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Thermodynamic optimisation of the system



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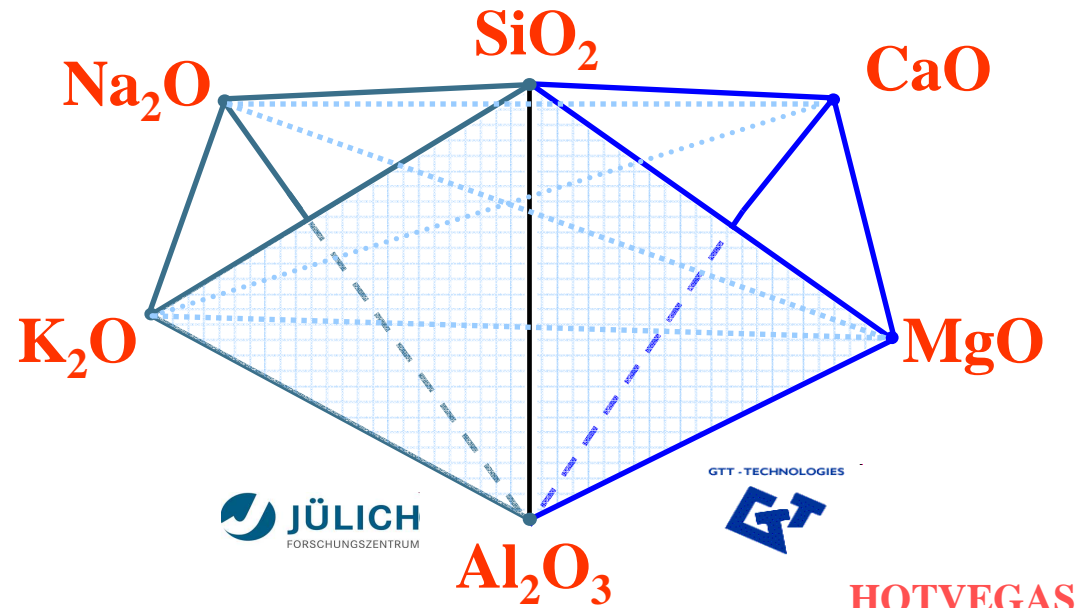
- Motivation and aim of the work
- Models and optimisation procedure
- Results of re-assessment for binary systems
- Assessment for ternary systems
- Conclusions and outlook

Motivation and aims

Thermodynamic calculation/prediction for slag relevant oxide systems, which are difficult from the point of view of experimental measurements

Calculation requires:

- Reliable database, based on the experimental data
- Software



Available databases are not sufficient to model the complete coal ash (slag) system

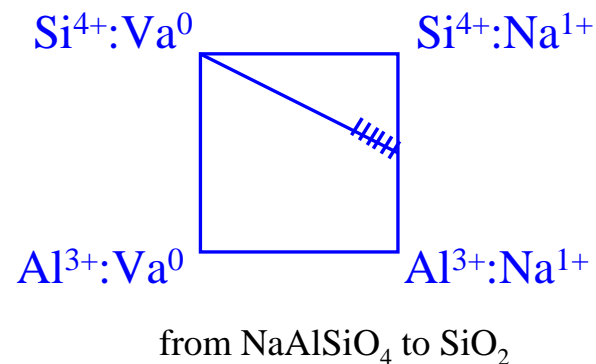
Purpose of our work - development of a new data base, which is:

- ✓ applicable for the slag relevant system containing alumina, silica, alkali, alkali-earth oxides
- ✓ suitable for the calculations and/or predictions of the phase equilibria and other thermodynamic properties by variation of temperature and composition

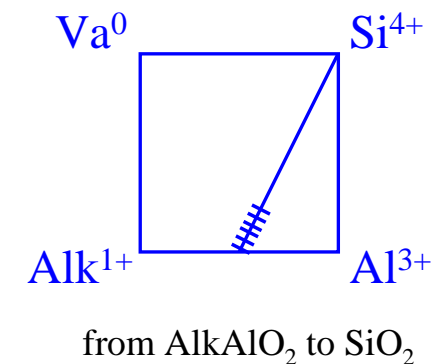
Modelling of liquid and solid solutions

Applied and *chosen* model for the phases under consideration

Phase name	Associate species model	Multi-sublattice model
Liquid	Liquid pure oxides, binary and ternary liquid species	-
Mullite	$\text{Al}_6\text{Si}_2\text{O}_{13}$: $\text{Al}_6\text{Si}_2\text{O}_{13} \cdot 1/4$, Al_2O_3 , $\text{SiO}_2 \cdot 2$	$(\text{Al}^{3+})_1(\text{Al}^{3+})_1(\text{Al}^{3+}, \text{Si}^{4+})_1(\text{O}^{2-}, \text{Va})_5$ (Mao et al., 2005)
Natrium disilicate	$(\text{Na}_{1-x}\text{K}_x)_2\text{Si}_2\text{O}_5$: $\text{Na}_2\text{Si}_2\text{O}_5$, $\text{K}_2\text{Si}_2\text{O}_5$	-
Potassium aluminate	$(\text{KAl})_{1-x}\text{Si}_x\text{O}_2$: KAlO_2 , KAlSiO_4	KAlO_2 - low T, high T 3 sublattices: $(\text{Al}^{3+}, \text{Si}^{4+})_1(\text{K}^{1+}, \text{Va}^0)_1(\text{O}^{2-})_2$
Nepheline, carnegieite	NaAlSiO_4 : NaAlSiO_4 , $\text{NaAlSi}_2\text{O}_6$	Nepheline (low T), carnegieite (high T) 4 sublattices: $(\text{Al}^{3+}, \text{Si}^{4+})_2\text{Va}^0_1(\text{Na}^{1+}, \text{Va}^0)_1(\text{O}^{2-})_4$
Natrium aluminate	$(\text{NaAl})_{1-x}\text{Si}_x\text{O}_2$: NaAlO_2 , NaAlSiO_4	NaAlO_2 - low T, high T 3 sublattices: $(\text{Al}^{3+}, \text{Si}^{4+})_1(\text{Na}^{1+}, \text{Va}^0)_1(\text{O}^{2-})_2$



Composition scheme



Modelling of liquid – Associate species approach

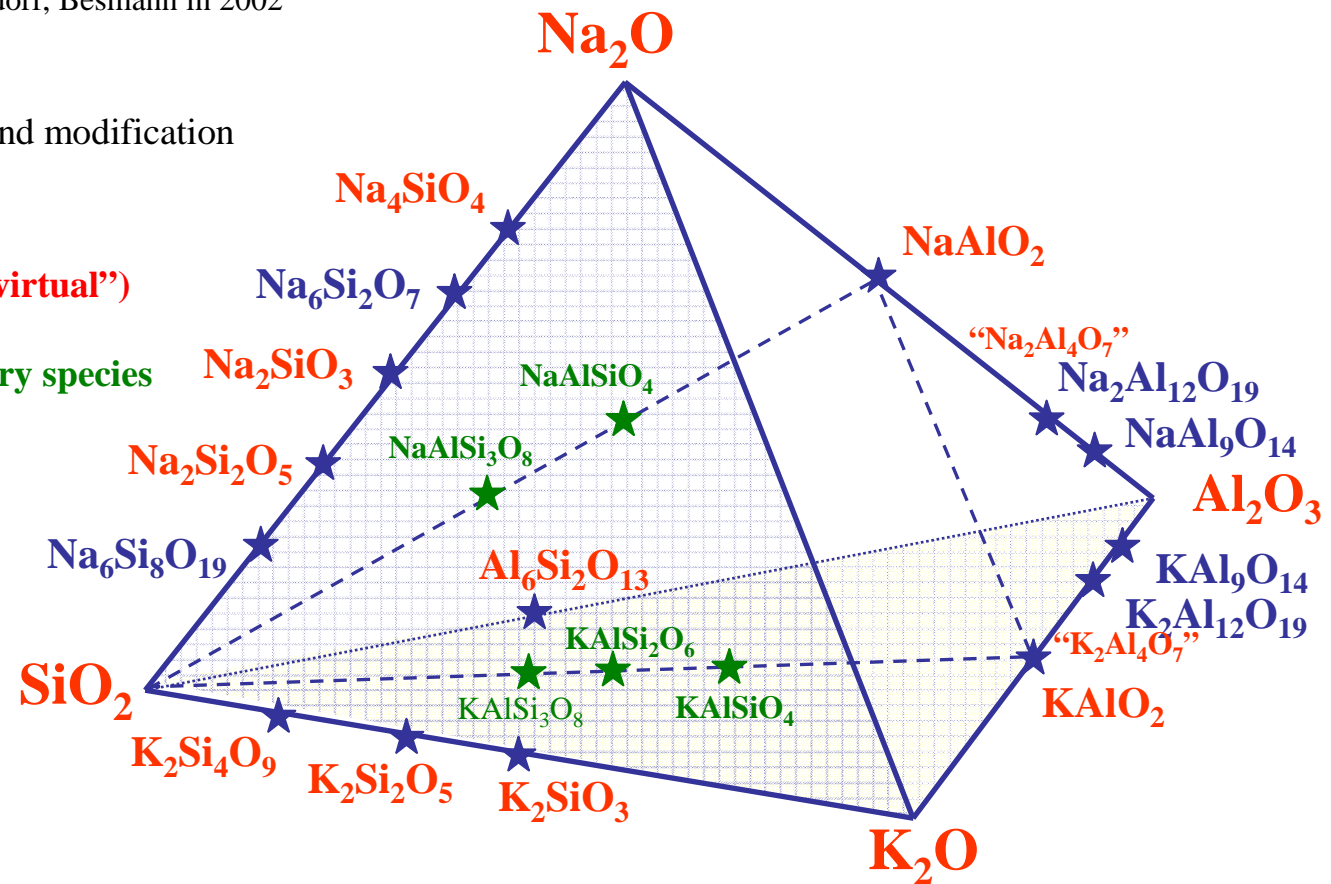
introduced for slag by Spear, Allendorf, Besmann in 2002

