

GTT-Technologies, 11th Annual Workshop, June 3-5, 2009

## Thermodynamic optimisation of the systems

**K<sub>2</sub>O-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> and Na<sub>2</sub>O-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub>**

June 3-5, 2009 | Elena Yazhenskikh, Klaus Hack\*, Michael Mueller

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# Content

Motivation and aim of the work

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Assessment for ternary systems

Summary and outlook

# Motivation and aims

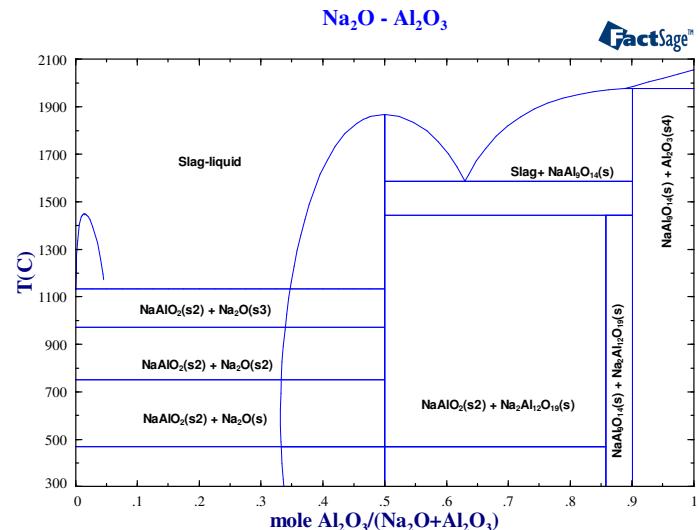
Hot gas cleaning: alkali removing by slags with high potential of alkali retention ( $\text{SiO}_2$ ,  $\text{Al}_2\text{O}_3$ ,  $\text{Fe}_2\text{O}_3$ ) or by getter materials (kaolin, bauxite)

Thermodynamic calculation/prediction for slag relevant oxide systems, which are different from the point of view of experimental measurements

- Calculation requires:
- Reliable database, based on the experimental data
  - Software

Available databases are not sufficient to model the complete coal ash (slag) system

No solution



Aim – development of a new data base for the slag relevant system containing alumina, silica, alkali oxides

# Modelling of liquid and solid solutions

Composition of the liquid slag – silica, alumina, Alk<sub>2</sub>O (Alk=Na, K)

Chosen model – associate species approach (introduced for slag by Spear, Allendorf, Besmann, 2002):

- suitable for this system
- relatively simple for using and modification

Pure liquid oxide	
Na <sub>2</sub> O, K <sub>2</sub> O, Al <sub>2</sub> O <sub>3</sub> , SiO <sub>2</sub> ·2	

+

Ternary components	
Compounds	Associate species
KAlSiO <sub>4</sub>	KAlSiO <sub>4</sub> ·2/3
KAlSi <sub>2</sub> O <sub>6</sub>	KAlSi <sub>2</sub> O <sub>6</sub> ·1/2
NaAlSiO <sub>4</sub>	NaAlSiO <sub>4</sub> ·2/3
NaAlSi <sub>3</sub> O <sub>8</sub>	NaAlSi <sub>3</sub> O <sub>8</sub> ·2/5

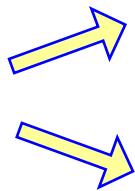
Binary components	
Compounds	Associate species
Na <sub>4</sub> SiO <sub>4</sub>	Na <sub>4</sub> SiO <sub>4</sub> ·2/5
Na <sub>2</sub> SiO <sub>3</sub>	Na <sub>2</sub> SiO <sub>3</sub> ·2/3
Na <sub>2</sub> Si <sub>2</sub> O <sub>5</sub>	Na <sub>2</sub> Si <sub>2</sub> O <sub>5</sub> ·1/2
K <sub>2</sub> SiO <sub>3</sub>	K <sub>2</sub> SiO <sub>3</sub> ·2/3
K <sub>2</sub> Si <sub>2</sub> O <sub>5</sub>	K <sub>2</sub> Si <sub>2</sub> O <sub>5</sub> ·1/2
K <sub>2</sub> Si <sub>4</sub> O <sub>9</sub>	K <sub>2</sub> Si <sub>4</sub> O <sub>9</sub> ·1/3
NaAlO <sub>2</sub>	NaAlO <sub>2</sub>
-	Na <sub>2</sub> Al <sub>4</sub> O <sub>7</sub> ·1/3
KAlO <sub>2</sub>	KAlO <sub>2</sub>
-	Na <sub>2</sub> Al <sub>4</sub> O <sub>7</sub> ·1/3
Al <sub>6</sub> Si <sub>2</sub> O <sub>13</sub>	Al <sub>6</sub> Si <sub>2</sub> O <sub>13</sub> ·1/4

*Interaction  
between  
solution  
components*

**Associate species model:**

Al<sub>6</sub>Si<sub>2</sub>O<sub>13</sub>·1/4, Al<sub>2</sub>O<sub>3</sub>, SiO<sub>2</sub>·2

Mullite



**4 sublattice model:**

(Al<sup>3+</sup>)<sub>1</sub>(Al<sup>3+</sup>)<sub>1</sub>(Al<sup>3+</sup>, Si<sup>4+</sup>)<sub>1</sub>(O<sup>2-</sup>, Va)<sub>5</sub>

**(KAl)<sub>1-x</sub>Si<sub>x</sub>O<sub>2</sub> solid solution:**

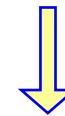
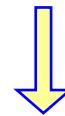
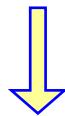
Associate species KAlO<sub>2</sub>, KAlSiO<sub>4</sub>

# Optimisation procedure

Experimental data: phase diagram data, activity data (for binary systems)

Pure solid and liquid substances from the FACT database

Some solution species from database of Spear et al.

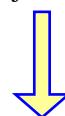


## Adjustable parameters:

$\Delta H_f^{298}$  and  $S^{298}$  for the liquid and solid solution species,  $\Delta H_f^{298}$  and  $S^{298}$  for the pure solid compounds (part.), interaction parameters between species

$$G_m = \sum x_i G_i^0 + RT \sum x_i \ln x_i + \sum_{i < j} x_i x_j \sum_v L_{ij}^{(v)} (x_i - x_j)^v$$

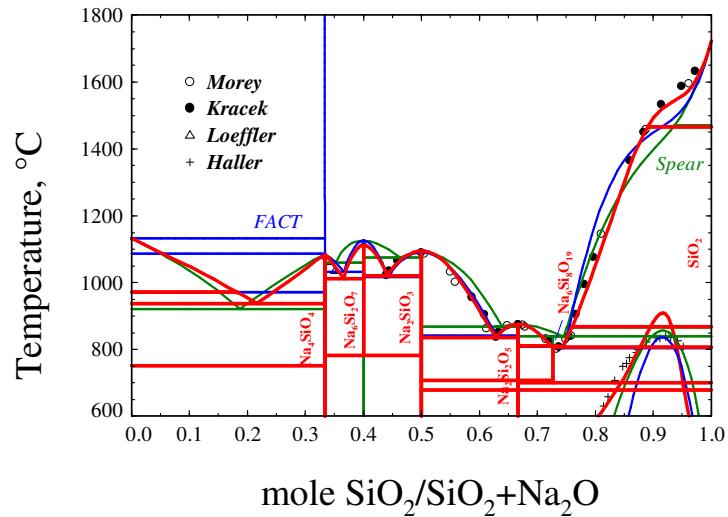
$$L_{ij}^{(v)} = A_{ij}^{(v)} + B_{ij}^{(v)} \cdot T + C_{ij}^{(v)} \cdot T \cdot \ln T + D_{ij}^{(v)} \cdot T^2 + \dots, v = 0, 1$$



