

# A Thermochemical Approach to Thermophysical Properties - Modelling Surface and Interfacial Tension of Liquids

Risto Pajarre

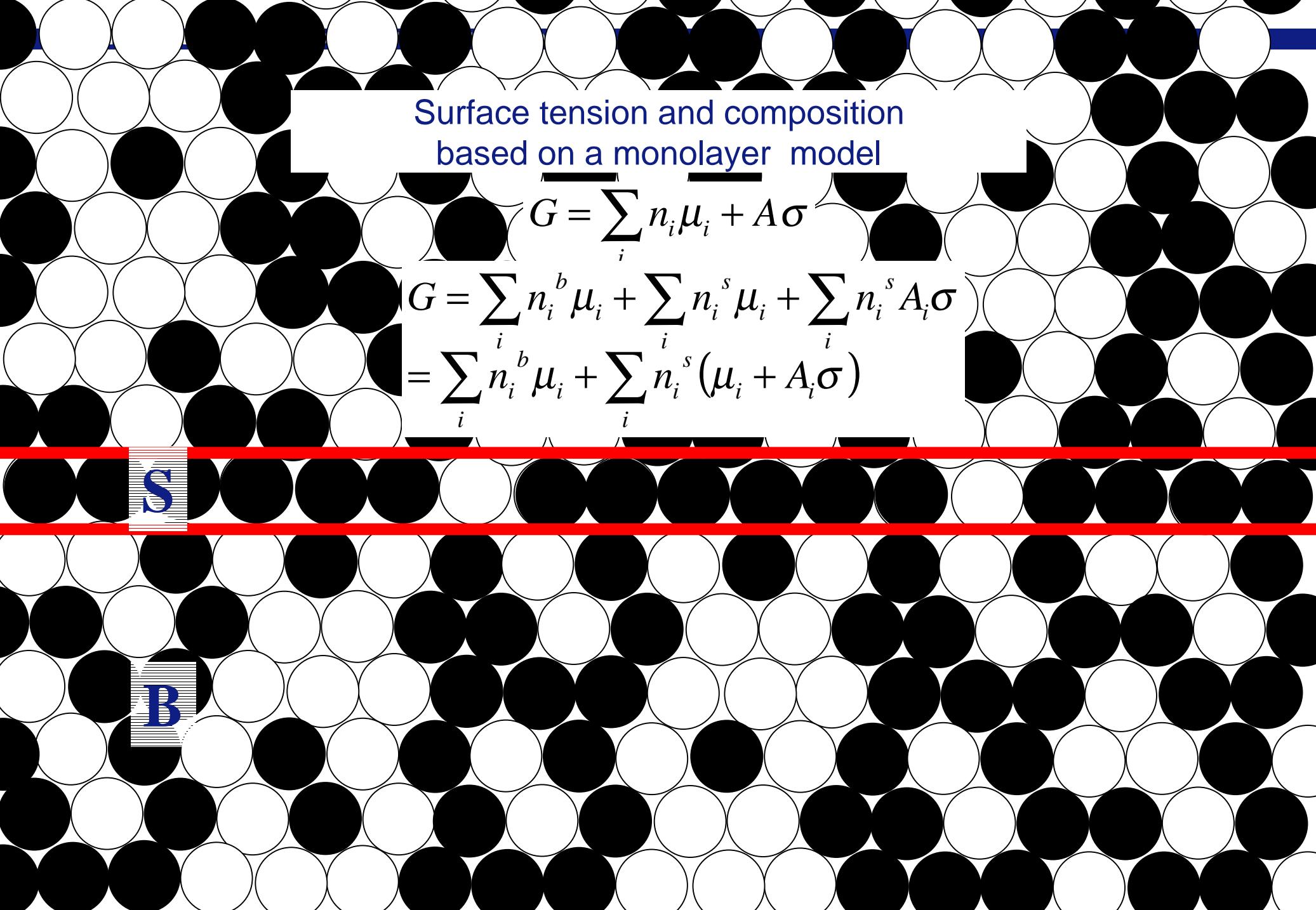
VTT, P.O. Box 1602 FIN-02044, FINLAND

GTT Workshop June 20<sup>th</sup>, 2007



## Multiphase models for (liquid) surfaces and interfaces

- Surfaces and interfaces modelled as one or more layers (phases)
- Strong adsorption can be included as a separate adsorption layer
- Aim to rely as much as possible on bulk thermodynamics (assumed to be known)
- Calculations done ChemSheet (based on ChemApp)



Surface tension and composition  
based on a monolayer model

$$G = \sum_i n_i \mu_i + A \sigma$$
$$G = \sum_i n_i^b \mu_i + \sum_i n_i^s \mu_i + \sum_i n_i^s A_i \sigma$$
$$= \sum_i n_i^b \mu_i + \sum_i n_i^s (\mu_i + A_i \sigma)$$

		Component(1)	Component(2)	...	Component( $M$ )	Area
bulk	Species (1)	$v_{11}$	$v_{12}$	...	$v_{1M}$	0
	Species (2)	$v_{21}$	$v_{22}$	...	$v_{2M}$	0
	:	:	:	..	:	:
	Species ( $N$ )	$v_{N1}$	$v_{N2}$	...	$v_{NM}$	0
surface	Species (1)	$v_{11}$	$v_{12}$	...	$v_{1M}$	$A_1/A_0$
	Species (2)	$v_{21}$	$v_{22}$	...	$v_{2M}$	$A_2/A_0$
	:	:	:	..	:	:
	Species ( $N$ )	$v_{N1}$	$v_{N2}$	...	$v_{NM}$	$A_N/A_0$

( $A_i$  is the molar surface area of species  $i$ ,  $A_0$  a normalization factor with dimensions of  $\text{m}^2/\text{mol}$ )

$$\sigma = \mu_{\text{Area}} / A_0 = (\mu_i^* - \mu_i) / A_i$$

(where  $\mu_i^* = \mu_i^{0,s} + RT \ln a_i^s$ )