- suitable for this system
- relatively simple for using and modification

- ✓ pure liquid oxide
- ✓ binary liquid species (incl. “virtual”)
- ✓ binary compounds (rest)
- ✓ ternary compounds and ternary species

+

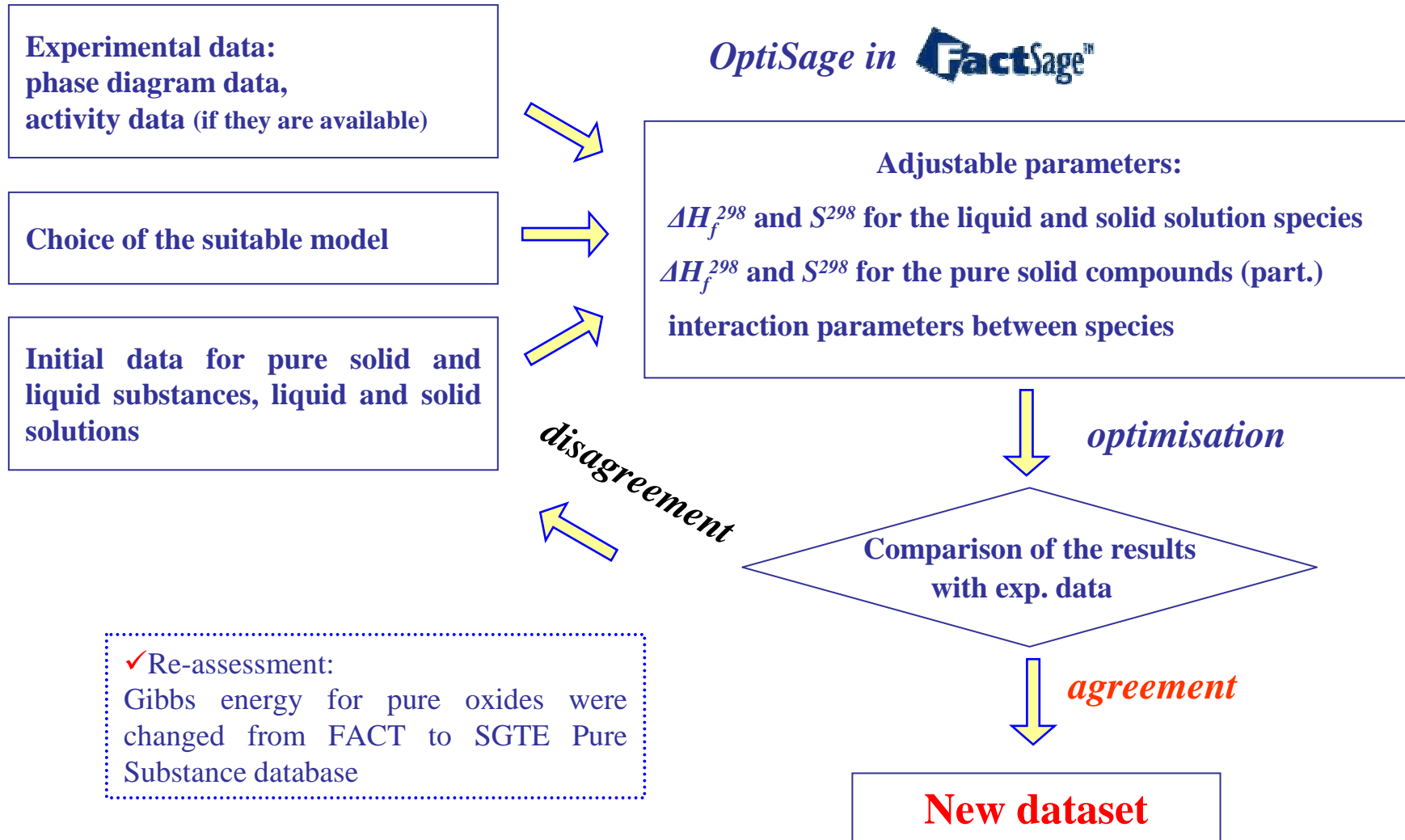
*Interaction between
solution components*



$$G_m = \sum x_i G_i^0 + RT \sum x_i \ln x_i + \sum_{i < j} \sum_{v} x_i x_j L_{ij}^{(v)} (x_i - x_j)^v$$

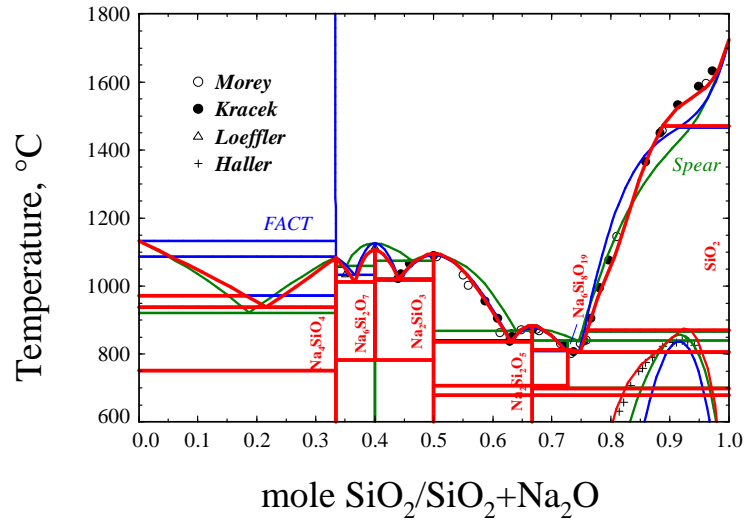
$$L_{ij}^{(v)} = A_{ij}^{(v)} + B_{ij}^{(v)} \cdot T + C_{ij}^{(v)} \cdot T \cdot \ln T + D_{ij}^{(v)} \cdot T^2 + \dots, v = 0, 1$$

Database development

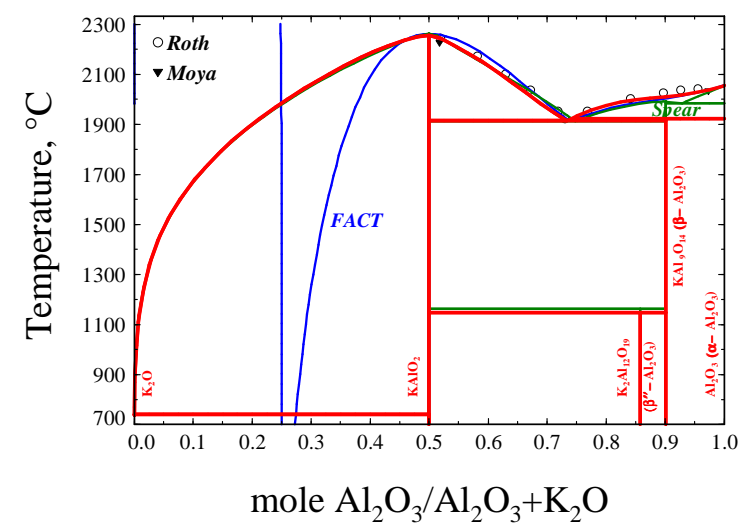
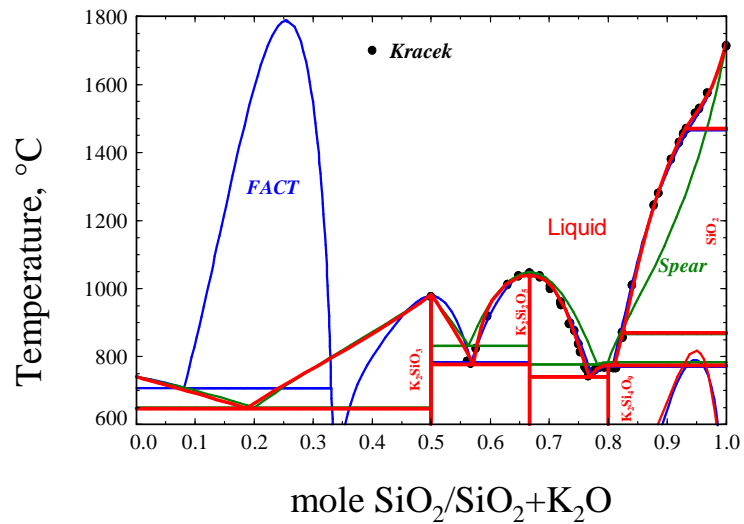
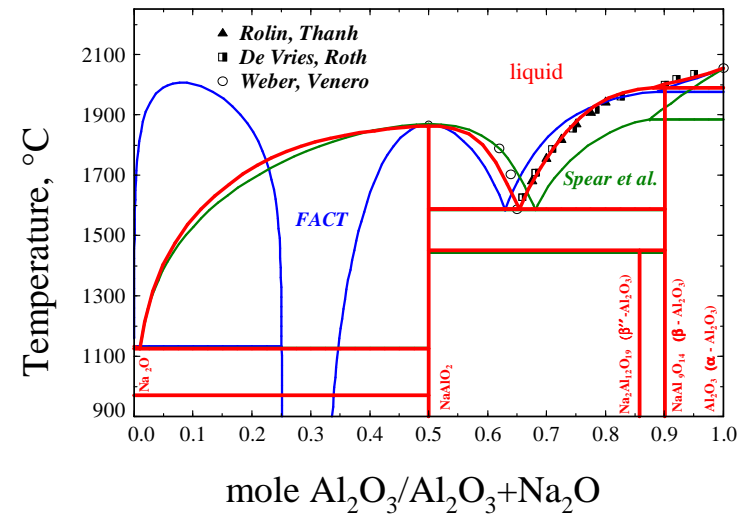