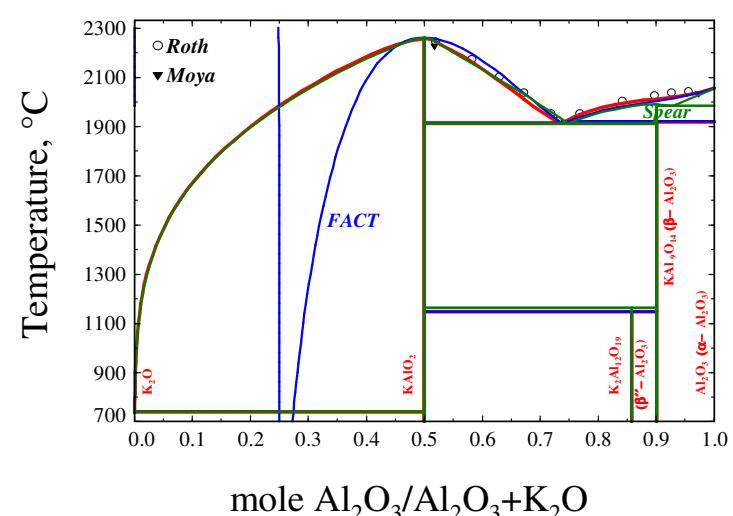
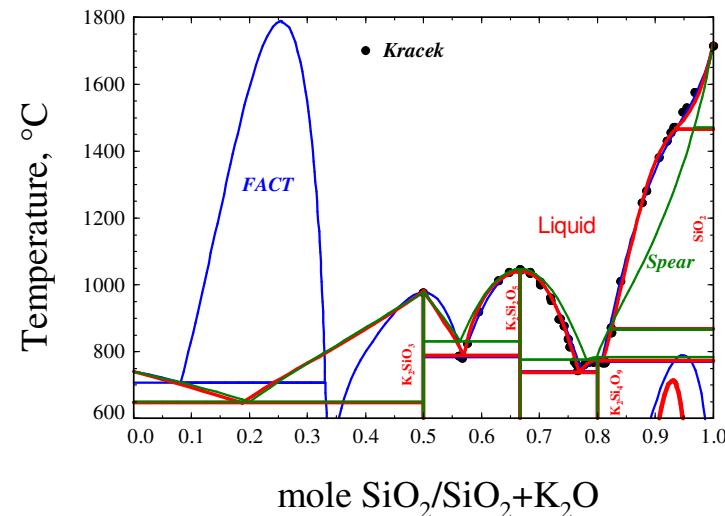
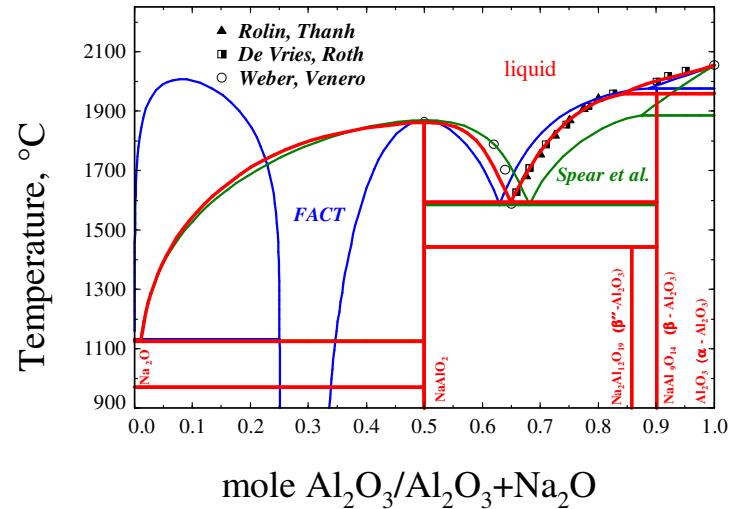
New database for the oxide systems

# Results of assessment for binary systems

Alk<sub>2</sub>O-SiO<sub>2</sub>, Alk=Na, K



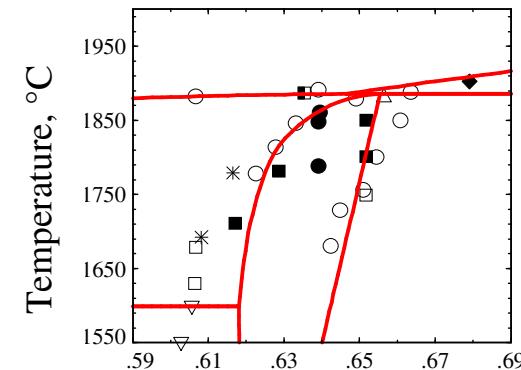
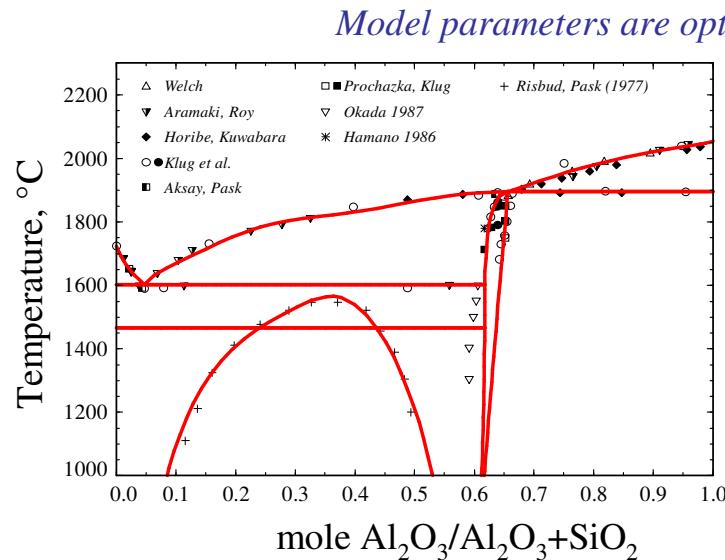
Alk<sub>2</sub>O-Al<sub>2</sub>O<sub>3</sub>, Alk=Na, K



# Results of assessment for binary systems

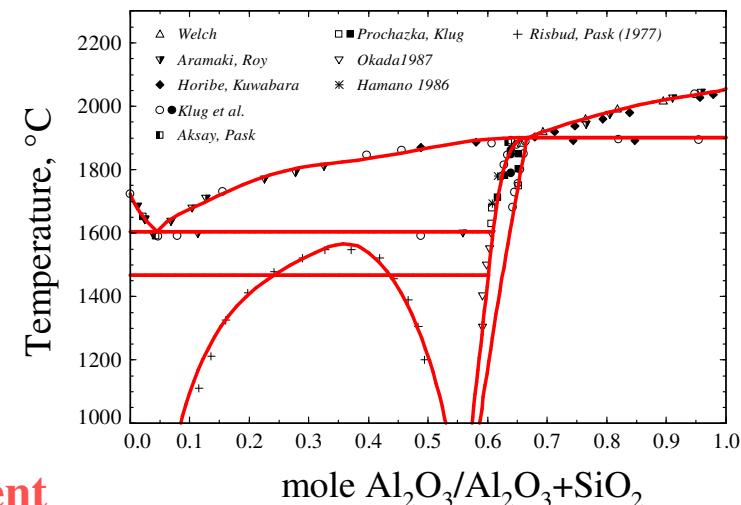
## Associate model for mullite

[Spear et al. in 2002]



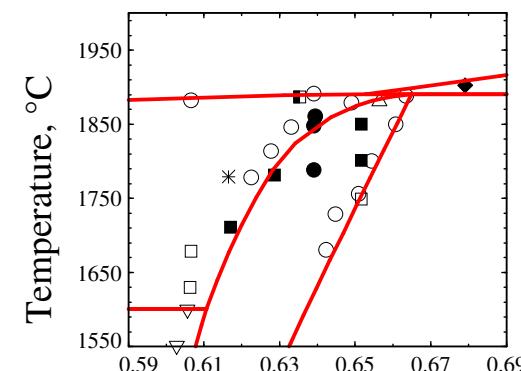
## Four-sublattice model for mullite

[Mao et al. in 2005 ]