(and  $\mu_i^{0,s} = \mu_i^{0,b} + A_i \sigma_i$ )

Modified excess energy expression for the surface layer, such as:

$$G_{\text{Ex}}^b = f(x_1^b, \dots, x_n^b, T)$$

$$G_{\text{Ex}}^s = \beta \cdot f(x_1^s, \dots, x_n^s, T)$$

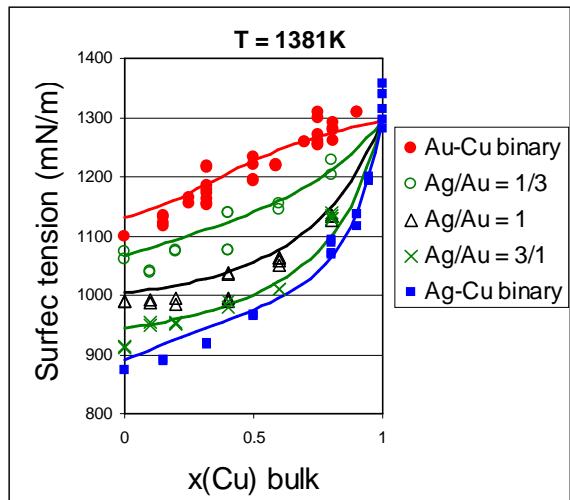
(Total molar Gibbs energy in the surface phase)  
(Standard state for the surface layer)

#### Simple example : Iron – Copper binary

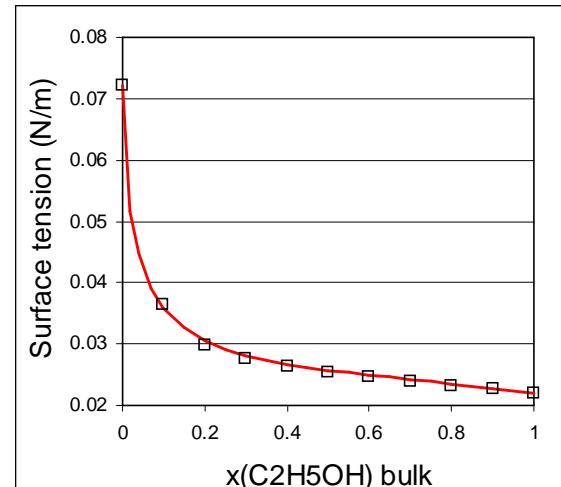
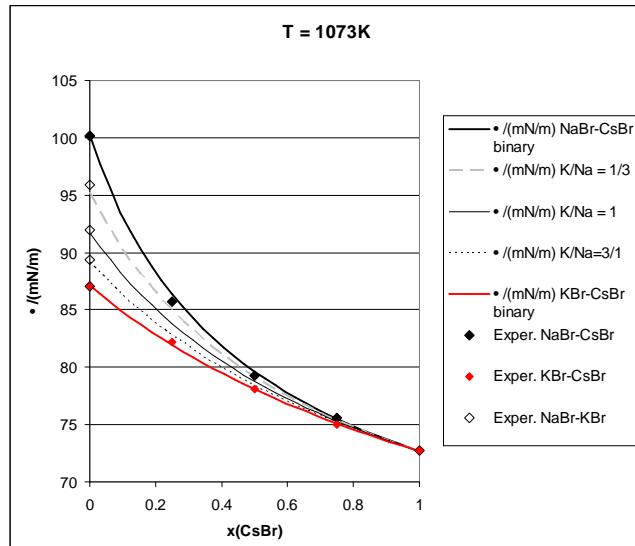
		Fe	Cu	Area
bulk	Fe(l)	1	0	0
	Cu(l)	0	1	0
surface	Fe(l)	1	0	3.672
	Cu(l)	0	1	3.780

## Example cases

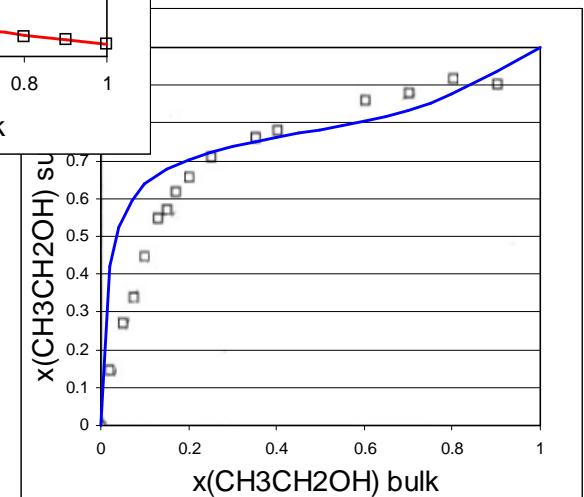
### Binary and ternary alloys: (Ag,Au-Cu)



