temperature dependence of complex formation constants

Coefficients used in fitting the stability constants of the lead chloride species with polynomial equations in temperature

Formation reaction	a	b	c	d
$\text{Pb}^{2+} + \text{Cl}^- = \text{PbCl}^+$	6.710	$-6.255 \cdot 10^{-2}$	$2.186 \cdot 10^{-4}$	$-2.266 \cdot 10^{-7}$
$\text{PbCl}^+ + \text{Cl}^- = \text{PbCl}_2$	4.316	$-5.977 \cdot 10^{-4}$	$2.570 \cdot 10^{-4}$	$-3.184 \cdot 10^{-7}$
$\text{PbCl}_2 + \text{Cl}^- = \text{PbCl}_3^-$	4.154	$-1.580 \cdot 10^{-2}$	$0.1051 \cdot 10^{-4}$	—
$\text{PbCl}_3^- + \text{Cl}^- = \text{PbCl}_4^{2-}$	6.111	$-2.674 \cdot 10^{-2}$	$0.2350 \cdot 10^{-4}$	—

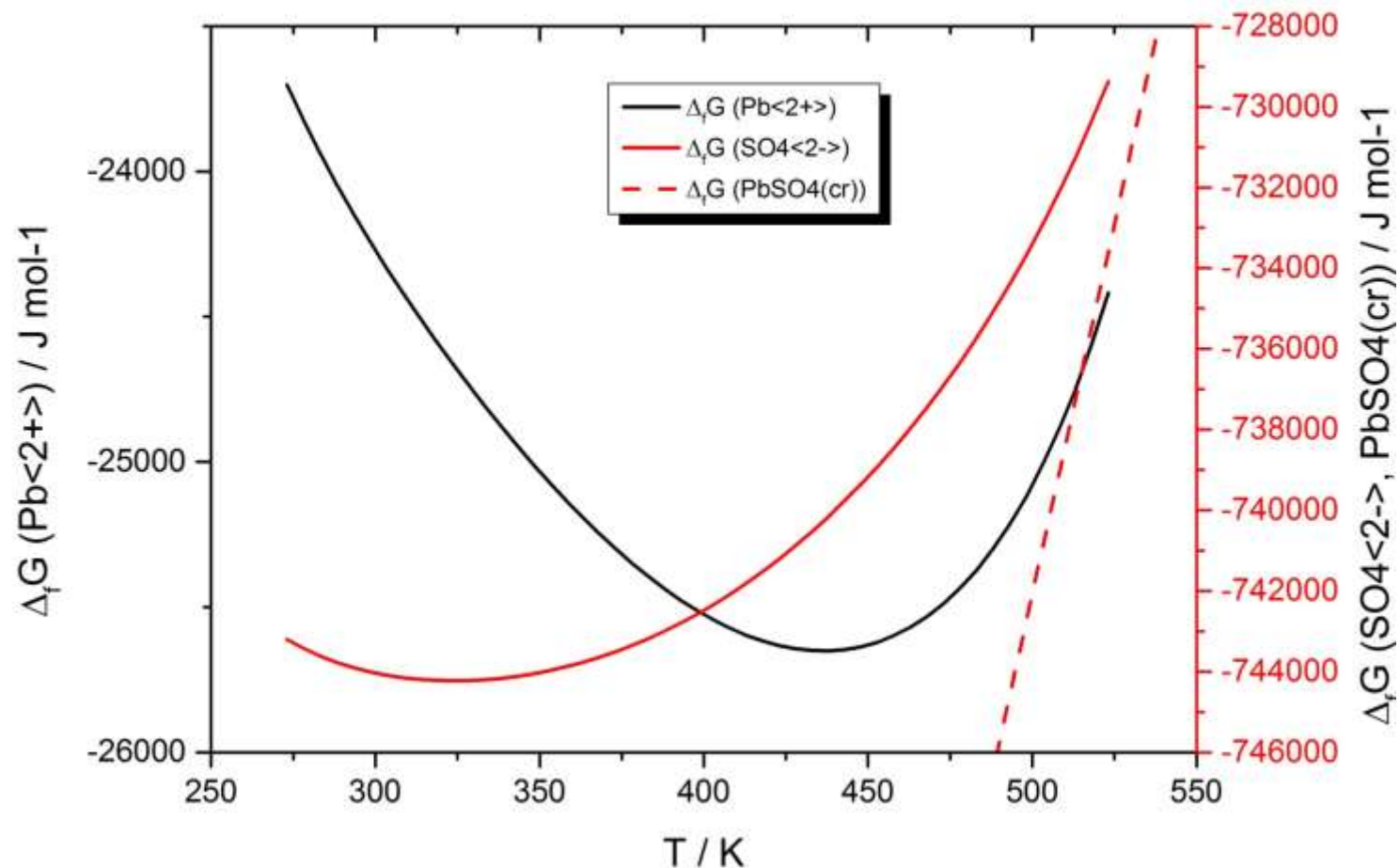
Quelle: J. O. Nriagu, G. M. Anderson: Stability of the lead (II) chloride complexes at elevated temperatures. Chemical Geology 7 (1971) 171-183.