Congruent

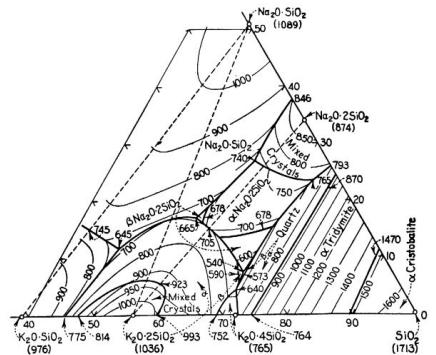
Incongruent



# Results of assessment for ternary systems

Comparison of the calculated isotherms with the experimental points

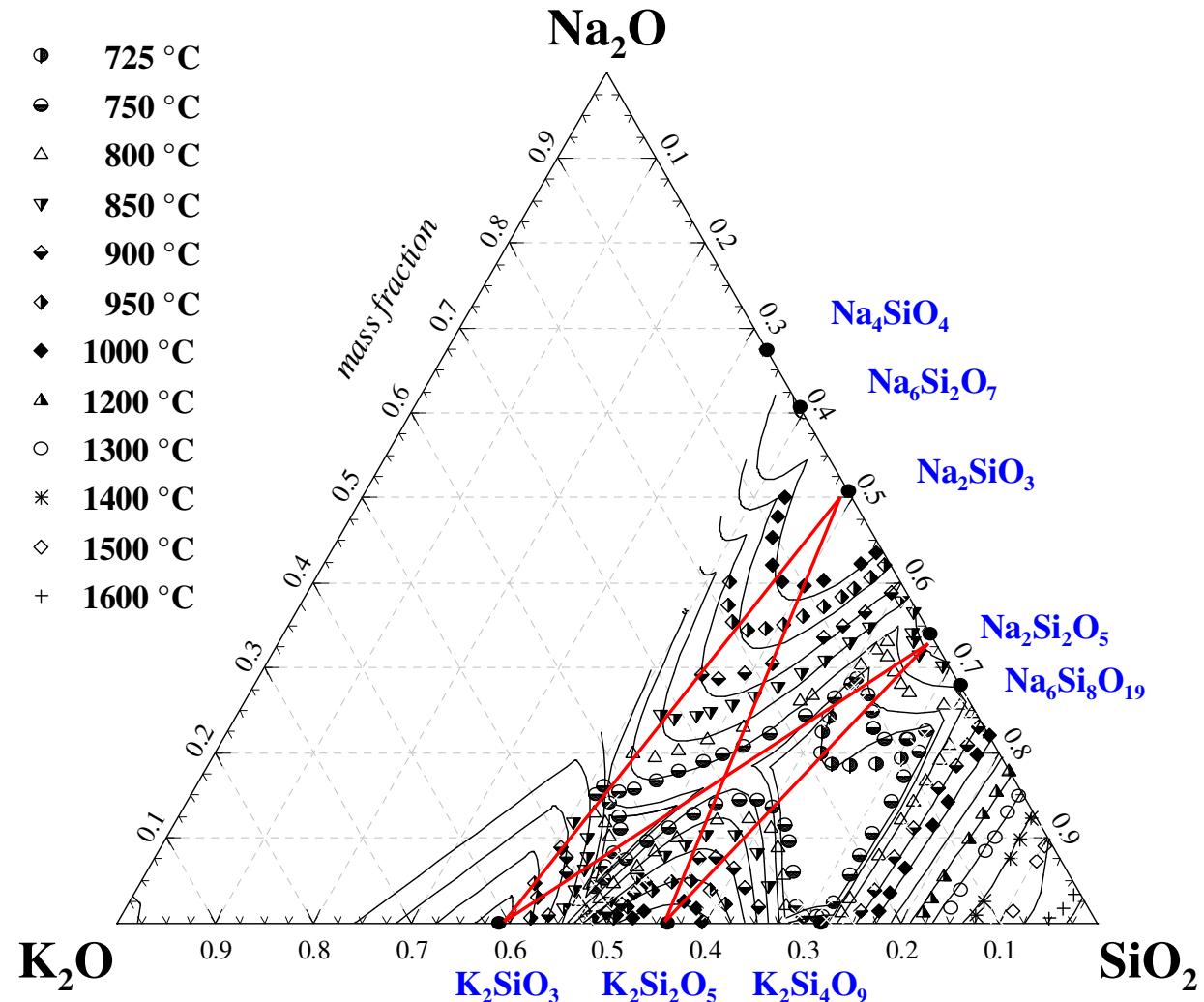
$\text{Na}_2\text{O}-\text{K}_2\text{O}-\text{SiO}_2$



The same binary species  
in ternary liquid

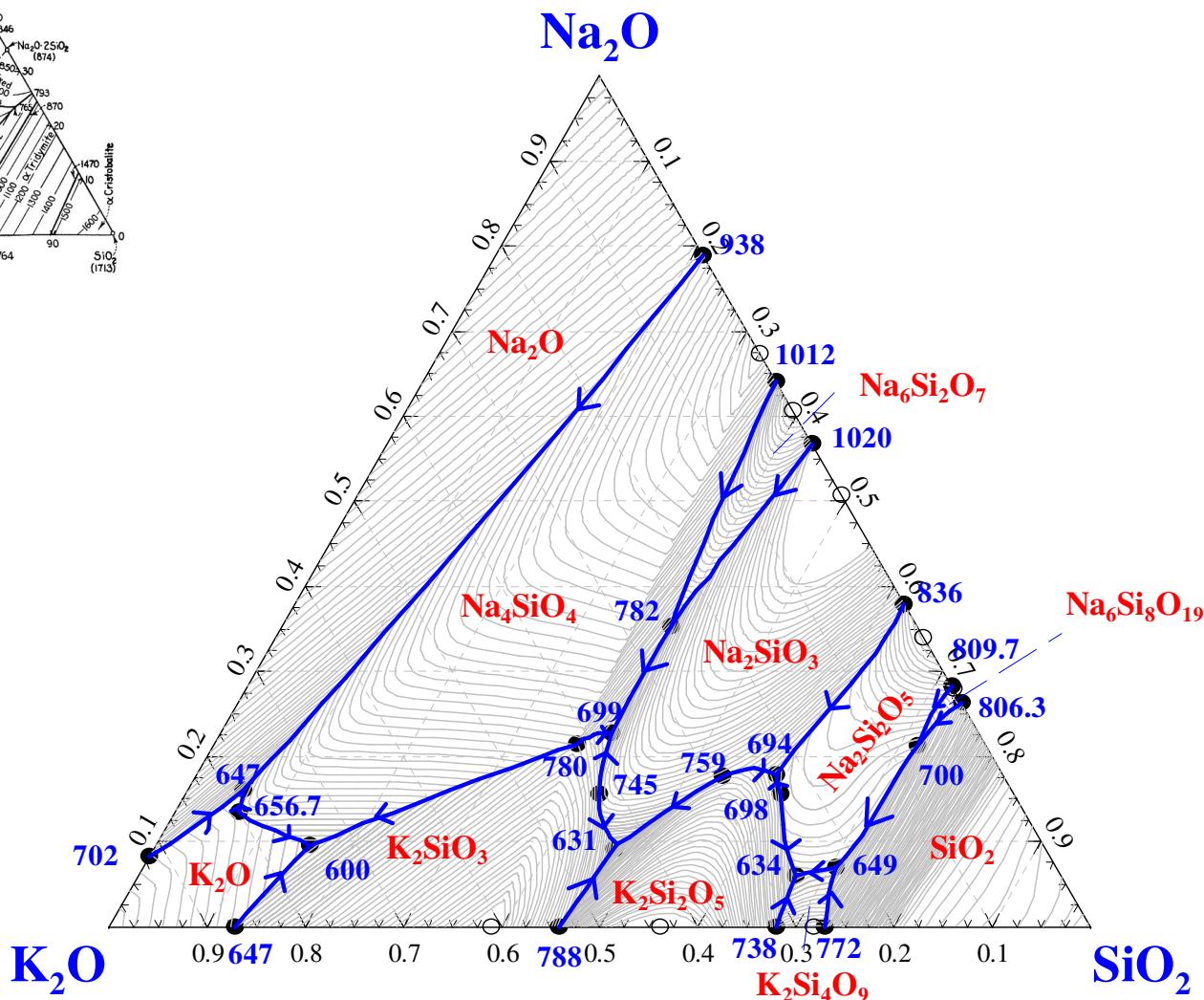
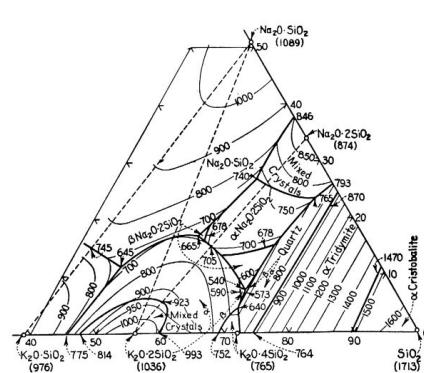
Interacting components:  
 $\text{Na}_2\text{SiO}_3^{*2/3} - \text{K}_2\text{SiO}_3^{*2/3}$   
 $\text{Na}_2\text{Si}_2\text{O}_5^{*1/2} - \text{K}_2\text{Si}_2\text{O}_5^{*1/2}$   
 $\text{Na}_2\text{SiO}_3^{*2/3} - \text{K}_2\text{Si}_2\text{O}_5^{*1/2}$   
 $\text{Na}_2\text{Si}_2\text{O}_5^{*1/2} - \text{K}_2\text{SiO}_3^{*2/3}$