### Molten salts: (Na/K/CsBr)

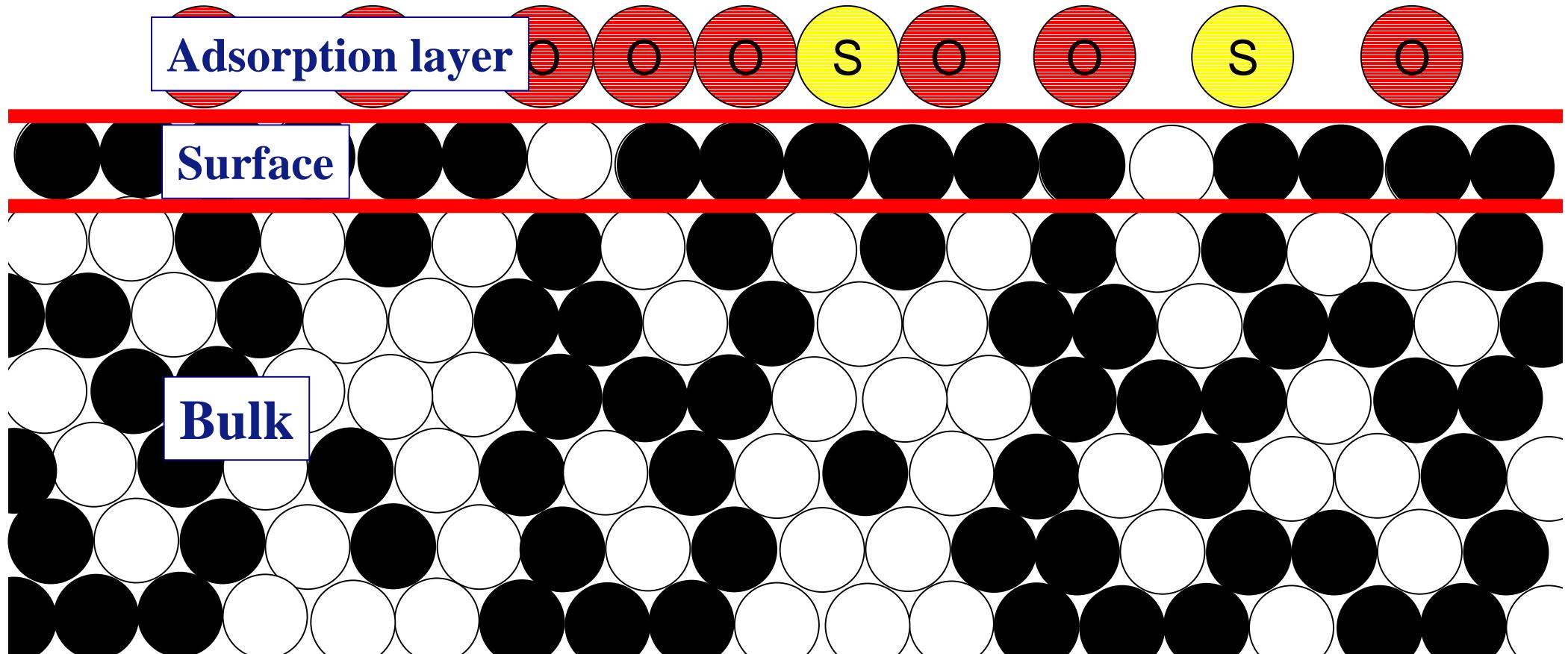


### Organics/aqueous: Ethanol-Water



## The three layer (phase) adsorption model

- Three phases: bulk, surface layer and adsorption layer



## Simple Langmuir adsorption equilibrium model:

	Fe	O	Adsorption location
Bulk	Fe O	1 1	
Adsorption layer	(Fe) <sub>l</sub> (Fe)O		1 1

- Standard states of the species on the adsorption layer have been set using the Langmuir adsorption constant  $\mu_{(Fe)[ ]}^0 \equiv 0$ ,  $\mu_{(Fe)O}^0 - \mu_{(Fe)[ ]}^0 = \mu_{(Fe)O}^0 = \mu_{O_{bulk}}^0 - RT \ln K$  and the total molar amount of adsorption locations based on the maximum adsorbed amount  $n_{\text{Adsorption location}} = n_{(Fe)[ ]} + n_{(Fe)O} = n_{(Fe)O}^{\text{MAX}}$
- Model gives Langmuir model type dependency for the surface coverage as a function of the activity of the adsorbing species
- It can be further combined to surface layer model for calculating the effect of adsorption on surface energy

## Langmuir type model with a surface energy contribution

		Fe	O	Area	Adsorption area
Bulk	Fe	1			
	O		1		
Surface	Fe	1		$A_{Fe}/A_0$	$-A_{Fe}/A_0$
Adsorption layer	(Fe)[]				$A_O/A_0$
	(Fe)O		1		$A_O/A_0$

For basic Langmuir model type behaviour the adsorption layer is modelled as an ideal mixture

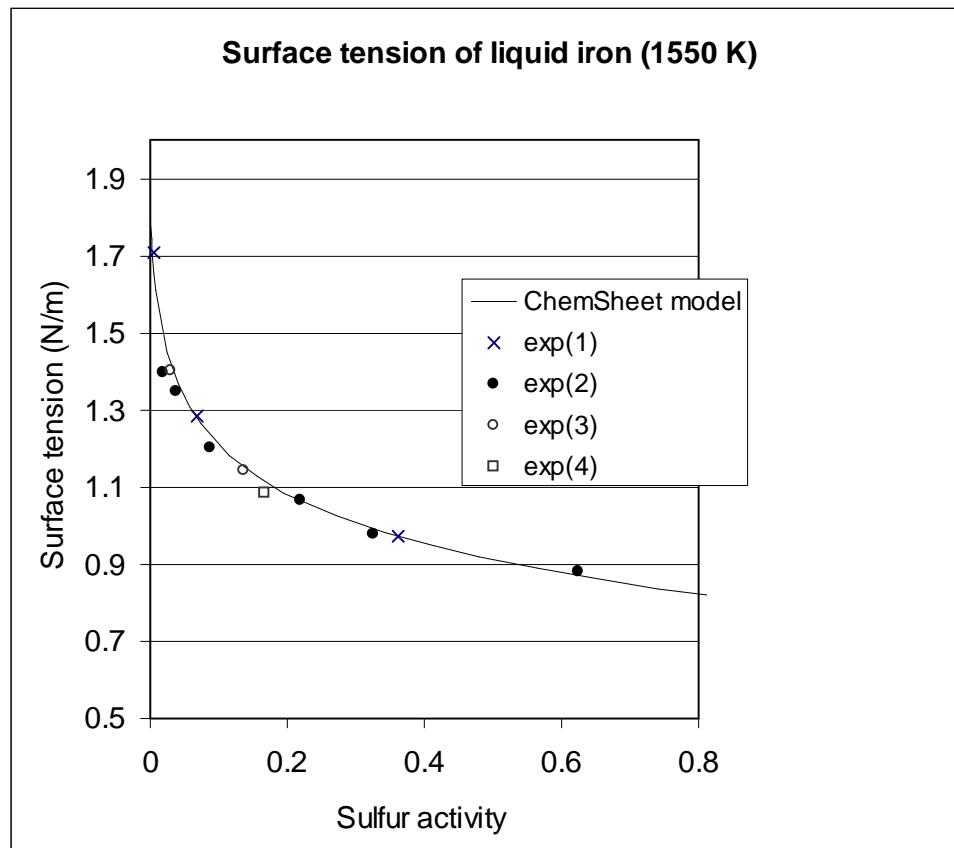
$$\mu_{(Fe)\square}^0 \equiv 0 \text{ (definition)}$$