Results of re-assessment for binary systems-1

Alk₂O-SiO₂, Alk=Na, K

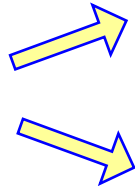


Alk₂O-Al₂O₃, Alk=Na, K

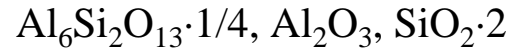


Results of re-assessment for binary systems-2

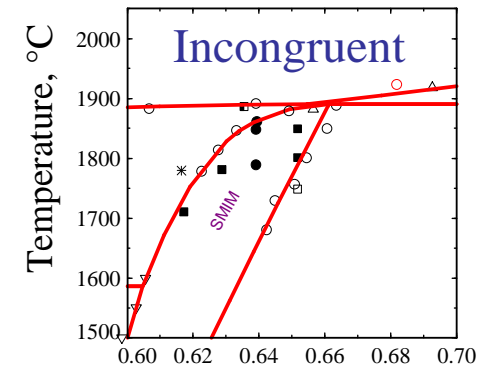
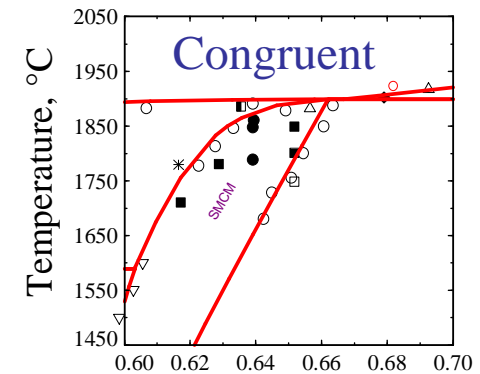
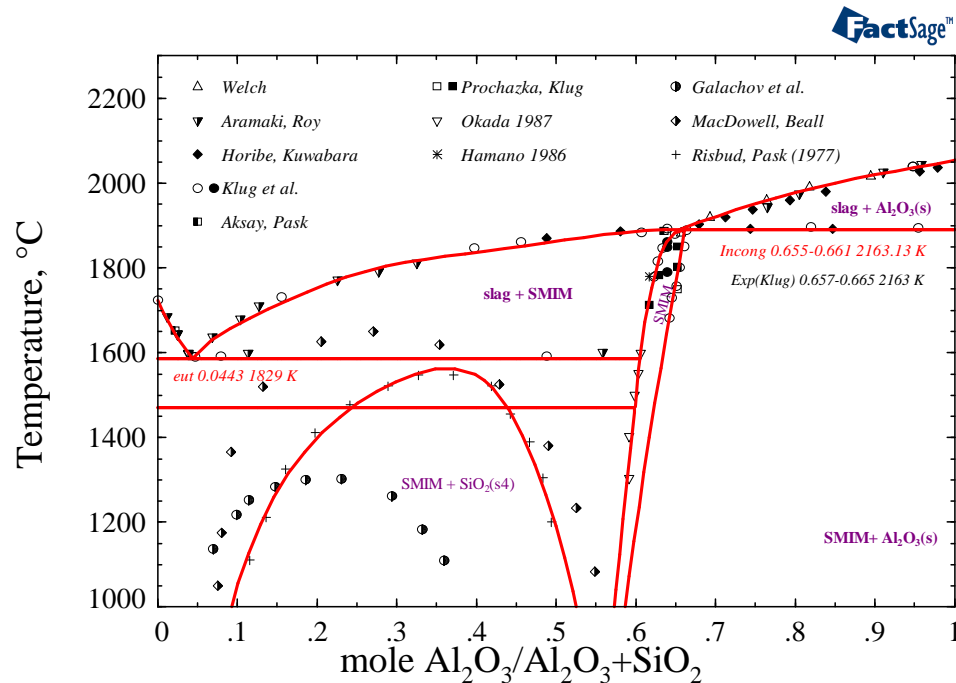
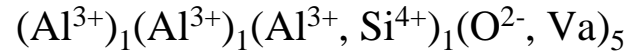
Mullite



Associate species model (introduced by Spear et al. in 2002):



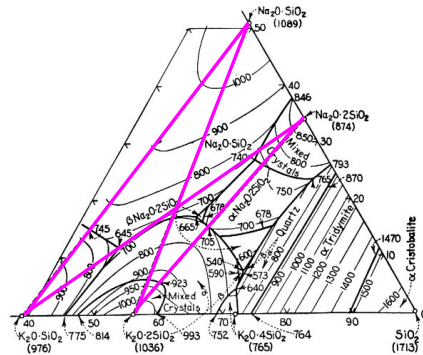
4 sublattice model (introduced by Mao et al. in 2005):



✓ Model parameters are optimised for both melting behaviour of mullite

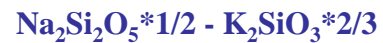
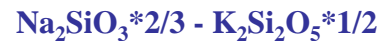
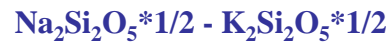
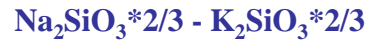
Re-assessment for ternary system $\text{Na}_2\text{O}-\text{K}_2\text{O}-\text{SiO}_2$