- 725 °C
- 750 °C
- △ 800 °C
- ▼ 850 °C
- ◆ 900 °C
- ◊ 950 °C
- ◆ 1000 °C
- ▲ 1200 °C
- 1300 °C
- \* 1400 °C
- ◊ 1500 °C
- + 1600 °C

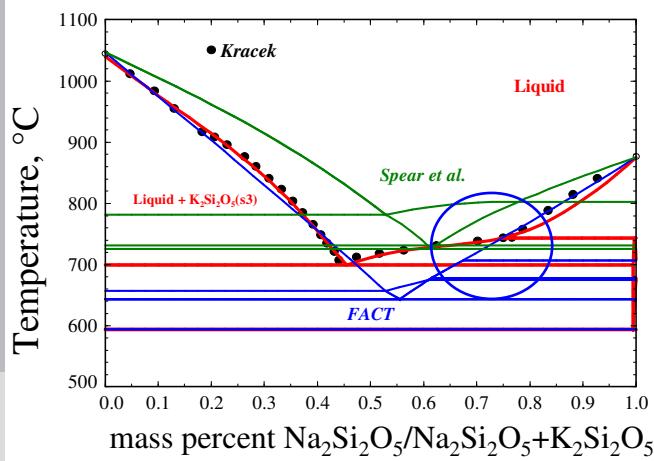
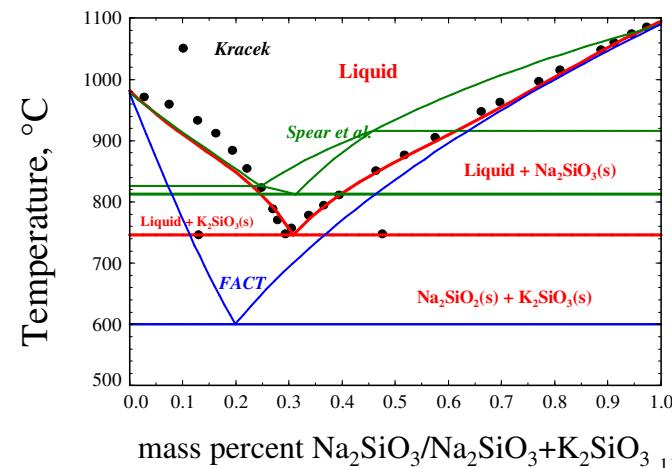
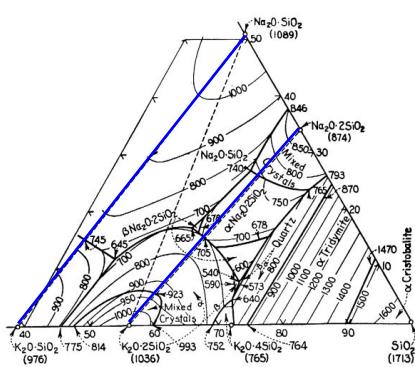


# Results of assessment for ternary systems

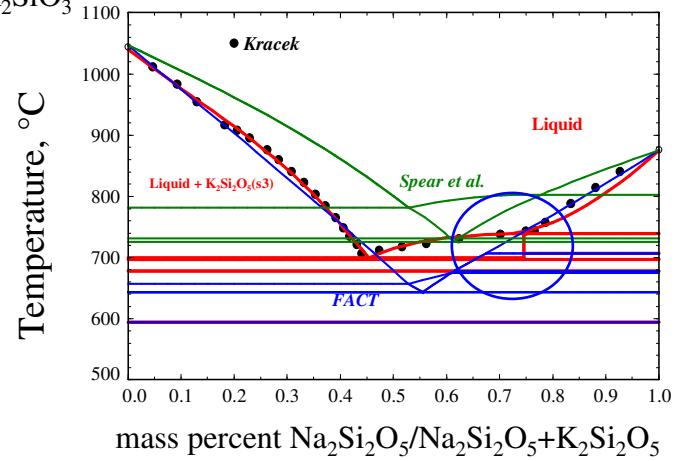
## Predicted phase fields and ternary points



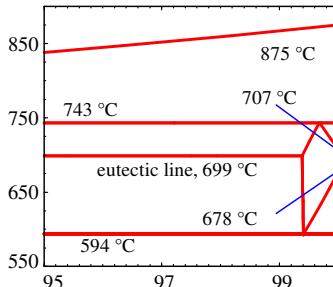
# Quasi binary section in the $\text{Na}_2\text{O}-\text{K}_2\text{O}-\text{SiO}_2$ system



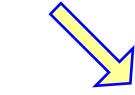
## $\text{K}_2\text{Si}_2\text{O}_5-\text{Na}_2\text{Si}_2\text{O}_5$



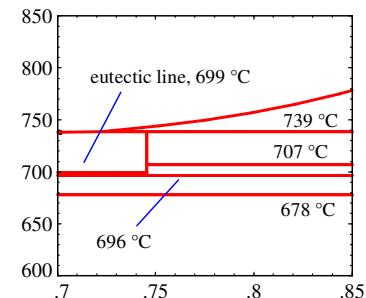
## Possible interpretations



Solubility region

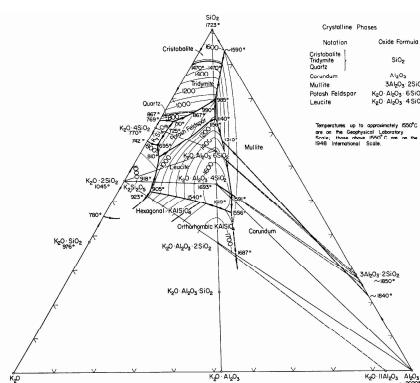


Additional “ternary” compound



# Results of assessment for ternary systems

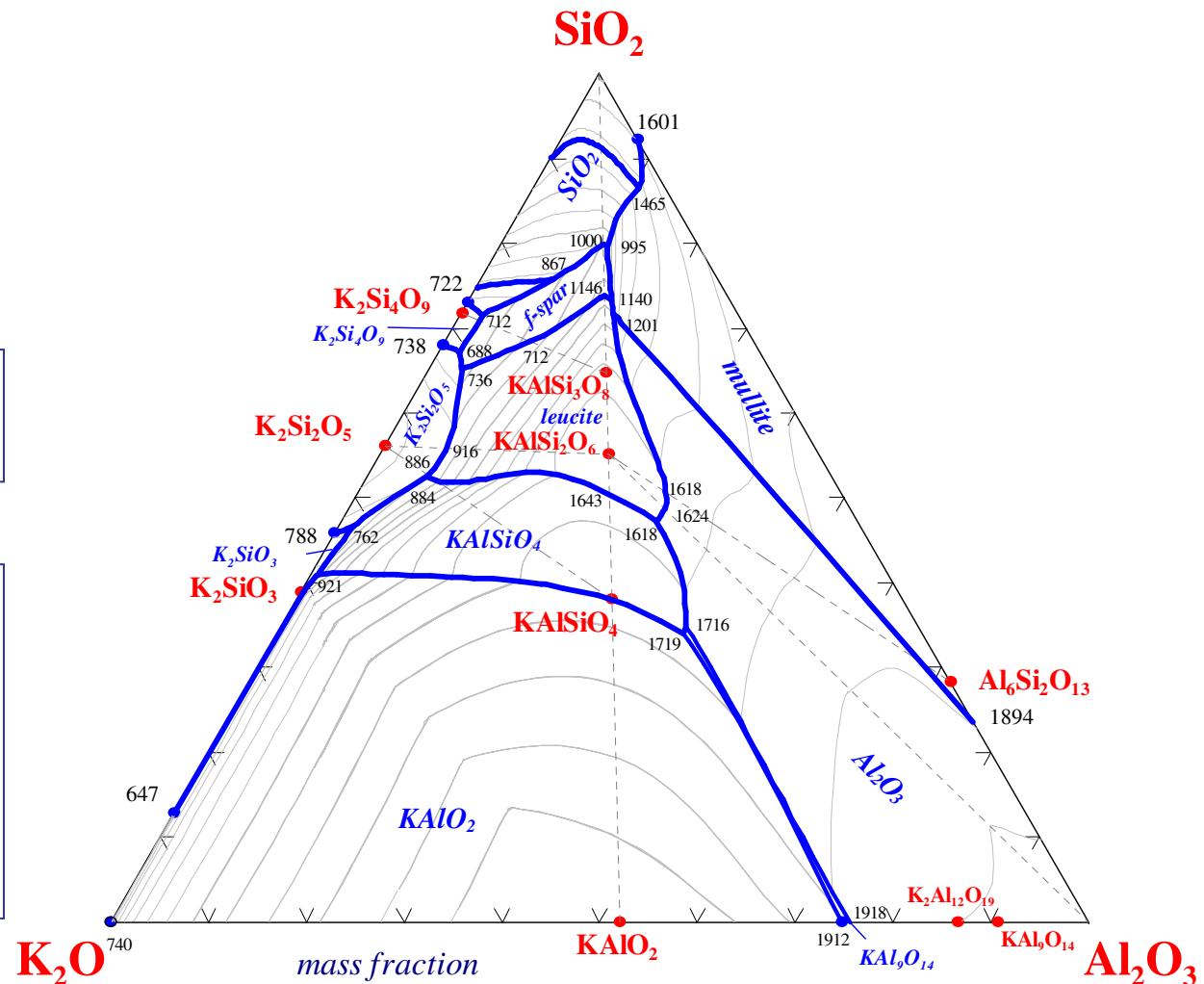
## Predicted phase fields and ternary points