$$\mu_{(Fe)ads}^0 - \mu_{(Fe)\square}^0 \equiv \mu_{(Fe)O}^0 = \mu_{O_{bulk}}^0 - RT \ln K_O^{ads}$$

$$A_O = \frac{1}{\Gamma_O^{MAX}}$$

$$\sigma \equiv \frac{\partial G}{\partial A} \equiv \mu_{Area} / A_0 = \left( \mu_i^{*(surface)} + \frac{A_i}{A_O} \mu_{(i)\square} - \mu_i \right) / A_i$$

## Example of Langmuir type adsorption (S on liquid Fe)



(Experimental values taken from  
*Metallurgical transactions B* 7B(1976)35)

## System with a mixed solvent

		Fe	Cr	O	Area	Fe-adsorption area	Cr-adsorption area
Bulk	Fe Cr O S	1	1	1			
Surface	Fe Cr	1	1		$A_{Fe}/A_0$ $A_{Cr}/A_0$	$-A_{Fe}/A_0$	$-A_{Cr}/A_0$
Adsorption layer	(Fe)[] (Fe)O			1		$A_{Fe}/A_0$ $A_{O(on\ Fe)}/A_0$	
	(Cr)[] (Cr)O			1			$A_{Cr}/A_0$ $A_{O(on\ Cr)}/A_0$

- Compared to the earlier case there is now one separate ‘adsorption area’ component for each solvent species into which adsorption can happen
- Fe and Cr adsorption places are located in separate sublattices, if non-ideal interactions within adsorption layer are not considered they can formally be divided to two separate phases

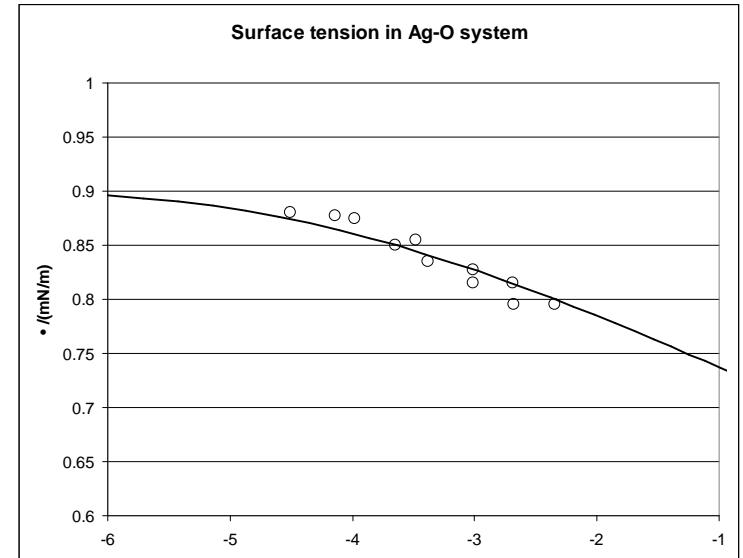
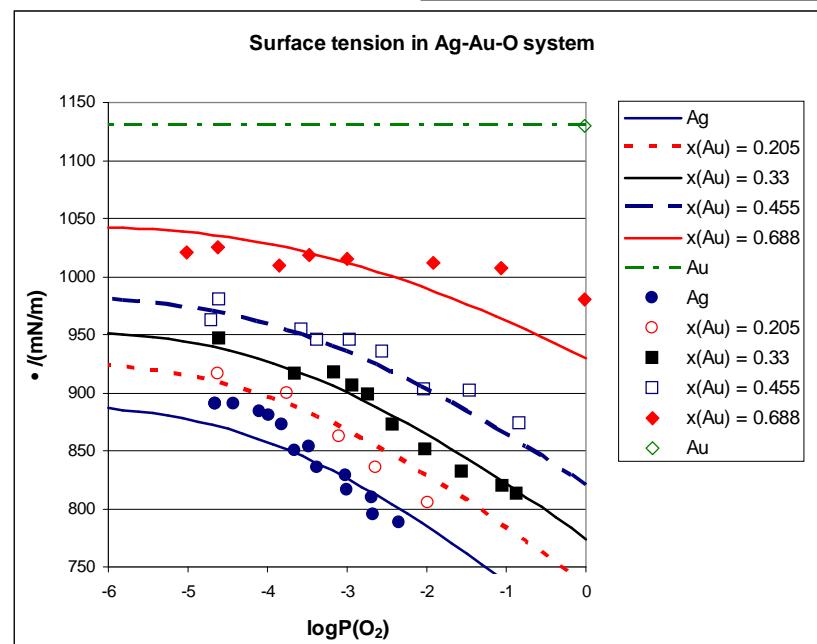
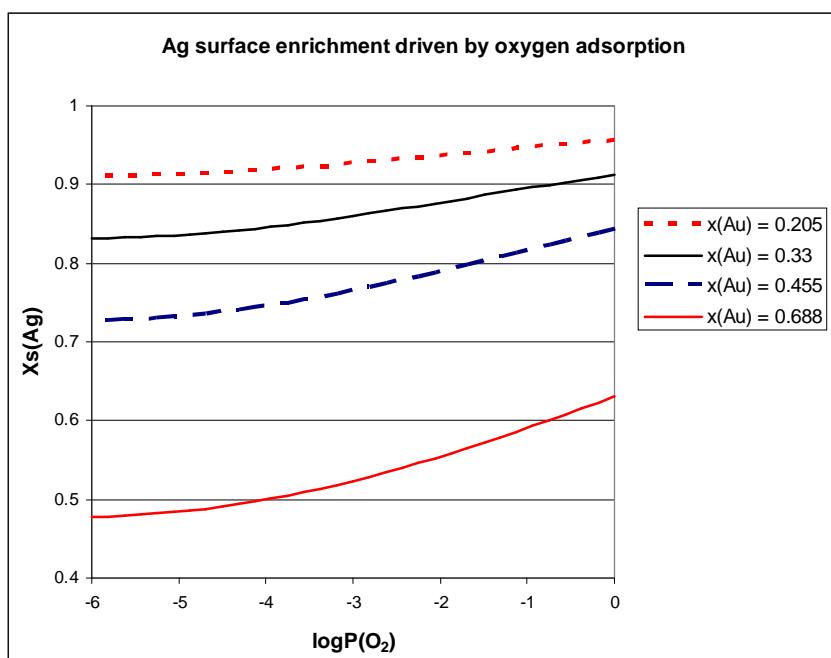
## Competing adsorption of several species (of unequal size)