Example: Speciation of lead in NaCl-solutions – 298.15 and 433.15 K

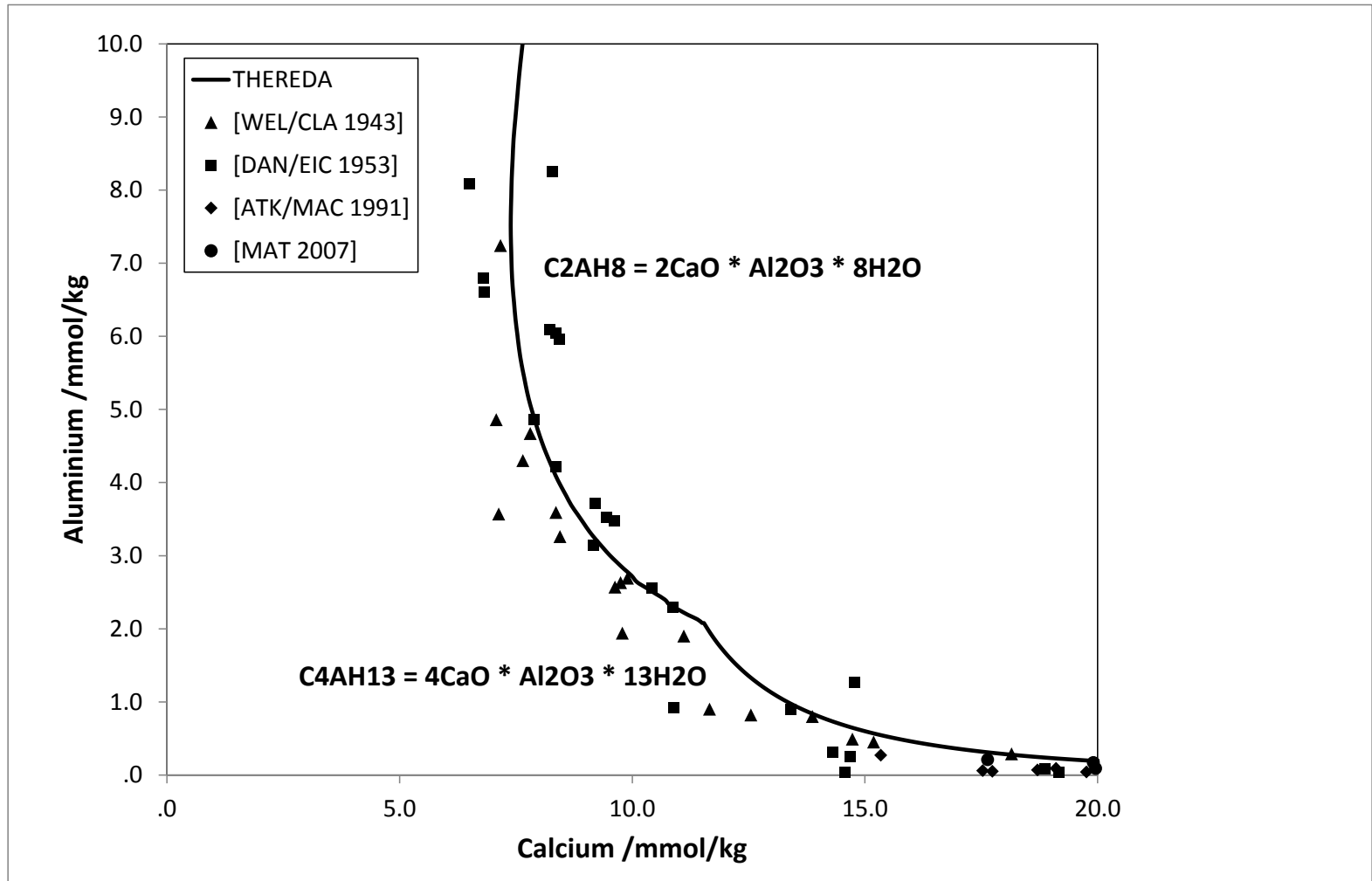


Estimate of solubility of Anglesite (PbSO₄) at elevated temperatures

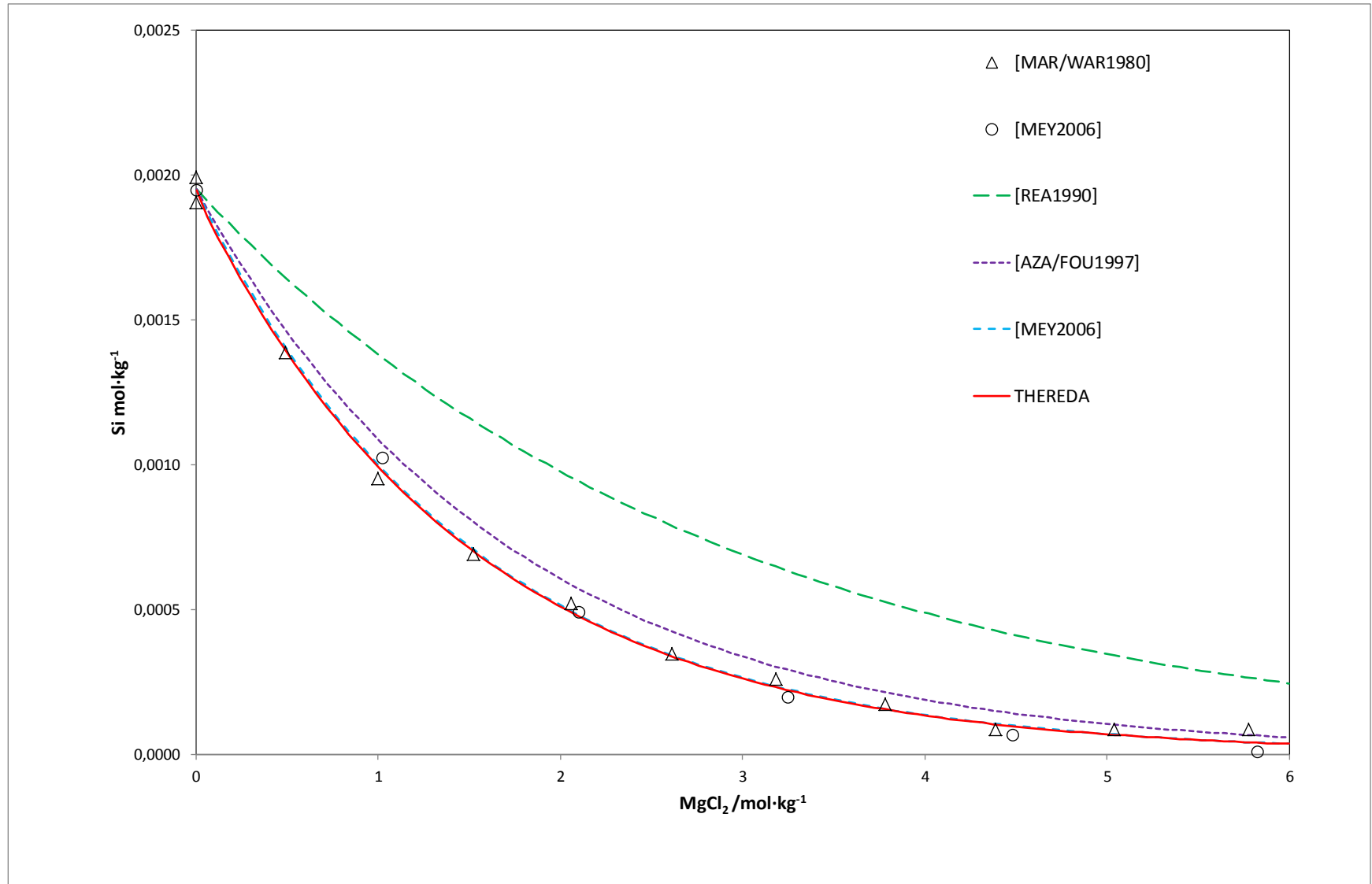
- Foundation: $\Delta_f H$, S^0 und $C_p(T)$
- Calculation of $\Delta_f G(T)$
- Optimization of $\Delta_f G(T = 298.15 \text{ K})$ for well-known solubilities (ca. + 3kJ/mol)



Solubility of C2AH8 and C4AH13 in low-saline solution



Solubility of $\text{SiO}_2(\text{am})$ in MgCl_2 -solution



Conclusion (I)