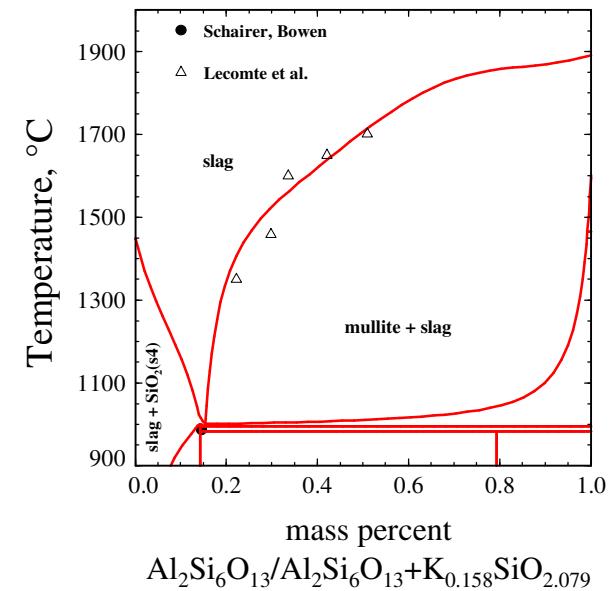
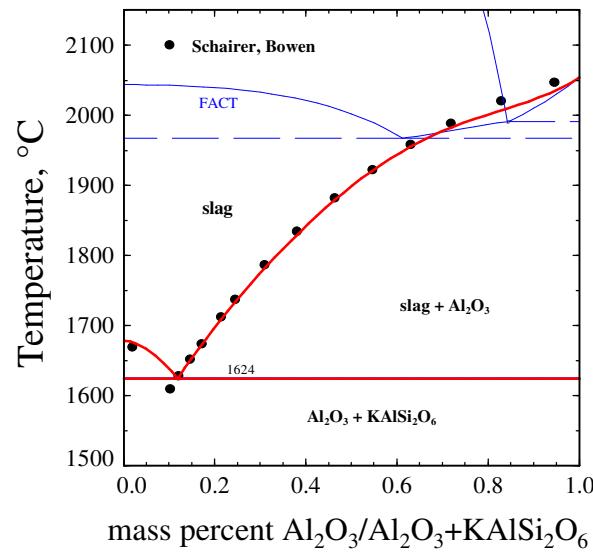
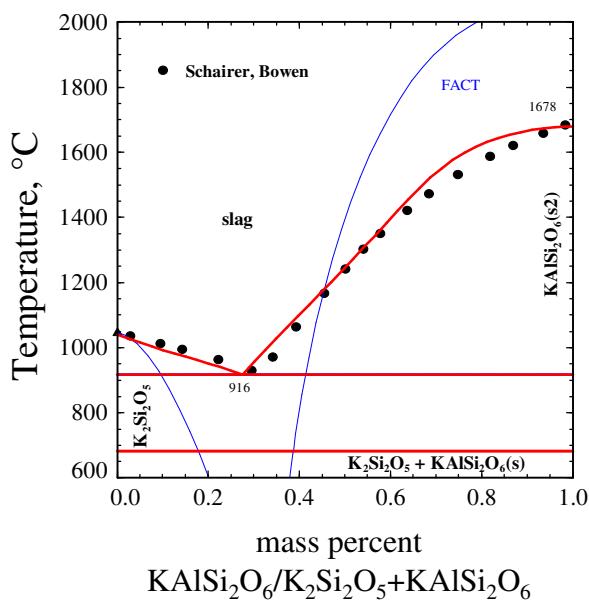
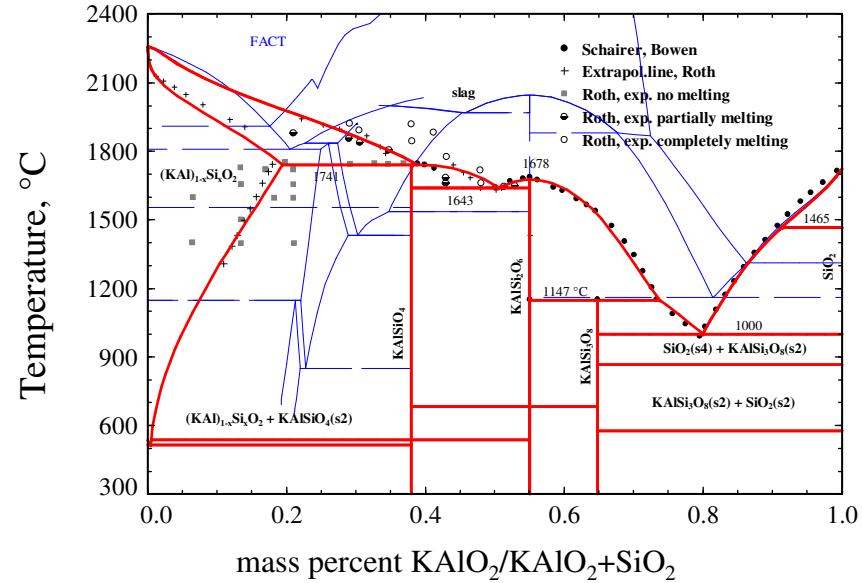
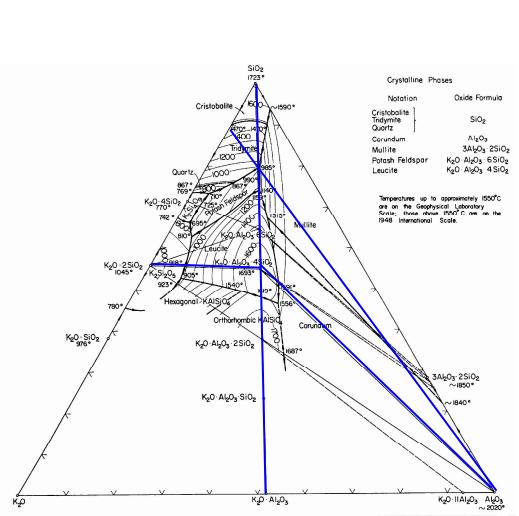
The same binary +  
ternary species

Interacting components:

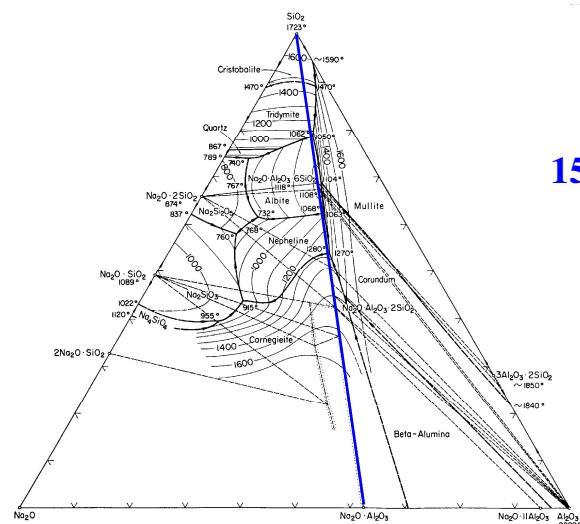
- $\text{Al}_2\text{O}_3 - \text{KAlSi}_2\text{O}_6^{*1/2}$
- $\text{K}_2\text{Si}_2\text{O}_5^{*1/2} - \text{KAlSi}_2\text{O}_6^{*1/2}$
- $\text{K}_2\text{Si}_4\text{O}_9^{*1/3} - \text{KAlSi}_2\text{O}_6^{*1/2}$
- $\text{Si}_2\text{O}_4 - \text{KAlSi}_2\text{O}_6^{*1/2}$
- $\text{Al}_6\text{Si}_2\text{O}_{13}^{*1/4} - \text{KAlSi}_2\text{O}_6^{*1/2}$