		Fe	Cr	O	S	Area	Fe-adsorption area	Cr-adsorption area
Bulk	Fe	1						
	Cr		1					
	O			1				
	S				1			
Surface	Fe	1				$A_{Fe}/A_0$	$-A_{Fe}/A_0$	
	Cr		1			$A_{Cr}/A_0$		$-A_{Cr}/A_0$
Adsorption layer	(Fe)[]						$A_{Fe}/A_0$	
	(Fe)O				1		$A_{O(on Fe)}/A_0$	
	(Fe)S					1	$A_{S(on Fe)}/A_0$	
			(Cr)[]				$A_{Cr}/A_0$	
			(Cr)O			1	$A_{O(on Cr)}/A_0$	
			(Cr)S			1	$A_{S(on Cr)}/A_0$	

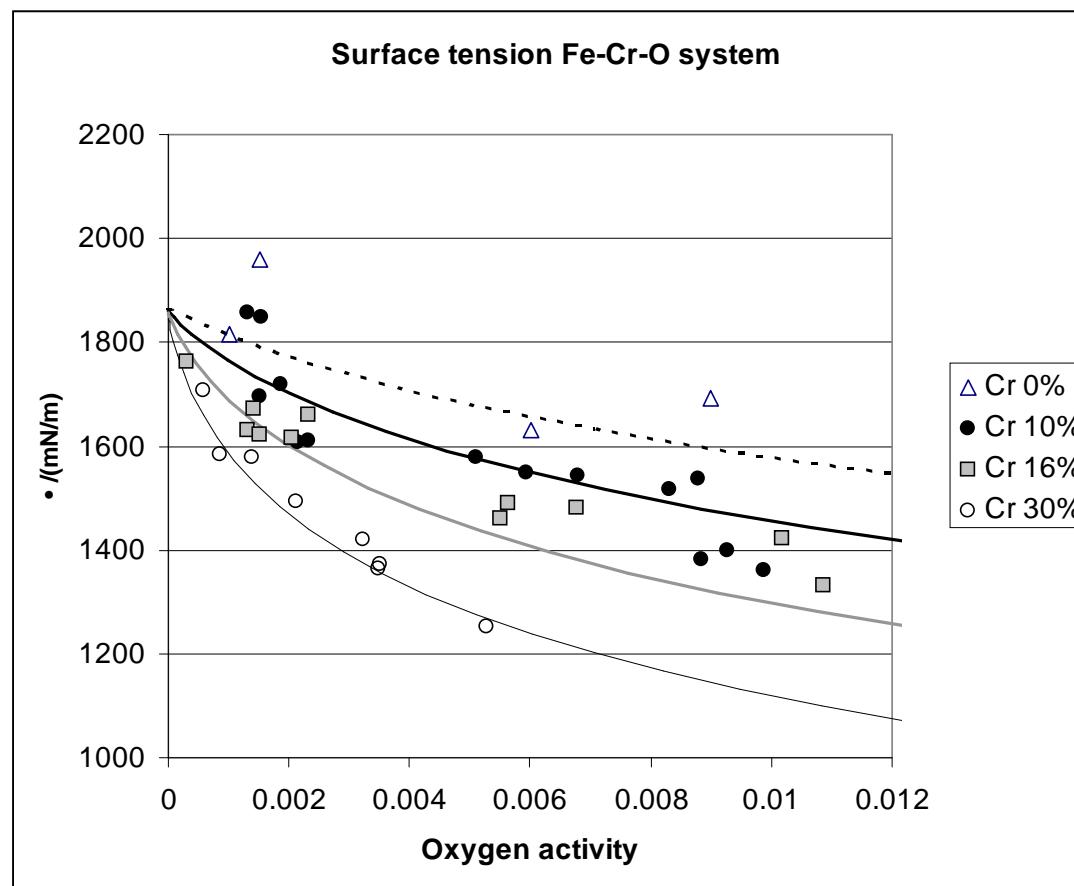
- The ‘Adsorption area’ of an empty adsorption place has been tentatively set same as the surface area of the corresponding metal

$$\sigma \equiv \frac{\partial G}{\partial A} \equiv \mu_{Area} / A_0 = (\mu_i^{*(surface)} + \mu_{(i)[]} - \mu_i) / A_i$$