Comparison of the calculated isotherms with the experimental points

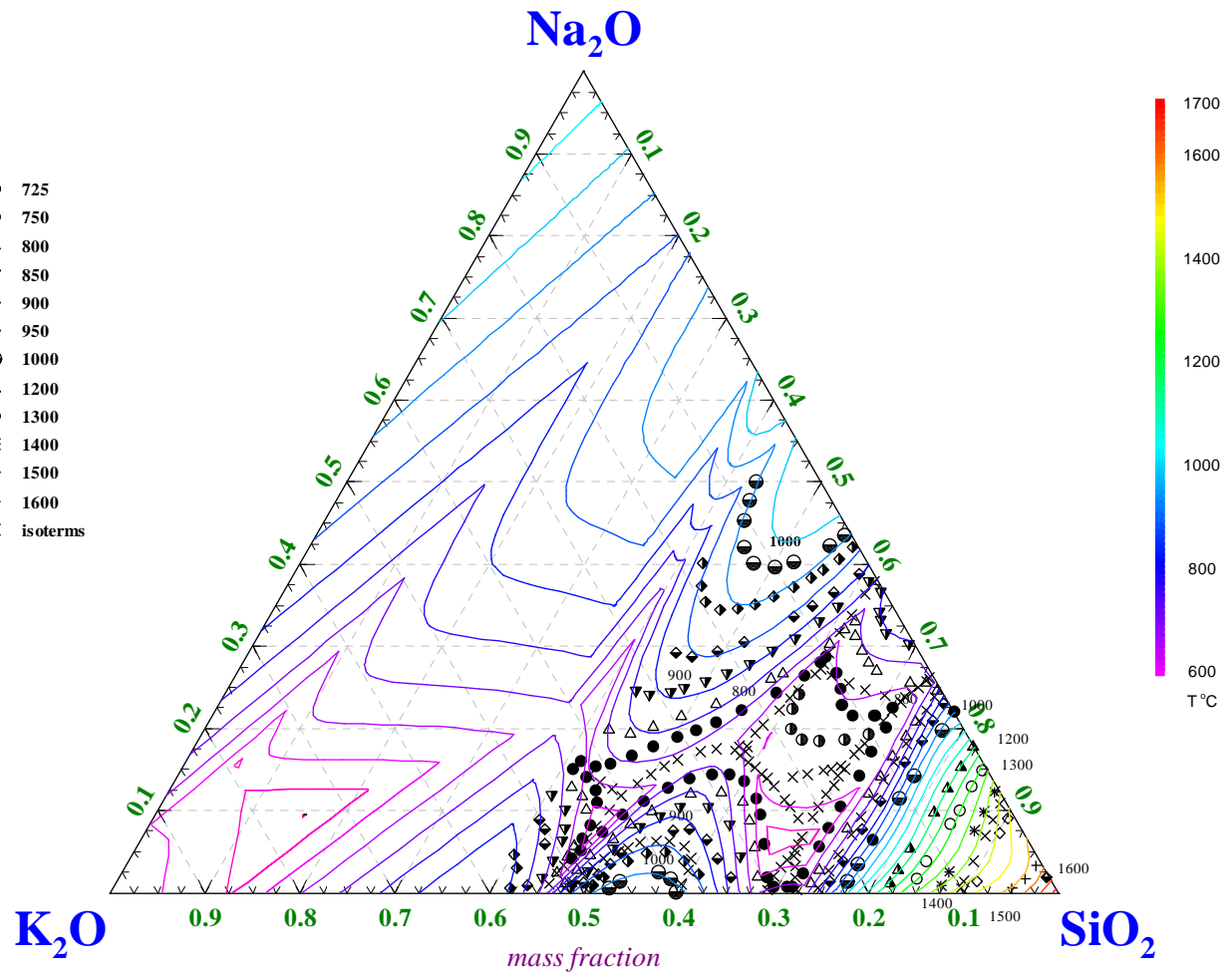


F.C. Kracek,
The ternary system $\text{K}_2\text{SiO}_3-\text{Na}_2\text{SiO}_3-\text{SiO}_2$,
J. Phys. Chem., **36** [10], (1932), 2529-2542

Interacting components:

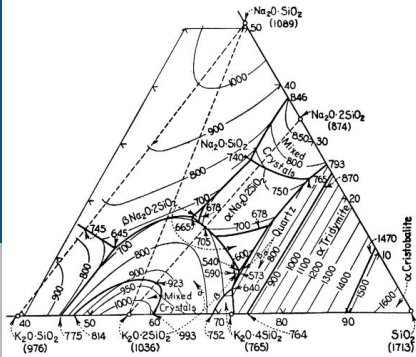


- 725
- 750
- △ 800
- ▽ 850
- ◆ 900
- ◇ 950
- ⊙ 1000
- ▲ 1200
- 1300
- * 1400
- ◇ 1500
- + 1600
- × isotherms



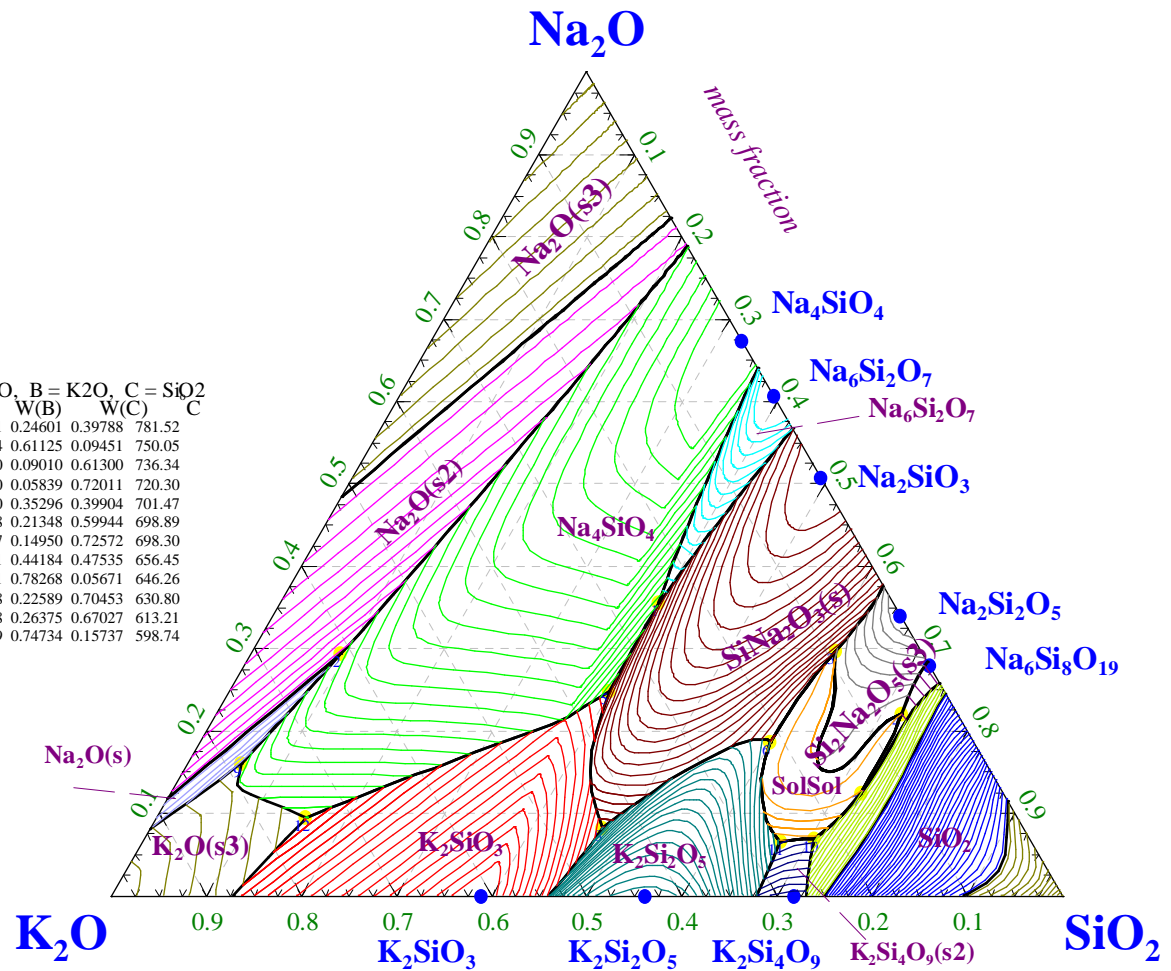
Re-assessment for ternary system $\text{Na}_2\text{O}-\text{K}_2\text{O}-\text{SiO}_2$

Predicted phase fields and ternary points

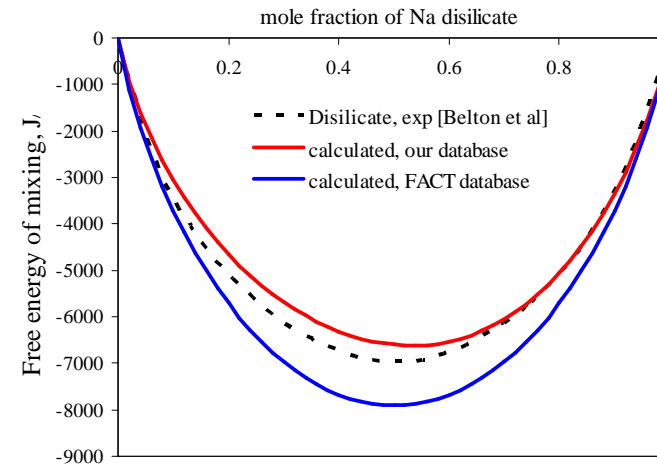
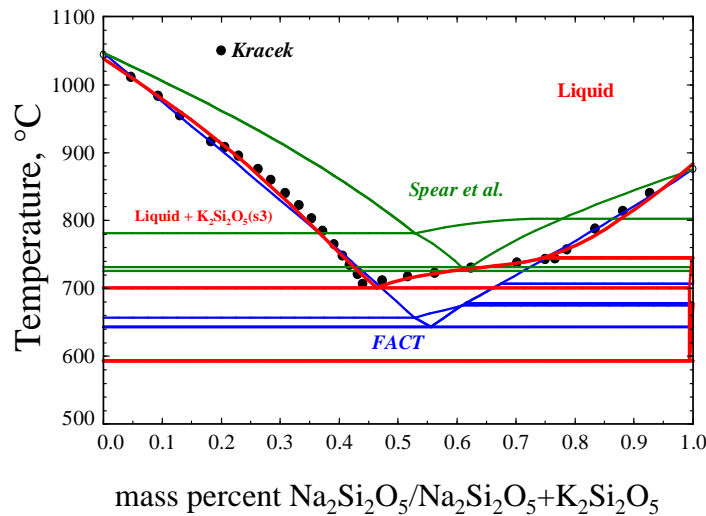
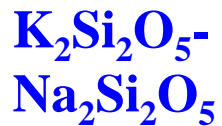
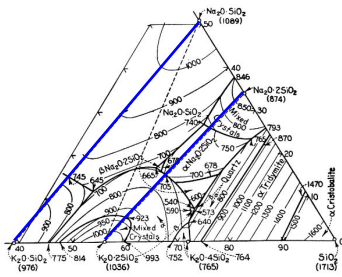
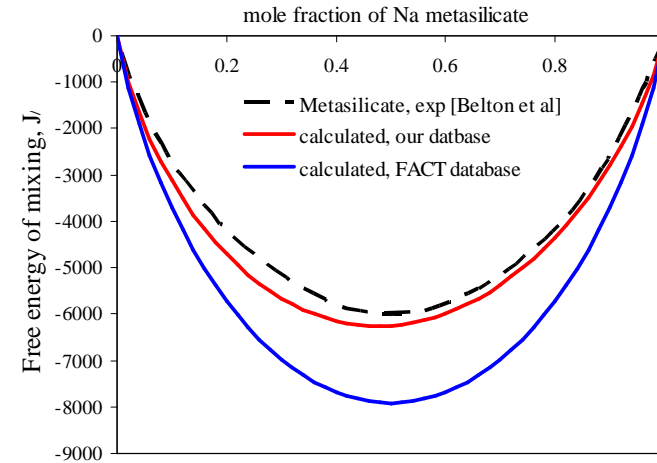
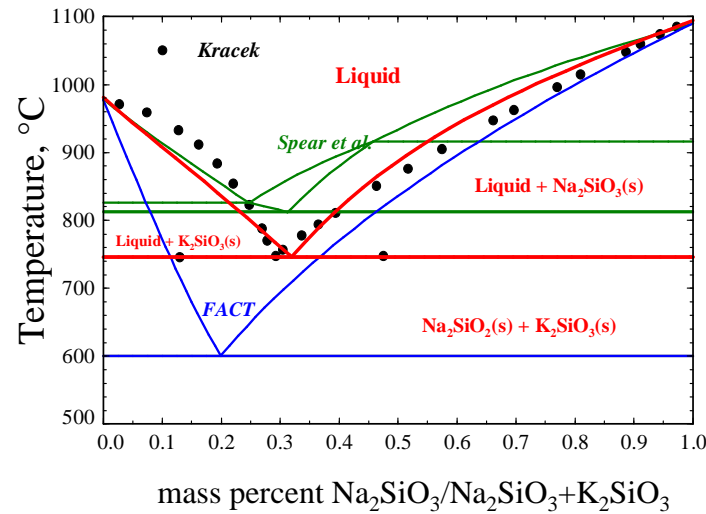
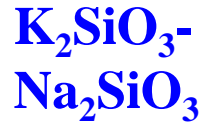