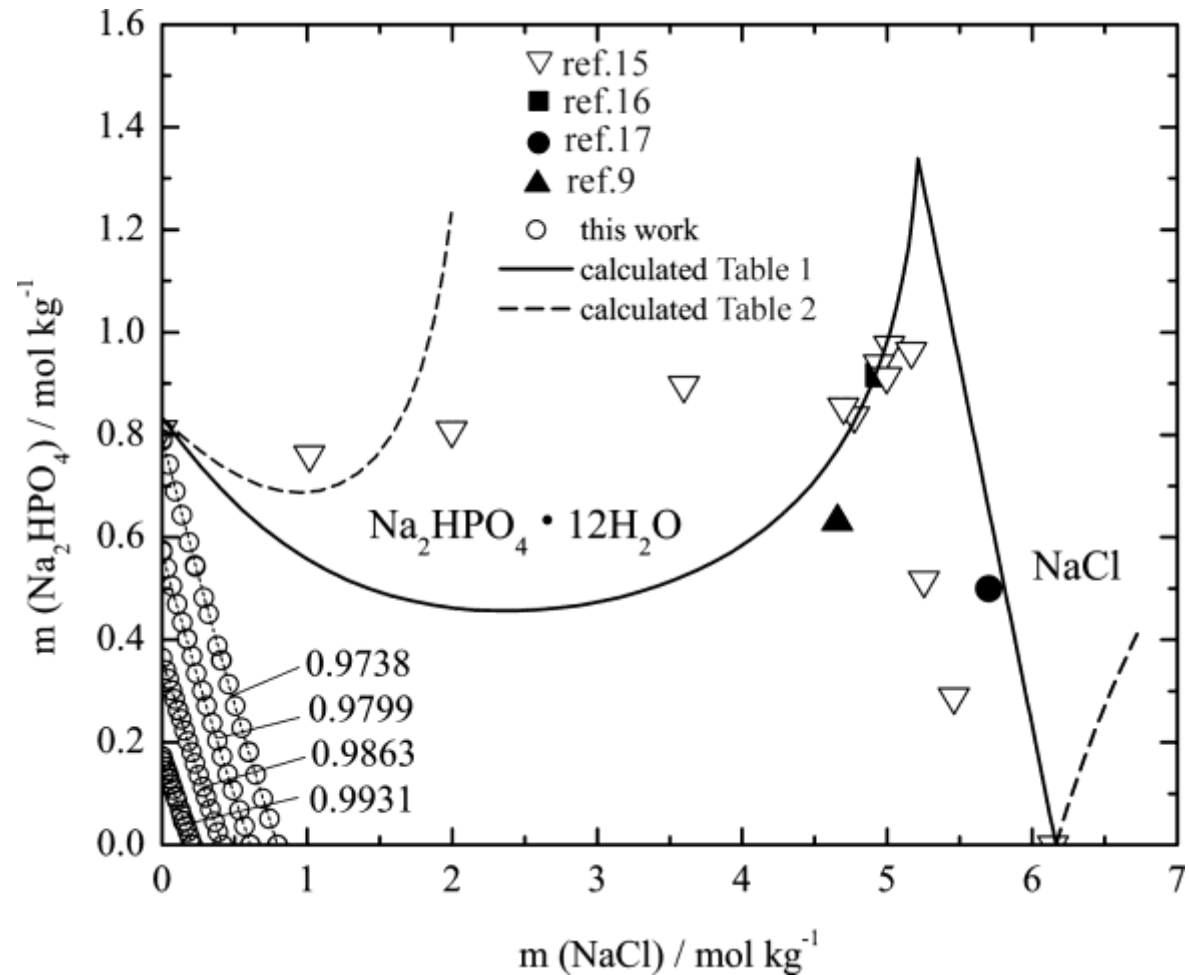
- **Cs, Rb:** complete set of data for 298.15K
- **Ba, Sr:** almost complete, but allowing for the calculation of solubilities of relevant solid phases
 - Closer look at solid solutions necessary
 - Data still need to be tested for more systems
- **Ra:** very few data for solubility, however, solid solution formation with EA-sulfates more important
 - We look for more data with regard to partitioning between solid solution and aqueous solution!
- **Phosphate:** for Na, K – HPO_4^{2-} , H_2PO_4^- - Cl, SO_4 complete
 - At present: investigation of low-soluble EA-phosphates
- **Cement-phases:**
 - Next release for 298.15 K only and mainly covering low-saline conditions
 - One example for equilibria in concentrated MgCl_2 -solution will be given
 - Overall solubility not much influenced by high salinity

Conclusion (II)

- **Pb:** good database for 298.15 K, approximations for elevated temperatures for chloride solutions
 - Applicability to higher pH values still under investigation
 - At present: investigation of data for sulfate-complexation at elevated temperatures and high-temperature solubility of Anglesite
 - No data at higher temperature for $\text{Pb}(\text{OH})\text{Cl}$
 - Application of alternative complexation model (Woosley and Millero, 2013) ?
- At present database for the **system of oceanic salts** for temperatures up to 200°C is updated in THEREDA . Then, some of the systems presented here will be recalculated and, if necessity arises, adjusted.
- Implementation in THEREDA by the end of 2013.

Thank you very much for your attention!

Na₂HPO₄-NaCl, ternary system, solubility and isoactivity lines



Source:

T. Schrage, A.G. Muñoz and H.C. Moog: Thermodynamic Modeling of High Salinary Phosphate Solutions II. Ternary and higher Systems. J. Chem. Thermodynamics (in preparation).

Erweiterung für höhere Temperaturen des Modells für Blei in hochsalinaren Lösungen (II)