## Ag+O – Ag/Au+O (1381K)



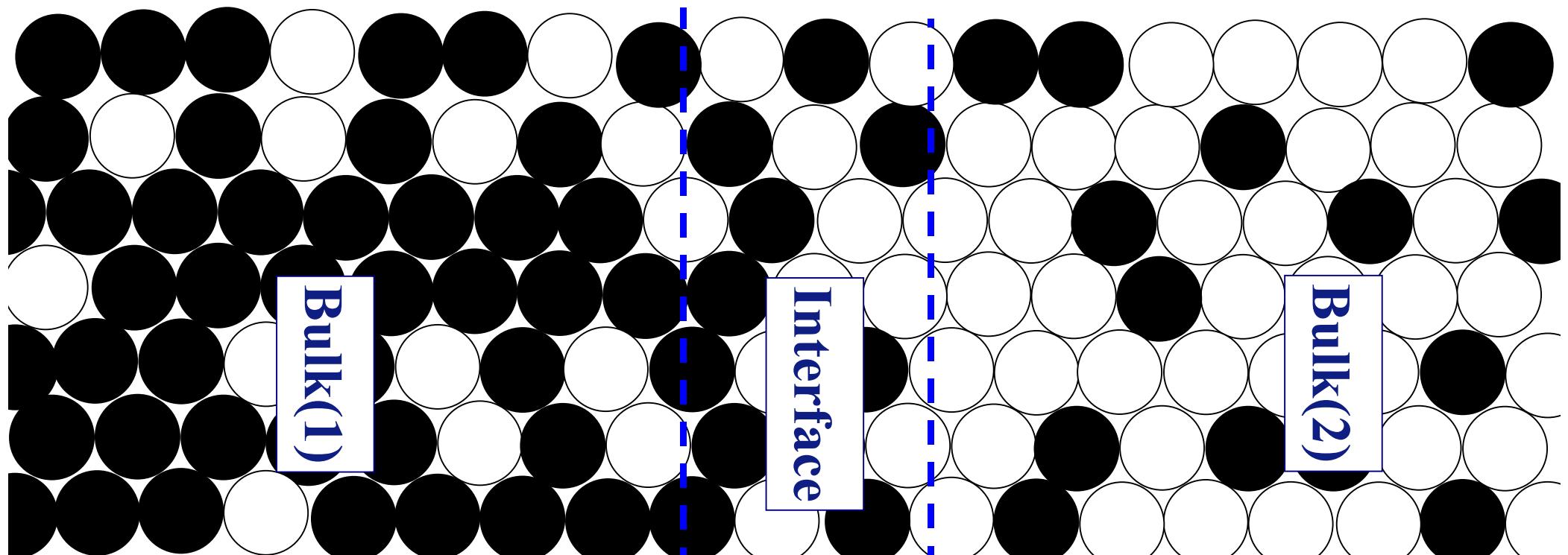
## Fe/Cr/O (1823 K)



Experimental results from Metallurgical and Materials Transactions B, 36 (2005), 241

## Interface model

- Interface modelled as one or more monolayers between two condensed bulk phases



## Matrix representation

		Bi	Al	area
bulk(1)	Bi(l)	1	0	0
	Al(l)	0	1	0
Interface	Bi(l)	1	0	$A_{Bi}/A_0$
	Al(l)	0	1	$A_{Al}/A_0$
bulk(2)	Bi(l)	1	0	0
	Al(l)	0	1	0

$$\begin{aligned}
 G &= \sum_i n_i^{bulk(1)} \mu_i + \sum_i n_i^{bulk(2)} \mu_i + \sum_i n_i^{interface} \mu_i * \\
 &= \sum_i n_i \mu_i + \sum_i n_i^{interface} \text{[blue bar diagram]} \quad \leftarrow
 \end{aligned}$$

from differences in activity  
coefficients/excess energy only

$$= \sum_i n_i \mu_i + \sum_i n_i^{interface} \frac{A_i}{A_0} \mu_{area} = \sum_i n_i \mu_i + \frac{A}{A_0} \mu_{area}$$

$$\sigma^{interfacial} = \pi_{area} / A_0 = (\mu^* - \mu_i) / A_i$$

## Interfacial energy model

- Fundamental requirement for the model is to have a reasonable expression for the activity coefficients in a atomic layer that has neighbouring layer of differing composition
- The actual implementation requires the usage of the *User defined* model features of ChemApp (as rather naturally in none of the GTT supplied ChemApp models is the excess energy of one phase dependent on the composition of another phase)
  - Equation used for activity coefficient for Redlich-Kister model for a system with one interfacial layer