A = Na₂O, B = K₂O, C = SiO₂

	W(A)	W(B)	W(C)	C
1:	0.35611	0.24601	0.39788	781.52
2:	0.29424	0.61125	0.09451	750.05
3:	0.29690	0.09010	0.61300	736.34
4:	0.22150	0.05839	0.72011	720.30
5:	0.24800	0.35296	0.39904	701.47
6:	0.18708	0.21348	0.59944	698.89
7:	0.12477	0.14950	0.72572	698.30
8:	0.08281	0.44184	0.47535	656.45
9:	0.16061	0.78268	0.05671	646.26
10:	0.06958	0.22589	0.70453	630.80
11:	0.06598	0.26375	0.67027	613.21
12:	0.09529	0.74734	0.15737	598.74



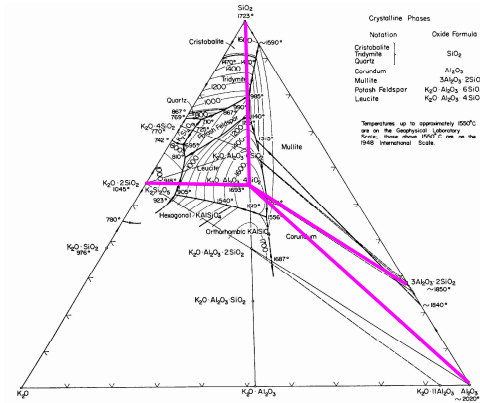
Quasi binary section in the $\text{Na}_2\text{O}-\text{K}_2\text{O}-\text{SiO}_2$ system



[Belton et al.] G.R. Belton, U.V. Choudary, D.R. Gaskell, Thermodynamics of mixing in molten sodium-potassium silicates, Phys. Chem.Process. Metall., Richardson Conf., (1974), 247-253

Assessment for ternary system $K_2O-Al_2O_3-SiO_2$

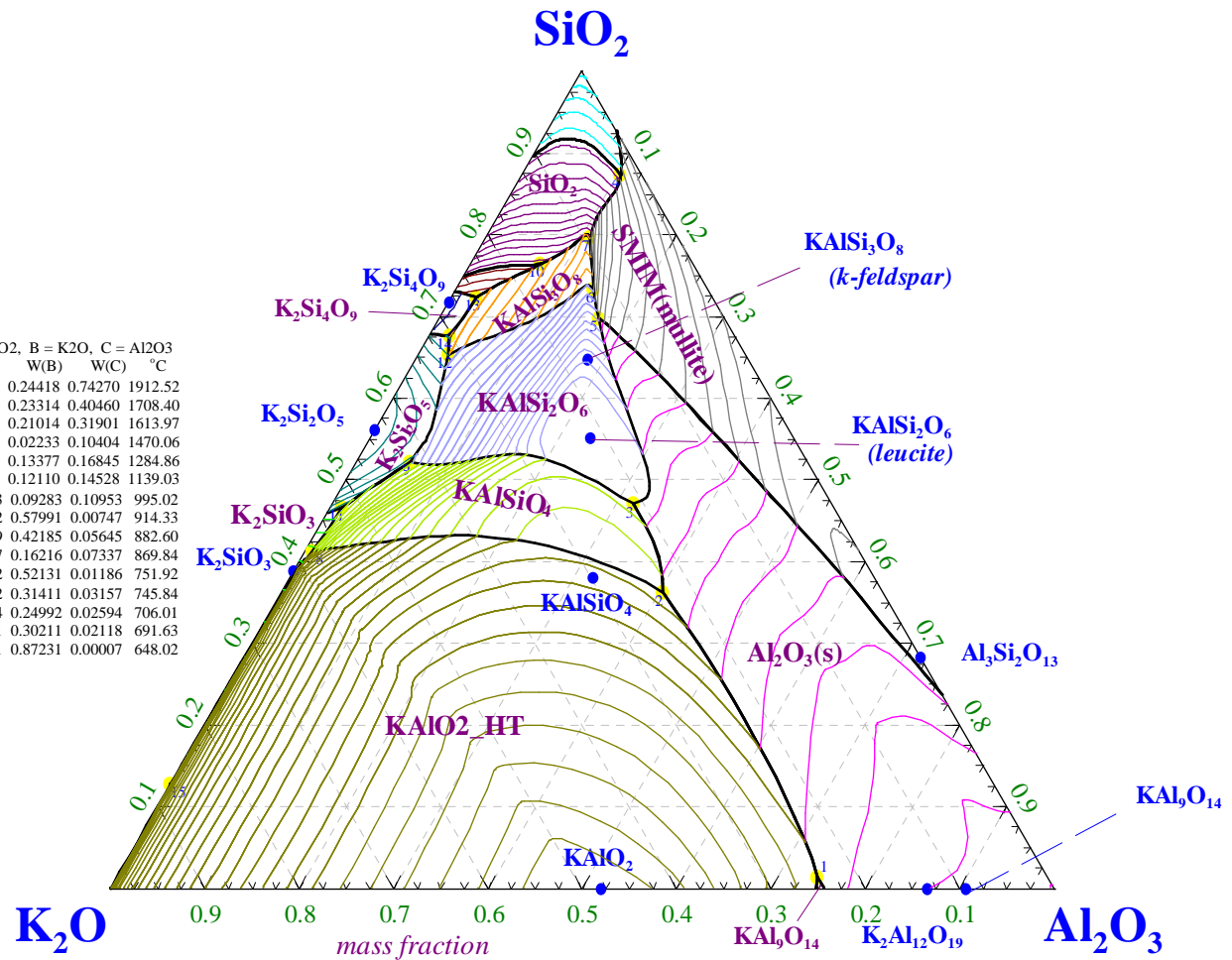
Predicted phase fields and ternary points