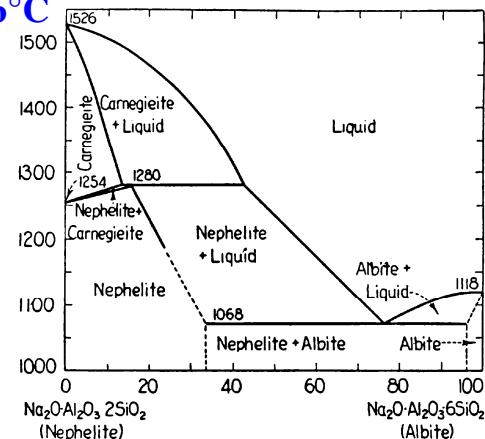
# Quasi binary section in the $\text{K}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$ system



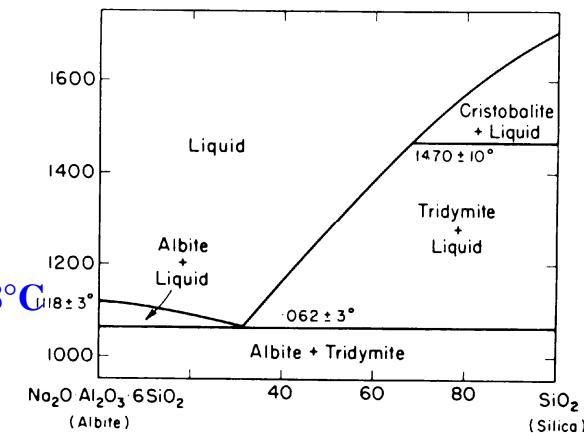
# Available experimental phase diagram



1526°C

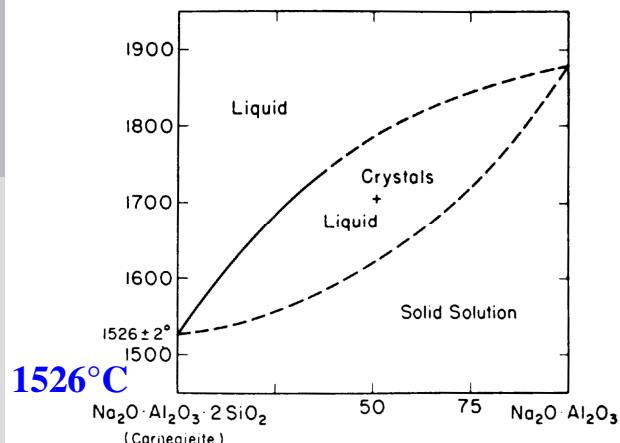


1526



1118

$\text{NaAlSiO}_4$  (Neph/Carn) –  $\text{NaAlSi}_3\text{O}_8$   
Greig and Barth (1938)

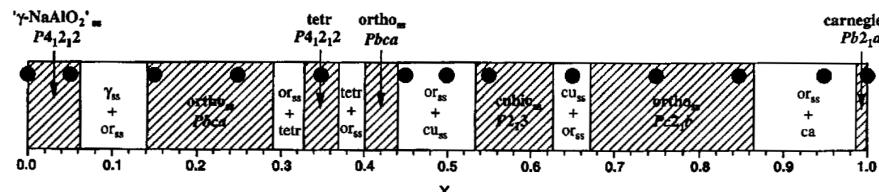


1526°C

$\text{NaAlSiO}_4$  -  $\text{NaAlO}_2$

Schairer and Bowen (1956)

$\text{NaAlO}_2$ - $\text{NaAlSiO}_4$  SYSTEM



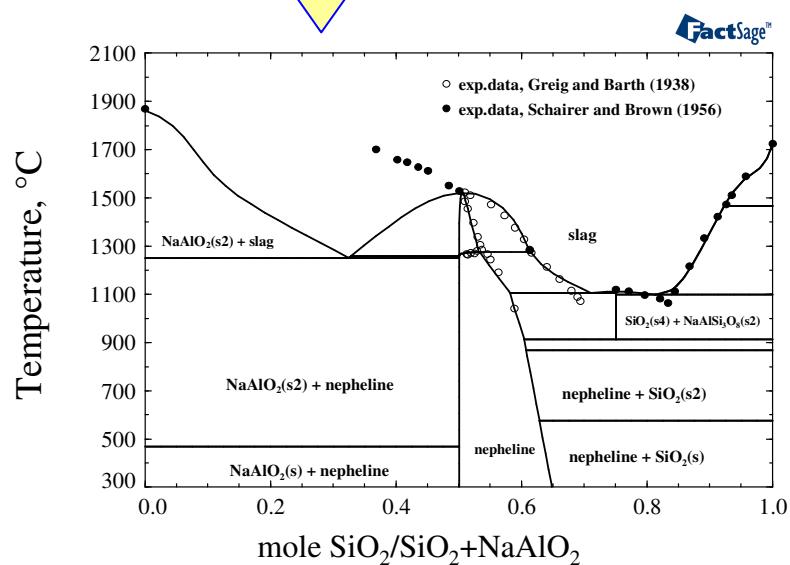
$\text{NaAlO}_2$  -  $\text{NaAlSiO}_4$

Thompson (1997), Proposed compositional phase diagram at 1300 °C for the system  $\text{Na}_{2-x}\text{Al}_{2-x}\text{Si}_x\text{O}_4$ ,  $0 \leq x \leq 1$

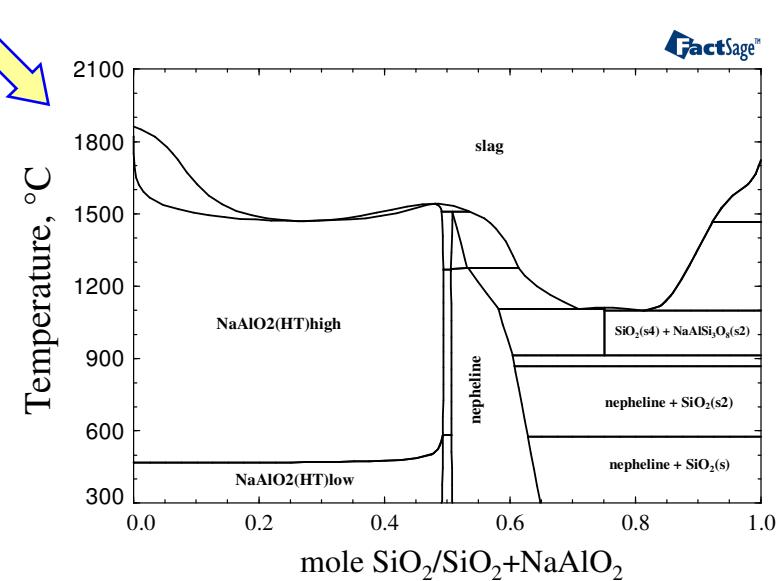
# Modelling of solid phases

Associate  
Species

Name	Solid solution components	remark
Mullite	$\text{Al}_6\text{Si}_2\text{O}_{13}$ : $\text{Al}_6\text{Si}_2\text{O}_{13} \cdot 1/4$ , $\text{Al}_2\text{O}_3$ , $\text{SiO}_2 \cdot 2$	OK
Natrium disilicate	$(\text{Na}_{1-x}\text{K}_x)_2\text{Si}_2\text{O}_5$ : $\text{Na}_2\text{Si}_2\text{O}_5$ , $\text{K}_2\text{Si}_2\text{O}_5$	OK
Potassium aluminate	$(\text{KAl})_{1-x}\text{Si}_x\text{O}_2$ : $\text{KAlO}_2$ , $\text{KAlSiO}_4$	OK
Nepheline, carnegieite	$\text{NaAlSiO}_4$ : $\text{NaAlSiO}_4$ , $\text{NaAlSi}_2\text{O}_6$	OK
Natrium aluminate	$(\text{NaAl})_{1-x}\text{Si}_x\text{O}_2$ : $\text{NaAlO}_2$ , $\text{NaAlSiO}_4$	?