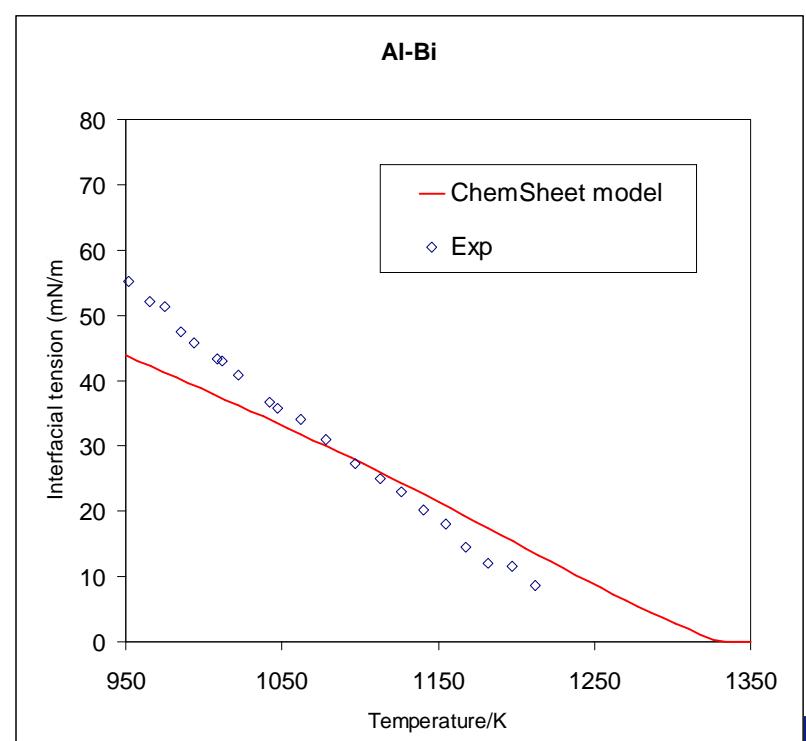
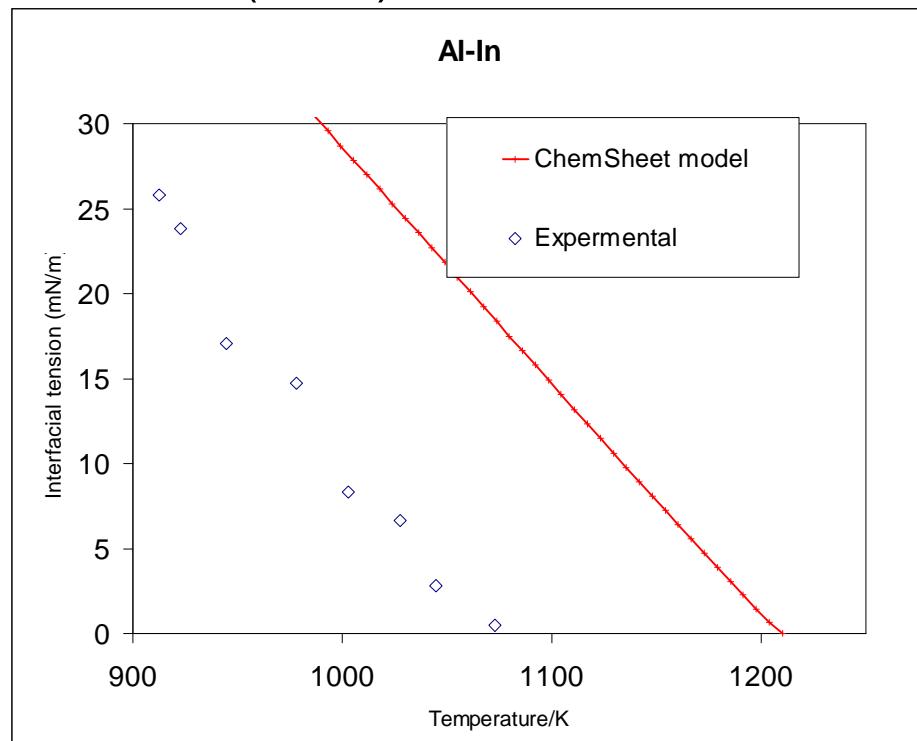
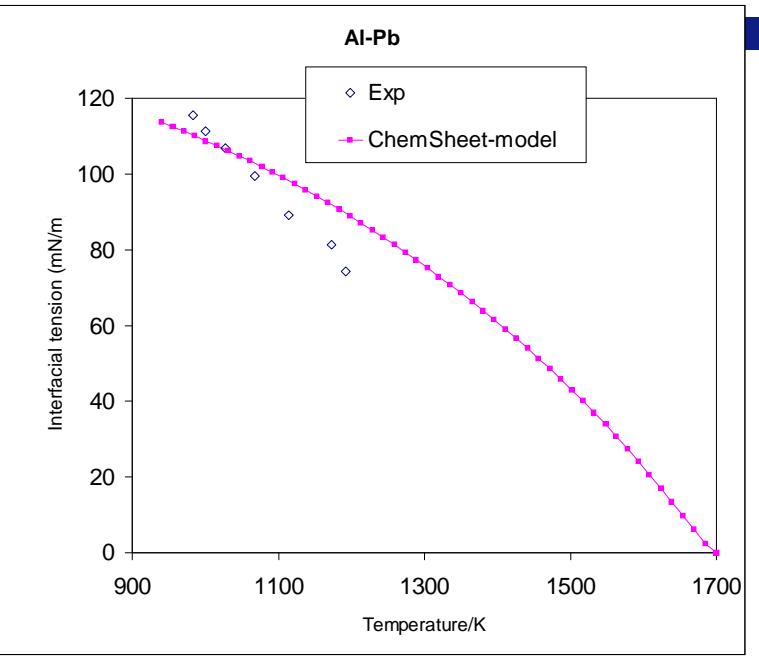
$$RT \ln \gamma_1^i = \sum_j W_j \left[ l(x_2^i)^2 \left[ (x_1^i - x_2^i)^{j-1} + 2(j-1)(x_1^i - x_2^i)^{j-2} x_1^i \right] + m \left[ (x_1^i - x_2^i)^{j-1} \left( (x_2^{b1})^2 + (x_2^{b2})^2 \right) \right. \right. \\ \left. \left. + (j-1)(x_1^i - x_2^i)^{j-2} 2x_2^i \left( 2x_2^i (x_1^{b1} - x_2^{b2}) + x_2^{b1} x_2^{b1} + x_2^{b2} x_2^{b2} \right) \right] \right]$$

(Reduces to the standard form when the bulk phases (and the interfacial layer) are of the same composition

$$RT \ln \gamma_1^i = \sum_j W_j \left[ (l + 2m)(x_2)^2 \left[ (x_1 - x_2)^{j-1} + 2(j-1)(x_1 - x_2)^{j-2} x_1 \right] \right]$$