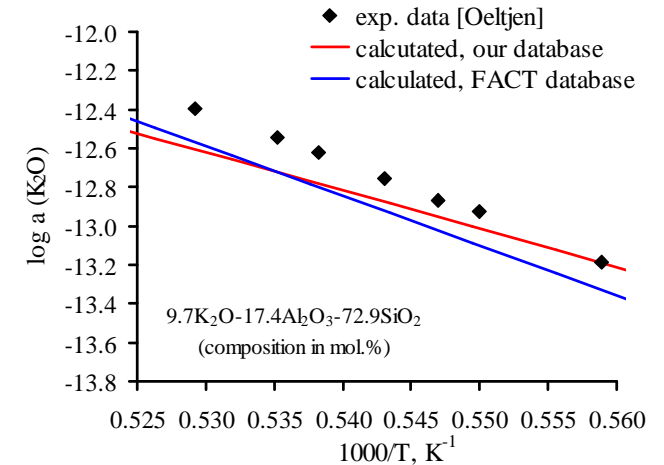
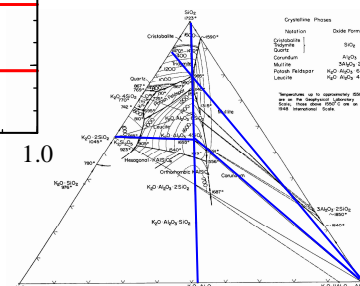
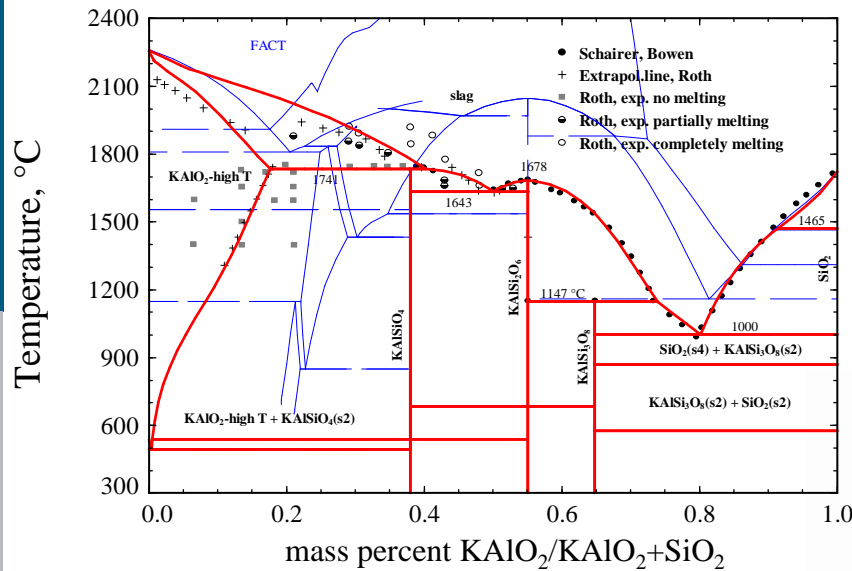
J.F. Schairer, N.L. Bowen, *The system $K_2O-Al_2O_3-SiO_2$* , *Am. J. Sci.* **253** (1955) 681-746.

	A = SiO ₂	B = K ₂ O	C = Al ₂ O ₃
	W(A)	W(B)	W(C) °C
1:	0.01311	0.24418	0.74270 1912.52
2:	0.36226	0.23314	0.40460 1708.40
3:	0.47085	0.21014	0.31901 1613.97
4:	0.87363	0.02233	0.10404 1470.06
5:	0.69778	0.13377	0.16845 1284.86
6:	0.73362	0.12110	0.14528 1139.03
7:	0.79763	0.09283	0.10953 995.02
8:	0.41262	0.57991	0.00747 914.33
9:	0.52169	0.42185	0.05645 882.60
10:	0.76447	0.16216	0.07337 869.84
11:	0.46682	0.52131	0.01186 751.92
12:	0.65432	0.31411	0.03157 745.84
13:	0.72414	0.24992	0.02594 706.01
14:	0.67671	0.30211	0.02118 691.63
15:	0.12761	0.87231	0.00007 648.02

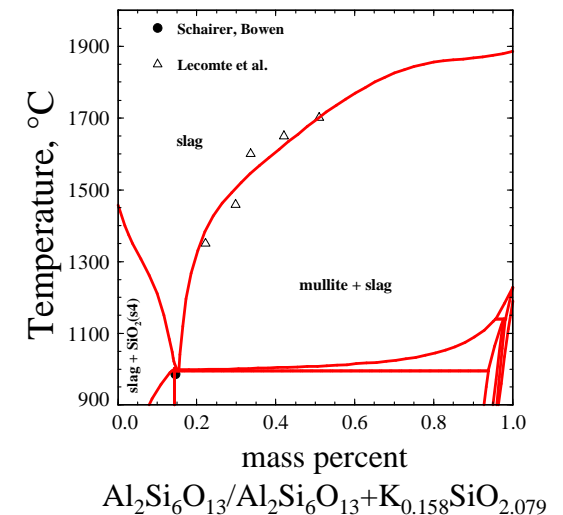
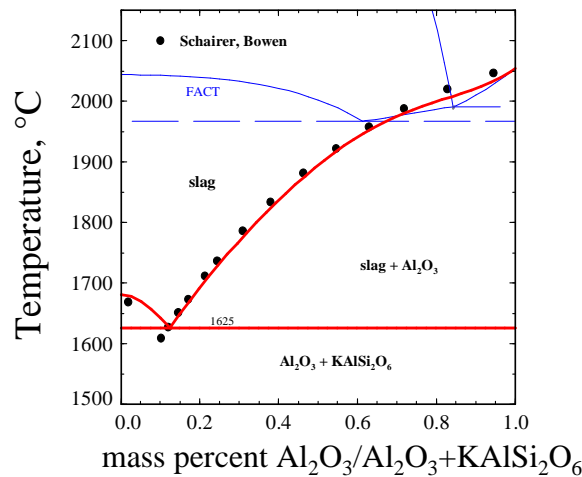
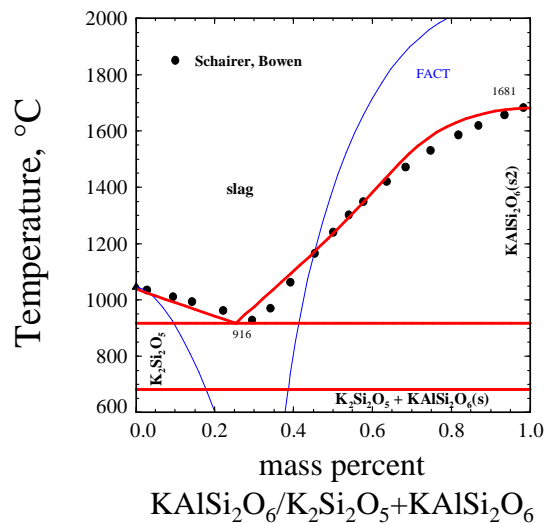
Interacting components



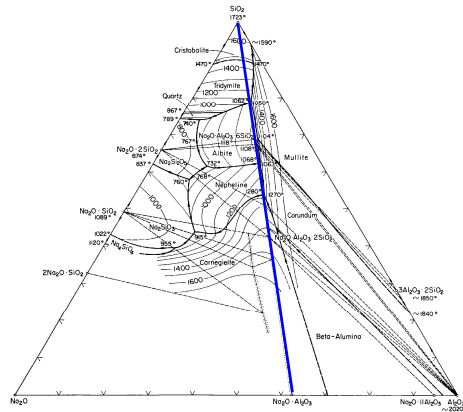
Quasi binary sections in the $K_2O-Al_2O_3-SiO_2$ system



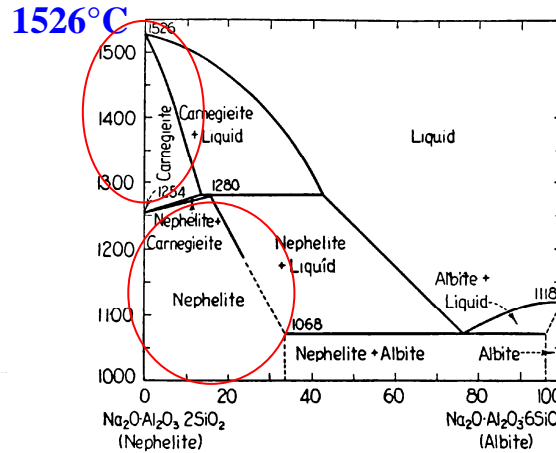
[Oeltjen] L. Oeltjen, *Diss. RWTH Aachen, 1999*
 [Lecomte et al.] G. Lecomte, B. Pateyron, P. Blanchart, *Mater. Res. Bull.* **39** (2004) 1469-1478.



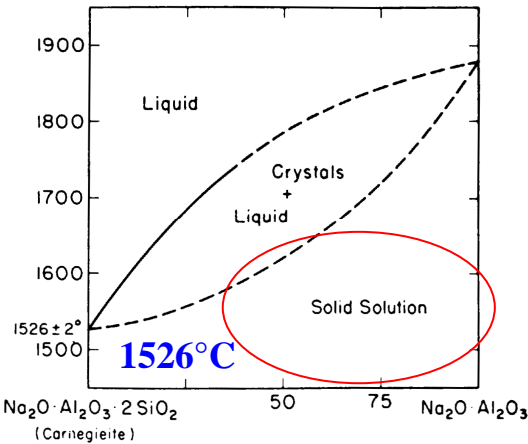
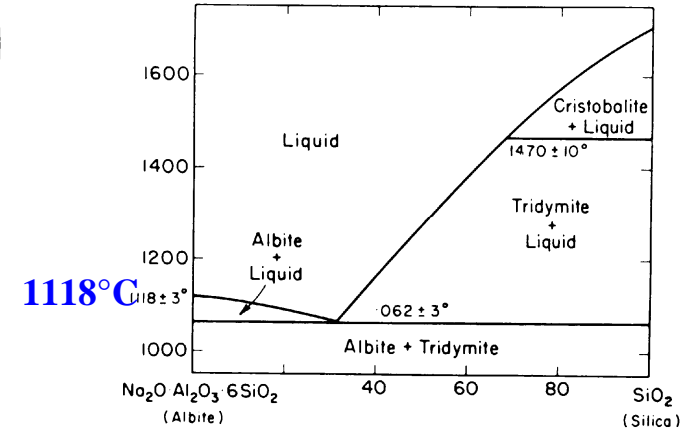
Available experimental phase diagram $\text{NaAlO}_2\text{-SiO}_2$