$\text{NaAlSiO}_4$  (neph, carn) as associate solutions  
 $\text{NaAlO}_2$  (low, high) as stoichiometric compounds

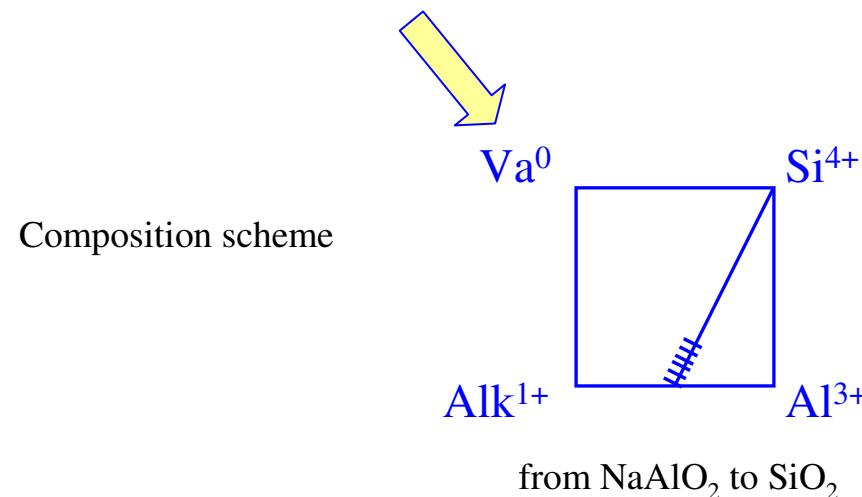
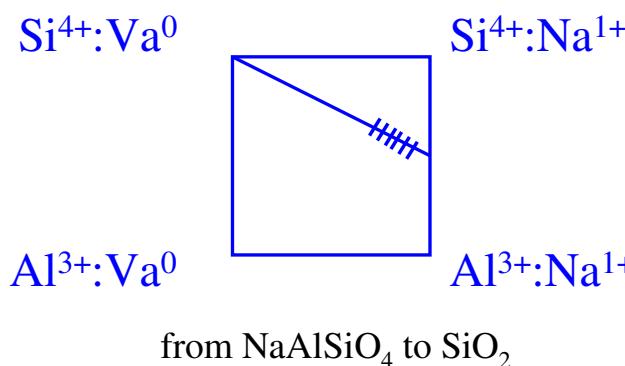


$\text{NaAlSiO}_4$  (low, high) and  $\text{NaAlO}_2$  (low, high)  
- as associate solutions

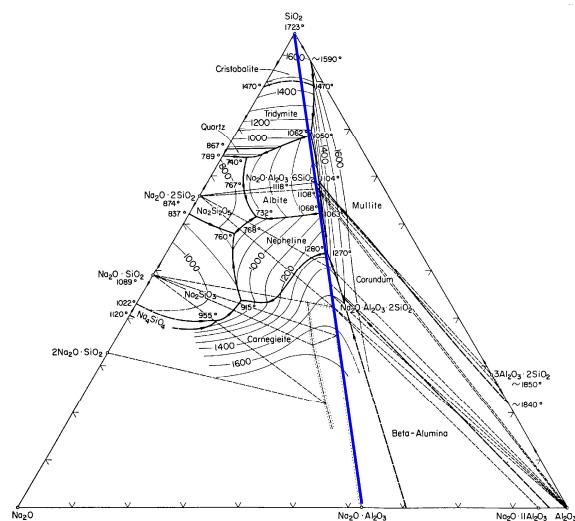
# Modelling of solid phases

Sublattice  
approach

Name	Formula	remark
Mullite	$(\text{Al}^{3+})_1(\text{Al}^{3+})_1(\text{Al}^{3+}, \text{Si}^{4+})_1(\text{O}^{2-}, \text{Va})_5$	OK
NaAlSiO <sub>4</sub>	Nepheline (low T), carnegieite (high T) 4 sublattices: $(\text{Al}^{3+}, \text{Si}^{4+})_2\text{Va}_1^0(\text{Na}^{1+}, \text{Va}^0)_1(\text{O}^{2-})_4$	new
Potassium aluminate	$\text{KAlO}_2$ - low T, high T 3 sublattices: $(\text{Al}^{3+}, \text{Si}^{4+})_1(\text{K}^{1+}, \text{Va}^0)_1(\text{O}^{2-})_2$	new
Natrium aluminate	$\text{NaAlO}_2$ - low T, high T 3 sublattices: $(\text{Al}^{3+}, \text{Si}^{4+})_1(\text{Na}^{1+}, \text{Va}^0)_1(\text{O}^{2-})_2$	new



# Preliminary results for the quasi binary section $\text{NaAlO}_2 - \text{SiO}_2$

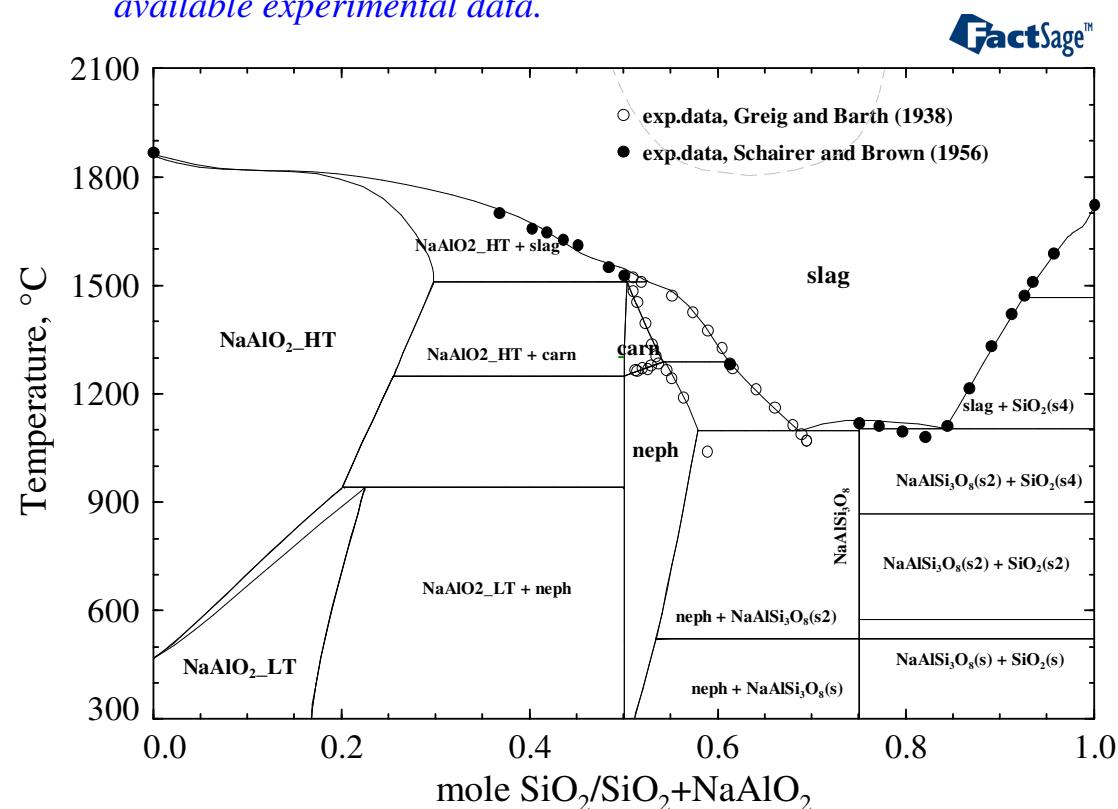


## Problems:

- ✓ Unknown solubility boundaries for  $\text{NaAlO}_2$  (low  $T$ , high  $T$ ) solutions
- ✓ Possible presence of a series of solid solutions with different crystallographic structure between  $\text{NaAlO}_2$  and  $\text{NaAlSiO}_4$

## $\text{Na}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$

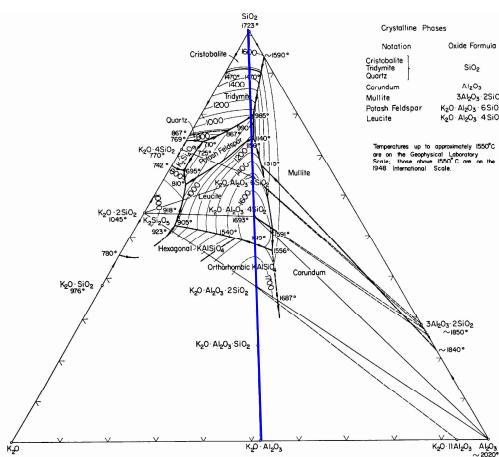
$\text{NaAlO}_2$  (low  $T$ , high  $T$ ), Nepheline, Carnegieite are represented by sublattice approach. The parameters of the solutions are optimised to obtain good description of the available experimental data.