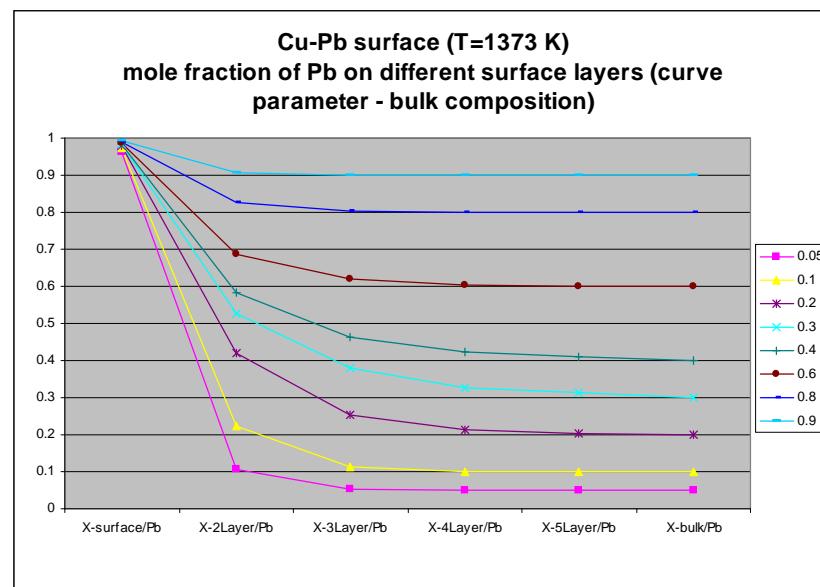
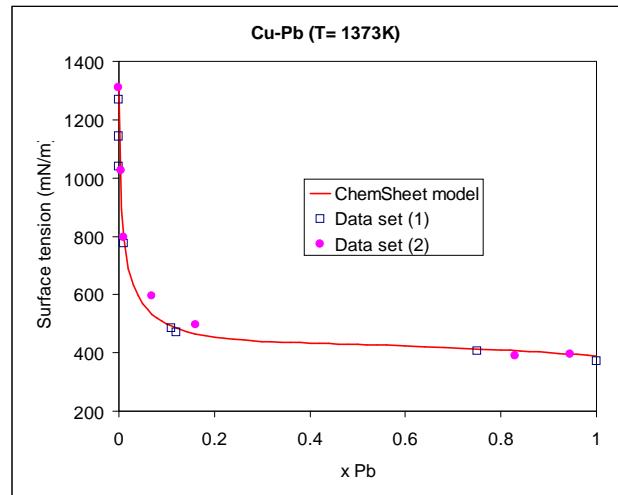
## Example case of liquid-liquid metal interfacial energies

Thermodynamic data from SGTE database  
 Experimental interfacial energy values from  
*Journal of Optoelectronics and Advanced Materials* 5 (2003) 1069



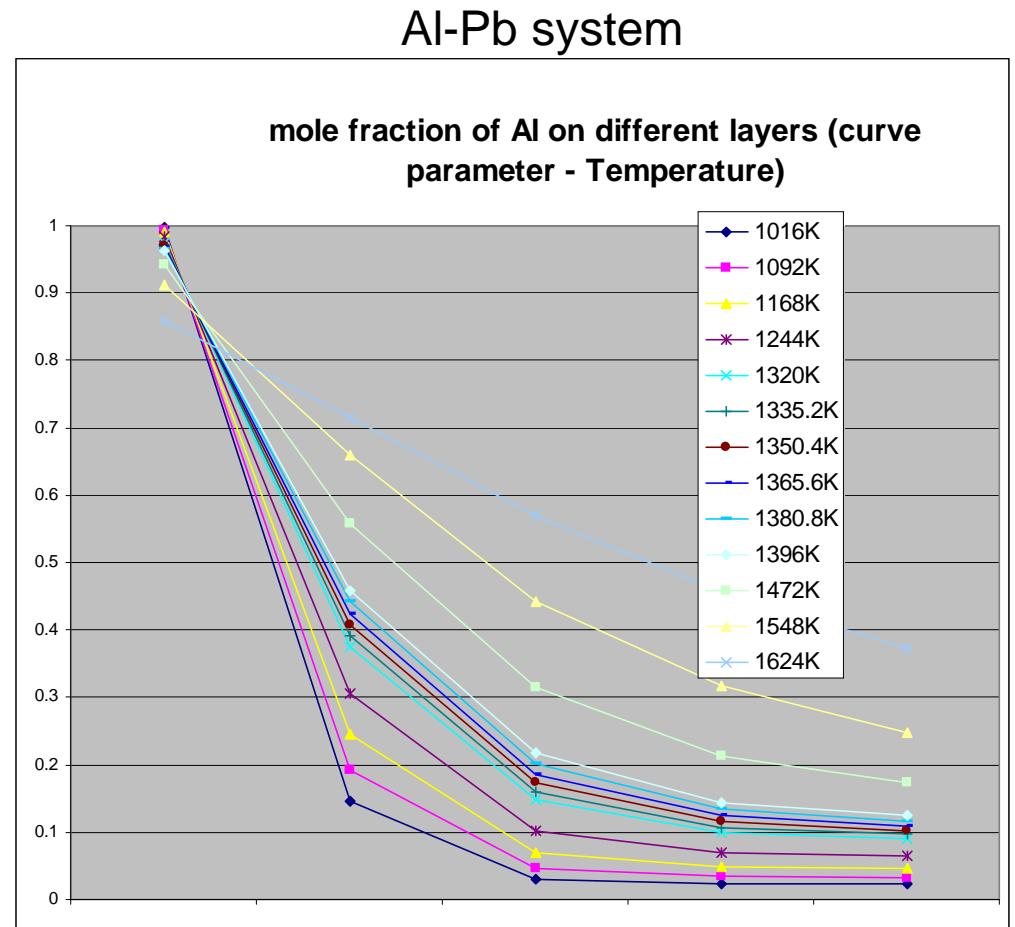
## Extension to more than one surface/interfacial layers

- Requires a model for interacting layers
  - For surfaces, a prediction for the composition as a function of depth is derived; the surface tension values remain practically unchanged



## Extension to more than one surface/interfacial layers

- Requires a model for interacting layers
  - For interfaces, similarly as the composition profiles for the interfacial region are received as a result. The received interfacial energies are (as one would expect) slightly lowered (but here I should actually still actually do some checking of the equations used)



**Thank you for your attention!**