$\text{NaAlSi}_3\text{O}_8\text{-NaAlSi}_3\text{O}_8$
Greig, Barth(1938)

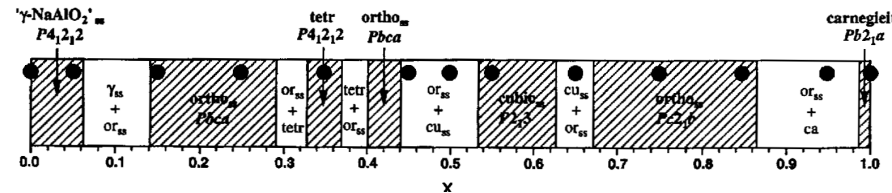


$\text{NaAlSi}_3\text{O}_8$ (Albite) - SiO_2
Schairer and Bowen (1956)



$\text{NaAlSiO}_4\text{-NaAlO}_2$
Schairer and Bowen (1956)

$\text{NaAlO}_2\text{-NaAlSiO}_4$ SYSTEM



$\text{NaAlO}_2\text{-NaAlSiO}_4$

Thompson (1997), Proposed compositional phase diagram at 1300 °C for the system $\text{Na}_{2-x}\text{Al}_{2-x}\text{Si}_x\text{O}_4$, $0 \leq x \leq 1$

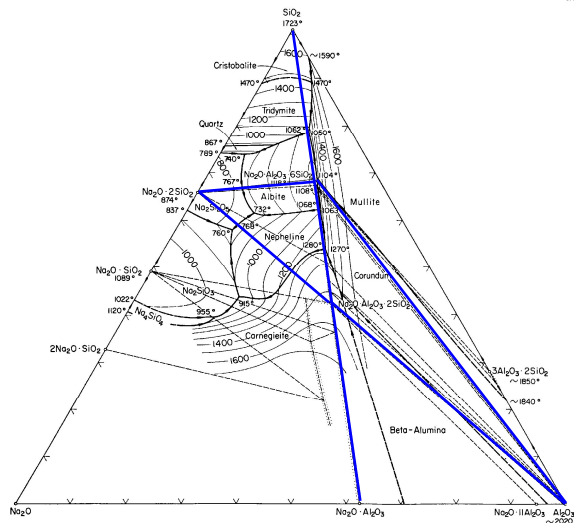
J.F. Schairer, N.L. Bowen, *The system $\text{Na}_2\text{O-Al}_2\text{O}_3\text{-SiO}_2$* , *Am. J. Sci.* **254**(2) (1956) 129-195.

Greig J.W., Barth T.F.W., *Am. Jour. Sci.*, 5th ser., **35A**, p.93-112 (1938)

Thompson J.G., Melnitchenko A., Palethorpe S.R., Withers R.L., *J. Solid State Chem.*, **131**, p.24-37 (1997)

Thompson J.G., Withers R.L., Melnitchenko A., Palethorpe S.R., *Acta Cryst.*, **B54**, p.531-546 (1998)

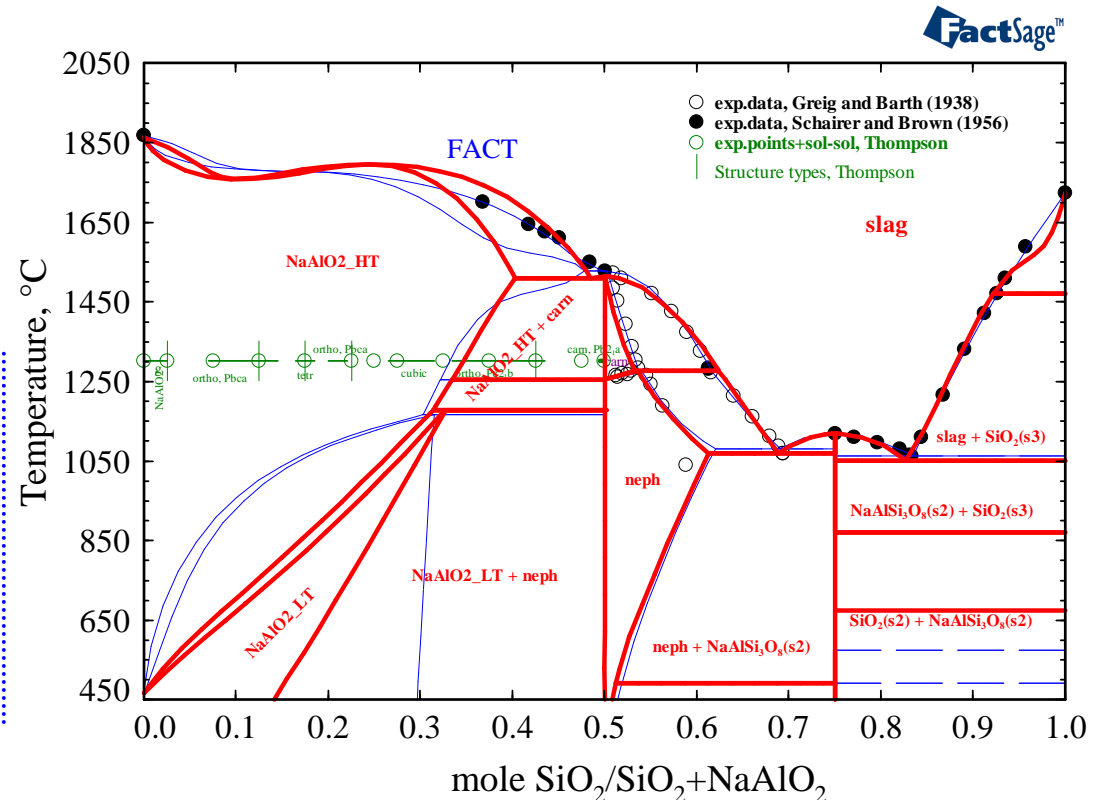
Current results of the assessment for the system $\text{NaAlO}_2\text{-SiO}_2$