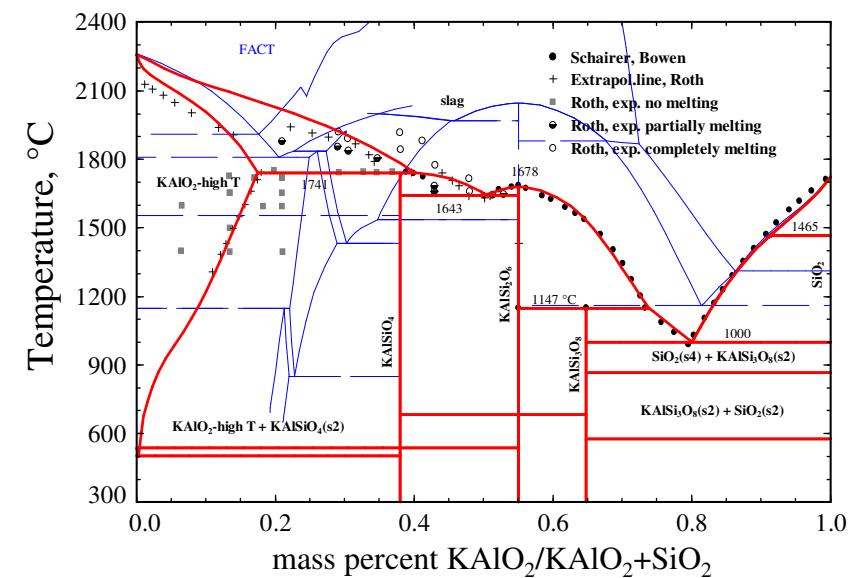
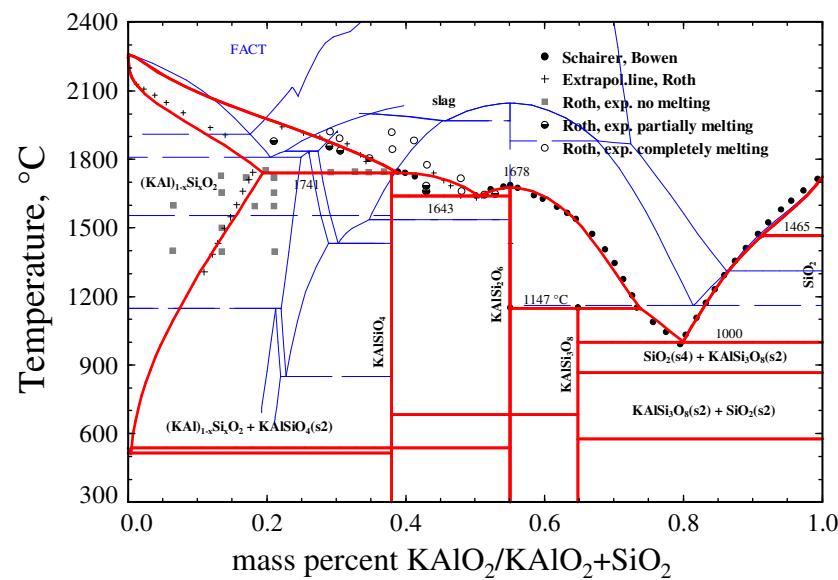
# Comparison between 2 models for the solid solution based on $\text{KAlO}_2$

$\text{K}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$

Slag, solid solution –  
Associate species



Slag– Associate species model  
solid solution - sublattice



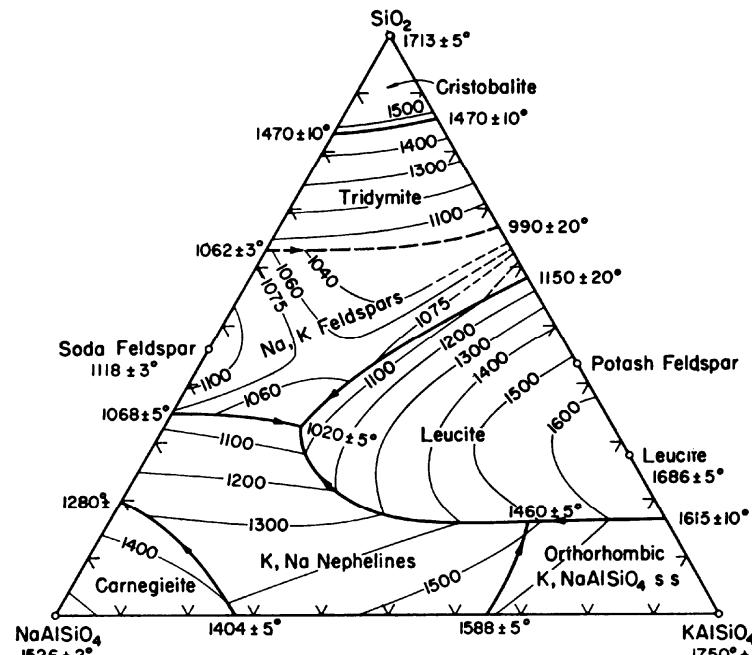
Sublattice model should be used for the purpose of „uniformity“ for both aluminates,  $\text{NaAlO}_2$  and  $\text{KAlO}_2$ , and further for quaternary solution ( $\text{Na}, \text{K}\text{AlO}_2$ )

## Summary and outlook

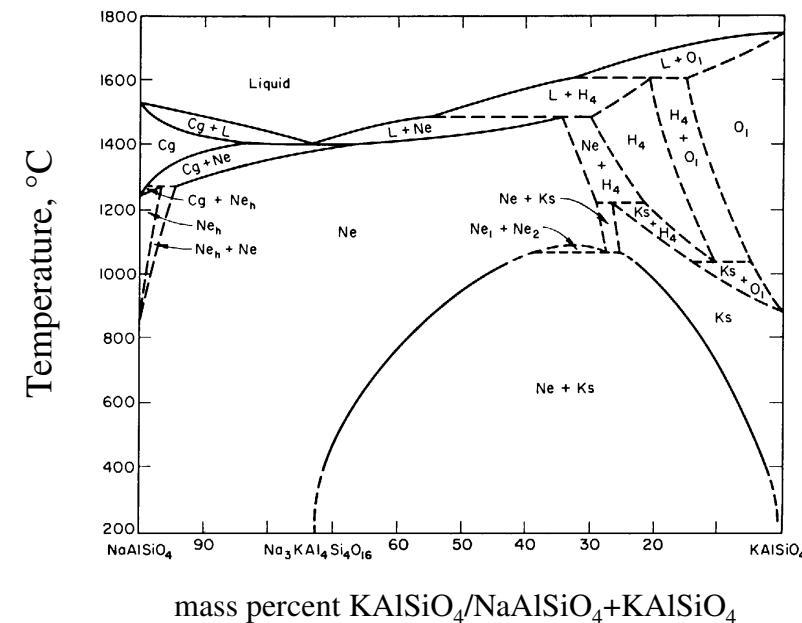
- The solution data for the binary systems  $\text{Alk}_2\text{O}-\text{SiO}_2$ ,  $\text{Alk}_2\text{O}-\text{Al}_2\text{O}_3$  ( $\text{Alk}=\text{Na, K}$ ) and  $\text{Al}_2\text{O}_3-\text{SiO}_2$  were generated to accurate description of the phase diagrams
- Solid and liquid solutions in the ternary systems  $\text{Na}_2\text{O}-\text{K}_2\text{O}-\text{SiO}_2$  and  $\text{K}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$  were described using the new database
- Sublattice model was successfully applied for the solid solutions in the  $\text{Na}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$  and  $\text{K}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$  systems

## In future:

- Optimisation of the solution parameters in the  $\text{Na}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$  system
- Creation of the database for possible quaternary solutions, e.g.  $(\text{Na}, \text{K})\text{AlO}_2$  and  $(\text{Na}, \text{K})(\text{Al}, \text{Si})\text{O}_4$



$\text{SiO}_2 - \text{KAlSiO}_4 - \text{NaAlSiO}_4$   
Schairer (1950)



$\text{NaAlSiO}_4 - \text{KAlSiO}_4$   
Tuttle, Smith (1958)

# Thank you for your attention