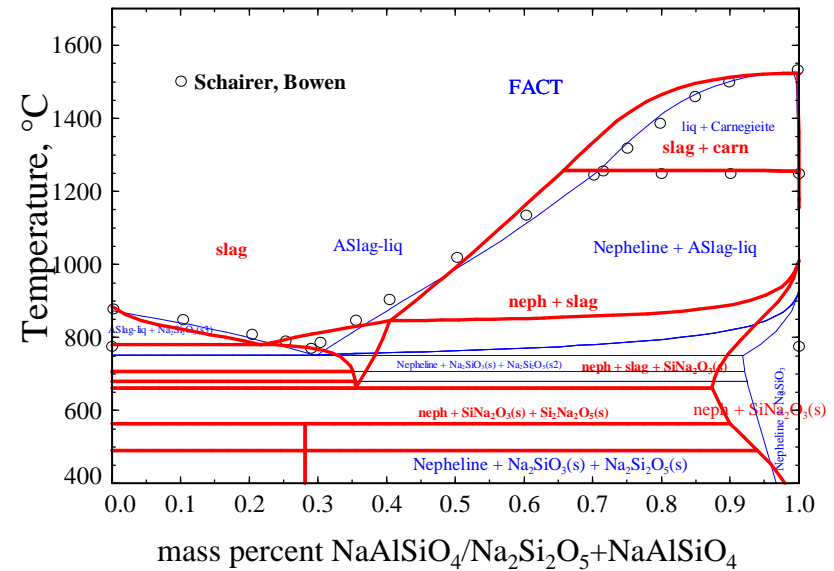
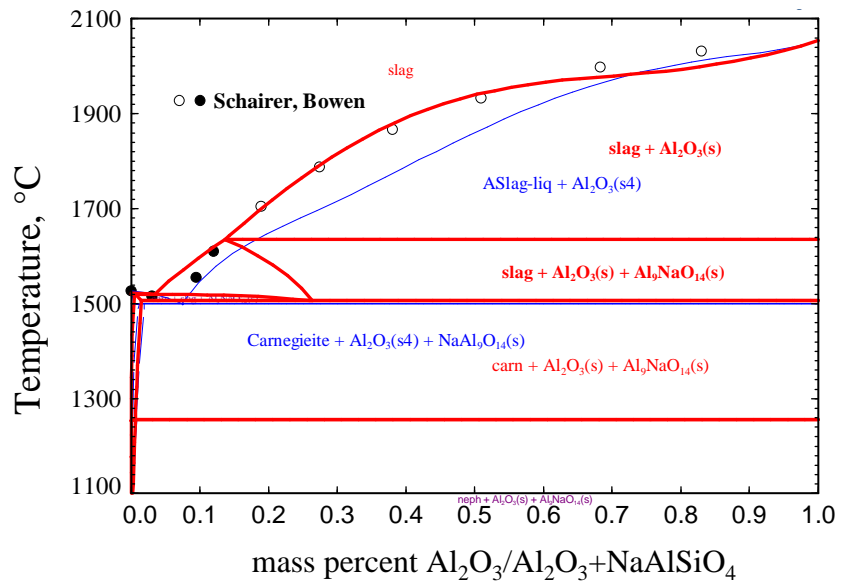
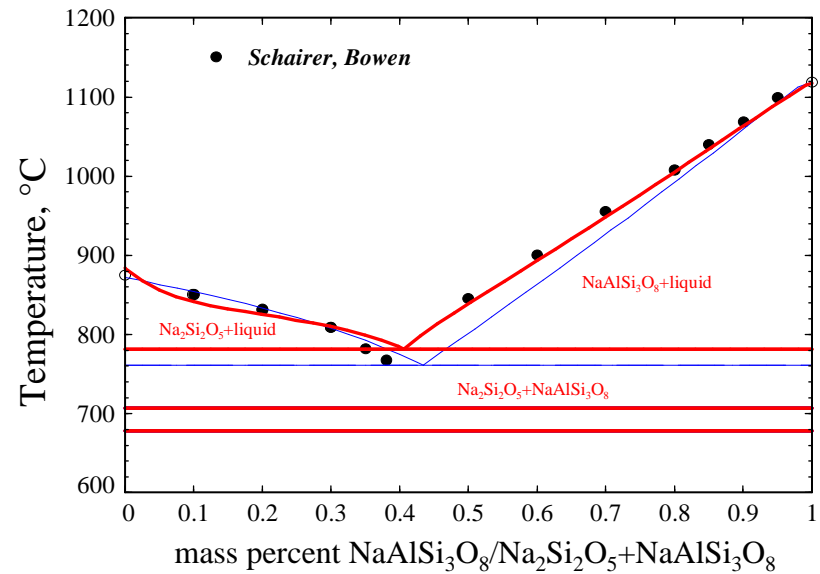
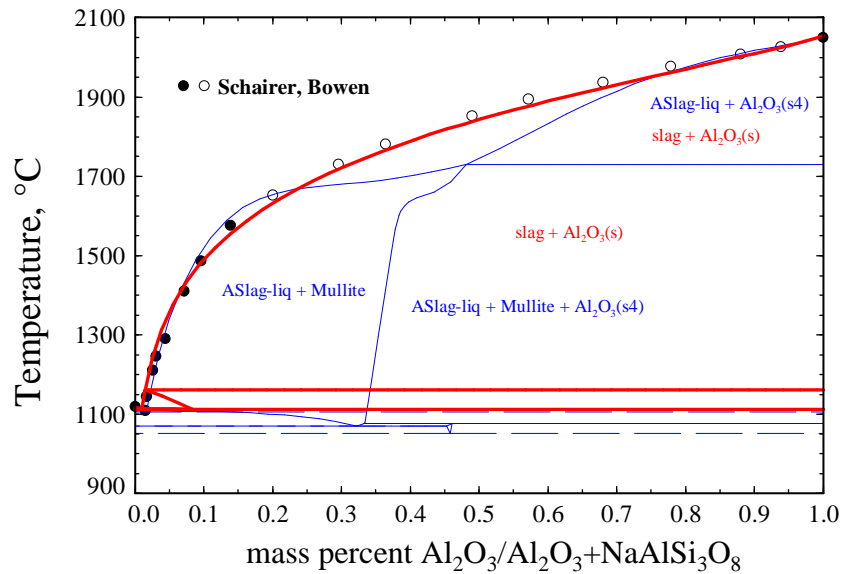
NaAlO_2 (low T , high T), Nepheline, Carnegite are represented by sublattice approach. The parameters of the solutions are optimised to obtain good description of the available experimental data.

Problems:

- ✓ Unknown solubility boundaries for NaAlO_2 (low T , high T) solutions
- ✓ Possible presence of a series of solid solutions with different crystallographic structure between NaAlO_2 and $\text{NaAlSi}_3\text{O}_8$



Quasi binary sections in the $\text{Na}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$ system

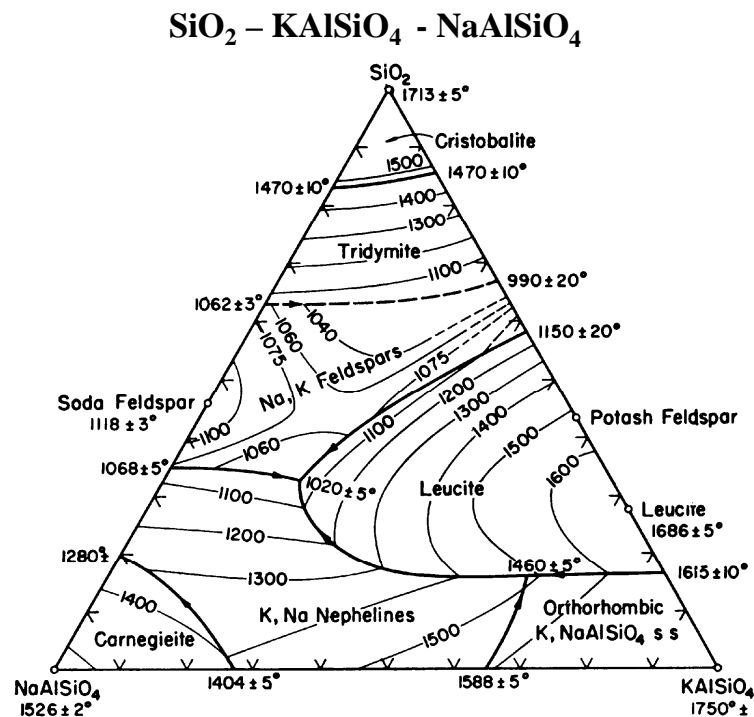


Conclusions

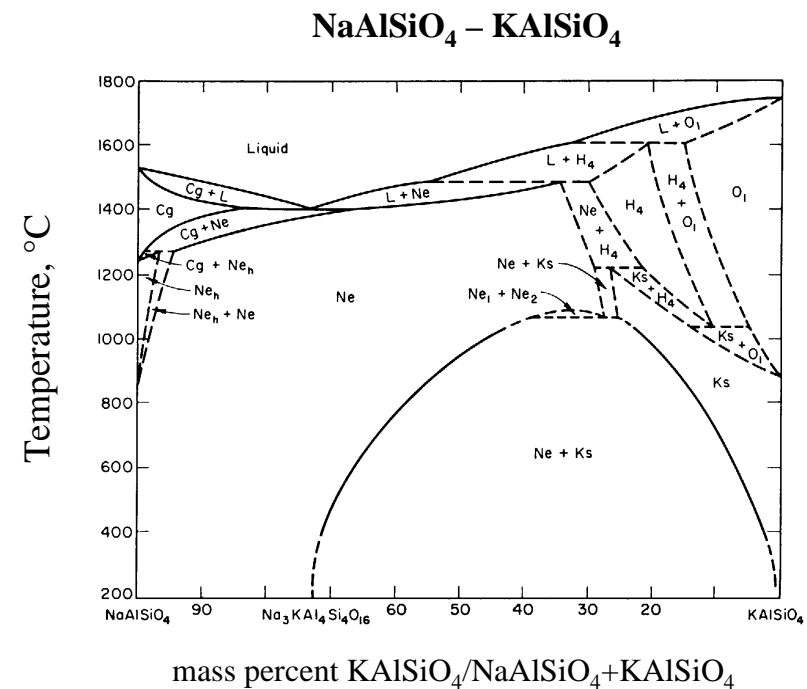
- The solution data for the binary systems $\text{Alk}_2\text{O-SiO}_2$, $\text{Alk}_2\text{O-Al}_2\text{O}_3$ (Alk=Na, K) and $\text{Al}_2\text{O}_3\text{-SiO}_2$ were re-optimised to accurate description of the phase diagrams taking into account the changes concerning the data on the pure liquid oxides
- Solid and liquid solutions in the ternary systems $\text{Na}_2\text{O-K}_2\text{O-SiO}_2$ and $\text{Alk}_2\text{O-Al}_2\text{O}_3\text{-SiO}_2$ (Alk=Na, K) were described using the new database
- Sublattice model was successfully applied for the solid solutions in the $\text{Na}_2\text{O-Al}_2\text{O}_3\text{-SiO}_2$ and $\text{K}_2\text{O-Al}_2\text{O}_3\text{-SiO}_2$ systems

Outlook

- Assessment of the system $\text{NaAlSiO}_4\text{-KAlSiO}_4\text{-SiO}_2$ system
- Creation of the database for possible quaternary solutions, e.g. $(\text{Na, K})\text{AlO}_2$ and $(\text{Na, K})(\text{Al, Si})\text{O}_4$



Schairer, J.F., *The alkali-feldspar join in the system NaAlSiO₄-KAlSiO₄-SiO₂*, *J. Geol.* **58** (5) 512-517



O.F. Tuttle, J.V. Smith, *The nepheline-kalsilite system II. Phase relations* *Am. J. Sci.* **256** (1958) 571-589

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